An introduction to logic

Horace William Brindley Joseph

AN INTRODUCTION

TO

LOGIC

.

H. W. B. JOSEPH

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ERRATA

Page 48, notes 1 and 2, for Met. M. read Met. Z. 90, L 82, for osprey read egret

140, note 1, 1, 8, for propietas read proprietas 201, note, 1, 5, for powdum read powdum

215, L 20, for converted read permuted 251, L 28, for If all is P read If all M is P 255, L 20, for affirmative read particular

256, L. 32, for distributed read undistributed 261, L. 20, omit reference to note at end of line

261, note 2, insert at end (40)

272, L 16, for C road B 282, L 25, for B is A read C is A

286, note 1, for Dialect, read Dialectic, 291, ll. 9, 11, 18, 23, for Barbara read Colarent 298, 1, 22, for Some Read Some C

298, 1. 32, for Some B read Some C 325, note 8, 1. 4, for 162* 16 read 158* 16 837, note 2, 1, 18, for 79* 20 read 79* 80

850, i. 9, for the verb read the passive verb 864, last line, for Roman read Greek 865, first line, for Greek read Roman

394, 1. 37, for are not related read are related
401, note, 1. 1, insert comma after reasoning
414. 1. 18. for concidence read coincidence

500, 1. 2, for x read y
518, 1. 11, for attributing it to read attributing to it
564, for Zabarella, Cardinal, read Zabarella, Count.

PREFACE

Is an analogy that precedes it could mitigate an offence. I should be inclined to convert my preface into an analogy for publishing this book Progress and the hone of progress in logical investion. tions have lain perhaps during the last three generations chiefly in two directions, either of analysing more closely the processes of thought exhibited in the sciences or of determining what knowledge is, and the relation of the knowing mind to what it knows. Though I have been compelled to deal in some degree with the first of these questions. I am well aware that it demands a scientific knowledge which I do not possess the second I have not attempted systematically to discuss. The aim of the following book is more modest. There is a body of what might be called traditional doctrine in Logic, which is not only in fact used by itself as an instrument of intellectual discipline, but ought also to be in some degree mastered by those who would proceed to the higher and abstruser problems. It is of this traditional doctrine that Benjamin Jowett is recorded to have said, that Logic is neither a science, nor an art. but a dodge. I could perhaps best describe the motive with which this work was begun, as the desire to expound the traditional Logic in a way that did not deserve this accusation. The accusation was doubtless provoked by the attempt to force into a limited number of forms processes of thought, many of which can only with pretence and violence be made to fit them: an attempt, it may be added, at least as characteristic of 'Inductive Logic' as of any other.

In the course of centuries, the tradition has become divergent, and often corrupt. In this difficulty, I have ventured, like one or two other modern writers, to go back largely to its source in Aristotle. Problems of thought cannot in any case be studied without careful regard to their terminology, and their terminology.

cannot be understood without reference to its history. The terminology of Logic owes more to Aristotle than to any one else; but there is this further reason for attention to what he said, that much prevalent falsehood or confusion in the tradition is a corruption of truths expressed by him. At the same time, I have not pretended to believe in the verbal inspiration of his writings.

I have in particular been anxious to teach nothing to beginners which they should afterwards have merely to unlearn. They may of course come to dissent from the positions here taken up; but only, I hope, because they think I have the worst of the argument on a proper issue, and not because, as meat for babes, I have been deomatically extonucling a knowledged fictions.

While dealing largely with the more technical parts of logical tradition and terminology. I have done my best to avoid a superfluity of technical terms : and the subjects discussed have been for the most part discussed in detail, and the principles involved in them debated. The dryness with which the more formal branches of Logic are often charged springs. I think, in part from their being presented in too cut and dried a manner: those who go beyond the iciune outline, and get into an argument, often find the subject then first begin to grow interesting. At any rate I have tried to secure this result by greater fullness, and attention to controversial issues. In every study there must be something to learn by heart; but Logic should appeal as far as possible to the reason, and not to the memory. Thus such a question as the 'reduction' of syllogisms has been dealt with at length, not from any wish to overrate the importance of syllogistic reasoning, or burden the student with needless antiquarianism, but because the only thing of any real value in the subject of reduction is just that investigation of the nature of our processes of thinking which is involved in asking whether there is any justification for reducing all syllogisms to the first

Topics whose main interest is obviously historical or antiquarian have been either relegated to footnotes or placed in closer type and between brackets; and as I have followed the advice to translate what Greek I quote, I do not think that there is anything in these PREFACE

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discussions which a reader need be altogether precluded from following by ignorance of that language. I have also put between brackets in closer type other passages which, for one reason or another, might be omitted without spoiling the argument; among the matters so treated is the fourth figure of syllogism; for I have reverted to the Aristotelian doctrine of three figures, with the moods of the fourth as indirect moods of the first.

I have that I have sufficiently acknowledged all detailed obligations to previous writers in the places where they occur. But I owe here a more comprehensive acknowledgement both to the published work of Sigwart, Lotze, Mr. F. H. Bradley, and Professor Bosanonet. and to the instruction received in private discussion with various friends. Among these I should like to mention in particular Mr. J. Cook Wilson, Fellow of New College, Wykeham Professor of Logic in the University of Oxford, whose reluctance to write is a source to many of serious disappointment and concern: Mr. J. A. Smith. Fellow of Balliol College: Mr. C. C. J. Webb. Fellow of Magdalen College: Mr. H. H. Joschim, Fellow of Merton College: and Mr. H. A. Prichard. Fellow of Trinity College, Oxford. To the last three of these, and also to Mr. C. Cannan, Secretary to the Delegates of the University Press, I am further indebted for the great kindness with which they read large portions of the work in MS, or in proof: without their suggestions and corrections it would be even more imperfect than it is. Lastly, I have to thank my sister, Miss J. M. Joseph, for the help she gave me in reading the whole of the proof-sheets and in undertaking the laborious and ungrateful task of checking the index.

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CHAPTER I

OF THE GENERAL CHARACTER OF THE ENGLISHY

It is a common practice to begin a treatise on any science with a discussion of its definition. By this means the reader's attention is directed to the proper objects, and to those features of them, with which the science is concerned; a real advantage, when, as in the case of Logic, those objects are not apprehended through the senses, and for this reason ordinarily attract little notice. But the same reason which makes a definition of Logic at the outset useful, makes any controversy about its definition neeless at such an early stage. The reader is too unfamiliar with the subject-matter of his science to be able to judge what definition best indicates its nature; he cannot expect thoroughly to understand the definition that is given, until he has become familiar with that which is defined. The definition will at first guide more than enlighten him; but if, as he proceeds, he finds that it helps to bring unity into the different enquiries upon which he successively enters, it will so far be justified.

Logic is a science, in the sense that it seeks to know the principles of some subjects which it studies. The different sciences differ in the subjects which they so study; astronomy studies the movements of the heavenly bodies, botany the structure, growth, history, and habits of plants, geometry the properties of figures in space; but each attempts to discover the principles underlying the facts with which it has to deal, and to explain the great variety of facts by the help of one set of principles. These principles are often spoken of as laws; and in the physical sciences that deal with change, as 'laws of nature'. The phrase may suggest that 'nature' is not the sum of things and of events in the physical universe, but a sort of power prescribing to these the rules which they are to follow in their behaviour; as the King in Parliament prescribes rules of conduct to his socole. That, however, is

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not what we have to understand in science by a 'law'. a law in science is not like human laws a rule enjoined but sometimes disrecorded . it is a principle illustrated—and existing only in the necessity of its being illustrated in the department of fact to which it belongs. There are therefore no breaches of scientific law or of a haw of nature 1: if events are observed which do not conform to what we have hitherto called a law, we conclude not that the law is broken. but that we were ignorant of the true law: if water for example. were observed to boil on the ton of Mont Blanc at a lower temperature than 212° Fahr. we should infer not that the law that water holls at 212° Fahr was broken but that it is not a law of nature that water boils at 212° Fahr ... that there are other conditions which have to be fulfilled, if water is to boil at that temperature and the 'law' is that it should boil only when those conditions are fulfilled. Such laws, the general principles to which objects in their properties and their behaviour do actually conform. are what the physical sciences seek to discover each in its own department, and if Logic is a science, it must have a department of its own, in which it seeks for principles and laws,

That department is thought, but thought is always thought about something; and thinking cannot be studied in abstraction from anything thought about. But yet in the same way that we may study the laws of motion, as they are exemplified in the movement of all bodies, without studying all the bodies that ever move, so we may study the laws of thought, as they are exemplified in thinking about all subjects, without studying all the subjects that are ever thought of. This comparison may be pushed further. Just as we must have experience of moving bodies, before we can investigate the laws of their motion, so we must have experience of thinking about things, before we can investigate the principles of thinking; only this means, in the case of thinking, that we must ourselves think about things first, for no one can have experience of thinking except in his own mind. Again, although, in studying the laws of motion, we do not study every body that moves, yet we must always have before our minds some body, which we take as representing all possible bodies like it; and in the same way, when we investigate the principles that regulate our thinking, though we do

¹ The question of the possibility of a breach of natural law need not be considered here; something is said of it in c. xix, infra.

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not need to study all subjects ever thought of, we must have before our minds some subject thought of, in order to realize in it how we think about it and all possible subjects like it. For example, it is a general principle of our thought, that we do not conceive of qualities except as existing in some subject; and that nevertheless the same quality is regarded as existing in many subjects; green is a quality, which exists not by itself, but in grass and leaves of trees and so forth; at the same time, green may exist in many different leaves or blades of grass. The general principle which is thus illustrated in the case of the quality green is readily understood to be true of all possible qualities; but unless we were able to think of some particular quality to illustrate it, we could not understand the convent principle at all.

What has been now said will serve to remove an objection which Locke brought against the study of Logic, 'God,' says Locke !. thes not been so spering to men to make them harely two-legged creatures and left it to Aristotle to make them rational.' He is urging that men thought rationally, or logically, i. e. in accordance with the principles that Logic discovers to regulate all sound thought. long before those principles were recognized; and that this is still the case with each of us : we do not therefore need Logic to teach ne how to think. That is onite true, and would be a pertinent criticism against any one who pretended that no one could think rationally without studying Logic: but it is not the object of Logic to make men rational, but rather to teach them in what their being rational consists. And this they could never learn, if they were not rational first: just as a man could never study (say) the principles of voluntary motion, if he was not first accustomed to move his limbs as he willed. Had God made men barely two-legged creatures. Aristotle would in vain have taught them to be rational. for they would not have understood his teaching.

Togic, then, is the science which studies the general principles in accordance with which we think about things, whatever things they may be; and so it presupposes that we have thought about things. Now our thought about them is expressed partly in the daily conversation of life or musings of our minds; partly and most systematically in the various sciences. Those sciences are the best examples of human thinking, the most careful, clear, and coherent,

that exist. In them, therefore, the logician can best study the laws of men's thinking and it is in this sense that we may accent the old definition of Logic evientia evientiarum. What the commen of the stars' are to astronomy, what figures are to geometry, what plants are to botany, or the calendar of Newgate to the criminologist, that the other sciences are to the logician they are the material which he has to investigate, the particular facts which are given him, in order that he may discover the principles displayed in them. He has to sak what knowledge is as knowledge apart -so far as possible-from the question, what it is about : and he must therefore examine divers 'knowledges', and see in what they are alike; and the best pieces of knowledge that exist the best 'knowledges', are the various sciences. But he is not concerned with the detail of any particular science; only with those forms of thinking which are exemplified in all our thinkings-though not necessarily the same in all-but best exemplified in the sciences.

It is important to understand what is meant by saving that Logic is concerned with forms of thinking : for many logicians who have laid stress on this, and pointed out that Logic is a formal science, have understood by that expression more than seems to be true. There is a sense in which Logic is undoubtedly formal. By forms we mean what is the same in many individuals called materially different—the device, for example, on different coins struck from the same die, or the anatomical structure of different vertebrates, or the identical mode in which the law requires the different Colleges of the University to publish their accounts. And all science is formal, in the sense that it deals with what is common to different individuals. A scientific man has no interest in a specimen that is exactly similar to one which he has already examined; he wants new types, or fresh details, but the mere multiplication of specimens all alike does not affect him.2 So the logician studies the forms of thinking, such as that involved in referring a quality to a subject possessing it; but when he has once grasped the nature of this act of thought, he is quite uninterested in the thousand different occasions on which it is performed during the day; they differ only materially, as to what quality is

Joannes Philoponus cites it ad Ar. Anal. Post. a. ix. 76° 15.
 Unless indeed he is collecting statistics as to the comparative frequency of different types.

referred to what subject; formally, so far as the notion of a quality as existing in a subject is concerned, they are the same; and the forms that run through all our thinking about different matters are what he studies. But those who have insisted most that Logic is a formal science.

or the science of the formal laws of thought, have not merely meant that Logic is in this like other sciences, which all deal with

what is formal or universal in their subject-matter. They have meant to exclude from Logic any consideration of forms or modes of thinking which are not alike exemplified in thinking about absolutely every subject. It is as if the botanist were to repard only those laws which are exemplified in every plant, or the geometer were to consider no properties of figures, except what are common to all figures. They have thought that one might abstract entirely from and disregard all question as to what he thinks about, and still find that there are certain principles in accordance with which, if he is to think about anything, he will think. But the truth is that we think in different wave about different kinds of subjects and therefore we must if we wish to study the principles that regulate our thinking consider to some extent the differences in the matter about which we think. The distinction between form and matter may as it were be taken at different levels. This is plain in the case of a science that deals with some order of sensible things, like zoology. We may say of all men and all horses that they have severally a common form. that as compared to a man a horse is formally different, but as compared to one another all horses are formally the same, though each horse in his body is materially different from every other. Or we may consider not the form of horse common to Black Bess and Bucephalus and Rosinante, but the form of vertebrate common to man, horse, eagle, crocodile, &c.; and now man and horse (as compared with ovsters for example) are formally alike. Or we may take the four orders in Cuvier's division of the animal kingdom, vertebrata, coelenterata, radiata, and annulosa, and regard them as only different examples of the common form of animal: and from this point of view a horse and an oveter differ materially. but not formally. When however we have reached this stage, and formed the conception of animal, as something exemplified equally

in kinds of animal so different, it is clear that we can only under-

stand what animal nature means by seeing it as it exists in all the different orders of animals; whereas we can understand fairly the nature of a vertebrate animal without seeing it as it exists in every genus of vertebrates atill more can we understand the nature of a horse without familiarity with all horses. The higher the level therefore at which in Zoology the distinction between form and matter is taken, the less can we study the form in isolation: no example taken from one order of animals, say the starfish, will enable us to realize what animal means. It is the same in studying the forms of thought. The most general forms of thought exist diversely modified in thinking about different matters; and they can no more be fully known without attending to the different matters in which they appear differently, than animal nature can be fully known without attending to the different orders of animal in which it appears differently. Thus we may take the Proposition, and point out that in every proposition there is a subject about which something is said, and a predicate or something which is said about it. This is true consily of the propositions 'A horse is an animal' 'First-class railway tickets are white,' and 'Londres is London'. We may if we like, because in all propositions there is formally the same distinction of subject and predicate, take symbols which shall stand for subject and predicate. whatever they are and say that all propositions are of the form 'S is P'. But when we sak for the meaning of this form, and in what sense S is P. it is clear that the meaning varies in different propositions. Londres is just the same as London : but a horse is not just the same as an animal; it may be said that 'animal' is an attribute of horse, and 'white' of first-class railway tickets. but animal is an attribute belonging to horses in quite a different way from that in which white belongs to first-class railway tickets: these might as well be any other colour, and still entitle the holder to travel first-class by the railway; a horse could not cease to be an animal and still continue to be a horse. The meaning of the formula S is P cannot possibly be fully known merely by understanding that δ and P are some subject and predicate: it is necessary to understand what kind of subject and predicate they are, and also the relation between them, and in what sense one is the other: and if this sense is different in different cases, just as animal is something different in a dog and a starfish, then the

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thorough study of the form of thought involves the consideration of material differences in the subjects of thought. But logicians who emphasize the purely formal character of Logic maintain that it can exhaust the form of thought in treating that as one and the same in every possible matter of thought; an impracticable task, because the form itself (as in the above instance of the form of

it can exhaust the form of thought in treating that as one and the same in every possible matter of thought; an impractisable task, because the form itself (as in the above instance of the form of thought which we call a proposition) is modified according to the matter in which it appears. On the other hand, and even although the forms of our thought cannot be studied apart from the particular sort of matter about which we may think, yet Logic is not interested in the variety of the matters that we think about for their own sake, but only for the sake of the divers forms of thinkine involved in them: and each as at the same form is

exemplified over and over again in different particular 'bits' of thinking, the study of the common form alone belongs to Logic.

[The truth that form cannot be studied apart from matter might be otherwise expressed by saying, that the general form can only be studied in connexion with the special forms in which it is manifested; and these special forms can only be illustrated in examples that are materially different from one another. The proposition 'Londors is London' is a special form of proposition

proposition 'Londres is London' is a special form of proposition equally well exemplified in 'Köln is Cologne'; as Bucophalus is an animal of a special form equally well exemplified in Black Bess. What is important to realize is the need of following the common form out into the differences which it displays in different matter.] The foregoing discussion will probably become plainer if it be read again at a later stage, when the reader is more practised in reflecting on his thoughts. A distinction which is readily seen in material objects, like medals from a common die, is not so easily seen in immaterial objects, like our thoughts. The natural man thinks much about things, and asks and answers questions about them: but it is by an effort that he comes to see how these things are only known to him in his perceptions of them and his thoughts about them, and so comes to turn his attention inward upon the nature of the acts of perceiving or of thinking. Nor can these new objects of his study be preserved and dissected like a material thing: a man cannot catch a thought and bottle it; he must create it by thinking it, if he wishes to think about it; and the task will be found difficult while it is strange.

[Mediagral logicians cometimes my that Logic deals with second intentions: by this is meant what has been pointed out in the last paragraph. The mind intends or directs itself at first upon material objects: and these are its first intentions: it may afterwards intend or direct itself mon its own modes of thinking as exhibited in its first intentions; and what it then discovers are its second intentions. Thus we observe animals, and give them names according to their kind calling them stag and ox worm and lobster; and again we observe how these kinds agree and differ. and call some vertebrate and some invertebrate but all animals; and all these names, which are names we give to objects. are names of the first intention. But we may also observe how we have been thinking about these animals, as having some properties common to all, and some neculiar to the members of each kind: and we may call the members of each kind a species, and the members of the several kinds together a genus; and genus and species are names of the second intention. The unity on the strength of which we call them of one species or of one genus may indeed be something in the animals themselves; and so our names of second intention will signify something real in things. The distinction therefore presents difficulties.

If now we sak for a definition of Logic, to keep before our minds in the following chapters, perhaps it is simplest and least objectionable to call it the Science, or the Study, of Thought; for to say of the Formal Principles of Thought might imply both that there were sciences which did not seek for principles, and that the form of thought can be studied without reference to differences in the matter of it; neither of which things is true.

It is sometimes held that Logic is rather an art than a science, or at any rate that it is an art as well. In considering the question, we must remember that there are two senses of the word art. We may say that a man understands the art of navigation when he is skilful in handling a ship, though he may be unable to explain the principles which he follows; or we may say that he understands it, when he is familiar with the principles of navigation, as a piece of book-work, though he may never have navigated a ship. Thus an art may either mean practical skill in doing a thing, or theoretical knowledge of the way it should be done. In the latter sense, art presupposes science; the rules of navigation are based upon a knowledge of the motions of the heavens, the laws of hydrostatics, and the build of ships. It is in this sense that Logic is called an art; and hence it is clear that if there is an art of

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Logic, there must first be a science, for the study of the nature of sound thinking must precede the giving of instructions for thinking soundly. And even granting the existence of such an art it remains distinct from the science : so that the name Tooic would be used of the two in different senses and we quest rather to say that Logic means the science or the art of thought than that it is the science and the art thereof. That there is an art of Logic based on the science of Logic might be projed on the ground that Logic reveals to us our own ideal of what knowledge about any subject must be, and certain canons of reasoning which no sound aroument can violate. But though we may thus prescribe to ourselves the conditions which should be fulfilled in science or in common thought, we are not thereby enabled to fulfil them: for art, as a theoretical knowledge of what is to be done, does not always bring the art or practical skill of doing it. An art of Logic would therefore be no infallible means of coming to know about all subjects: it is against that sort of pretension that a protest like Locke's, quoted above, may well be made; and yet the rules and the ideals which the study of Logic suggests are not without value in keeping our thoughts about things straight.

think about things. But a good deal of our so-called thinking is incoherent, and breaks down when we criticize it. That we can discover for ourselves without learning Logic; an economist can correct his own or his predecessor's errors in political economy, a mathematician in mathematics; they could no more wait for the logician to correct than to construct these sciences.\(^1\) Yet the study of the thinking, good and bad, which has gone to their construction may give us a more lively consciousness of the difference between what its character should be and what it sometimes is, or as the Greeks would have said, between knowledge and opinion. Herein Logic may be compared with Ethics. Ethics investigates human conduct; it discusses the judgements of right and wrong, of good and evil, that we pass upon men's acts and them; it tries to determine what we really mean in calling an act wrong, and what

We have said that Logic studies the way in which we already

¹ The word logic is sometimes used not for the study of thought which has been described in this chapter, but for the thinking which it studies: as when we say that some one is a man of powerful logic, or of great logical acumen. It is important to recognize that this is a different sense of the word.

we really require of a man in saying he should do what is right. All this would be impossible unless men already acted wrongly and rightly, and made moral judgements; Ethics does not teach men to do that. But it does bring into clearer consciousness the nature of the ideals which we already have, the grounds of the judgements which we already make, the frequent discrepancy between what is done and what we recognize should be done. To this extent Ethics tells us what to do, though it does not enable us to do it. Similarly Logic helps us to realize what knowledge of a subject means: but it does not enable us to bring our opinions on every subject into the form that knowledge requires. Both Logic and Ethics are thus in some degree practical; but we do not call Ethics an art, and it is not desirable any the more to call Logic act.

It is perhaps from a desire to show the practical value of the study of Logic that men have insisted on viewing it as an art. But it would be a mistake to suppose that its practical value can lie solely in its furnishing rules for 'the conduct of the understanding'. The direct help that it can give in this way is not very great. Its practical value in general education is firstly this; that it demands very careful and exact thinking about its own subject-matter, and thus tends to produce a habit of similar carefulness in the study of " any other subject. In this it only does for the mind what a thorough training in any other science might do. Secondly, it makes us , realize better what the general forms of speech that we habitually use really mean, and familiarizes us with the task of examining our reasonings and looking to see whether they are conclusive. In this it has an effect which the study of some special science like botany is not equally calculated to produce. Thirdly, it brings into clearer consciousness, as aforesaid, our ideal of what knowing is, and so far furnishes us with a sort of negative standard : it makes us more alive to shortcomings in our ordinary opinions. But its chief value

· lies in its bearing upon those ultimate problems, concerning the

¹ It must not however be supposed either that Ethics can determine what coght to be done in very difficult case of conceines, or that Logic determines exhaustively the forms of reasoning which the sciences must employ. Of. Bridley, Logic, p. 247-249. The phrase normatics science, which some writers have of slate applied to Logic, Ethics and Aesthetica, has perhaps been suggested by size character in them to which this paragraph of these enquiries to pragride mather than to asceptain the principles which our raisonal thinking, or action or appreciation of beauty exhibits.

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nature of reality, and man's place and destiny in the world, from which at first sight it might seem far remote. 'Logic,' save J. S. Mill. in the Introduction to his famous work 1, 'is common ground on which the partisans of Hartley and of Reid, of Locke and of Kant may meet and join hands.' Conserers manus—it is only in this sense that rival schools join hands on the field of Logic. The dream of a Logic that shall be 'neutralized' like the physical sciences will not be fulfilled. These may move securely within the limits of certain well-defined assumptions, which all workers, though they may fight over minor points, sores to respect. Logic, which studies the principles of our thought about all things. cannot be content to leave unquestioned the sesumptions within the limits of which it thinks: for it is those very assumptions that it investigates. The history of Mill's own work disproves his saving. for it is on its metaphysical side that it has been most vehemently attacked. Into such controversies, however, it is not the aim of this book to enter. It would be absurd to pretend that the treatment of many topics in it does not rest upon a metaphysic which some would reject, and of which the rejection would mean the restatement of what is written here. But he would essay a vain task, who should attempt to expound the rudiments of Logic with no metaphysical presuppositions: therefore it is better not to conceal them . but though the points at which they are most important will be indicated, they will not be discussed as they deserve

CHAPTER II

OF TERMS, AND THEIR PRINCIPAL DISTINCTIONS

We have to study the principles which regulate our thinking shout any subject and these can only be discovered by examining our various particular thoughts. Now the true unit of thought. the simplest complete act of thought or piece of thinking, is the Judgement, or Proposition: between which, if a distinction is ever intended, it is that the proposition is the expression in words of a indocement, and unless a judgement were expressed in words, we could not study it. This does not mean that it need be uttered aloud, or written down, though these may be helps to us in fixing our attention : but we must express it mentally to ourselves in words or in a proposition, if it is not to evade us. The judgement being thus the unit of thought, it might be expected that Logic should begin with a discussion of judgement; but it is more usual to begin with the elements of judgement, viz. terms. It is, however. only through its place in a judgement that we can understand what is meant by a term. When that has been explained, it may then he convenient to discuss the doctrine of Terms before ressing to a fuller consideration of Judgement.

To judge, in the logical sense of the word, is not to acquit or condemn, but to affirm or deny a predicate of a subject. It is easy, bewerer, to see the connexion between the two user of the word; for when I judge, in the logical sense, I decide with myself what is, or is happening. 'Vengwance belongeth unto the Lord;' Sweet are the uses of adversity,' xaxerà rà xaxá, Baloss accificat, are all judgementa. In each I recognize a matter of fact, and what I recognize in each is different.' But in the matter of fact there is a distinction seen when I under between the subject and the

Of course judgements with the same subject may have different predicates, and those with different subjects may have the same predicate. Yengence is sweet.

predicate . for I recognize comething in particular as characterizing the object of thought already before ma! Subject and predicate unite with one another in the chiect and we are aware that because distinguished they are not separate as the words that indicate them are in our proposition. Nevertheless the indeement admits of analysis into those two factors as has been already said. Subject and predicate (Gr. imprefuence and corresponduence), as the parts into which it is analysed, are called the terms of the judgement.

From this it will be clear that a term is not the same as a word : a proposition may contain any number of words; but one judgement never contains more than two terms. Subject and predicate may be expressed each in a single word, as in the proposition 'Tastes differ': more commonly each requires several words, as in 'Dead men tell no tales': while sometimes, on the other hand, a single word expresses both. Caesar's famous message of three words, 'Veni, vidi, vici,' containing as many distinct propositions. each of which may be howen up into the subject term 'I' the same in each, and a predicate-term which is different. Again. some words are not normally canable of signifying the terms of a indocement at all : they do not indicate by themselves any object of thought, but are either used, like an article, in conjunction with some descriptive word, to designate an object, or like an adverb, to qualify what another word expresses, or like conjunctions and prenositions, to indicate a relation between different parts of a com-

1 This statement needs modifying in the case of independents which define their subject; but in these also there is a distinction between the subject as an unity, and the elements composing it

⁸ Oper καλώ els δε διαλύτται ή πρότοσις Ar. Anal. Pri. a. i. 24⁵ 16. 'Term' is terminas, a translation of the Greek δρος. It is not quite easy to see why the parts into which the judgement can be broken up were called open The statement that 'a term is so called because it forms one end of a proposition' (Jesone) is clearly wrong; for that is an accident of language, and sition' (Jesses) is clearly wrong; for that is an accident of language, and of the proposition be locates set it is not tree. It is possible that Arntottle symbolized tha proposition in the form: B—A. (where we should write symbolized that proposition in the form: B—A. (where we should write symbols. Benink to the state of the s which might therefore be called son too. The word is, however, also used like dopents, to mean definition; and it may be that subject and predicate were called son as the determinate objects of our thought in a particular judgement, or as together comprising what is propounded, and limiting UB judgement in which they occur to its own field. plex object of thought.1 Such words are called syncatecorematic (συνκατηνοσηματικά) because only capable of being used along with others in predication: while words which signify what can by itself he a subject or predicate in thought are called categorematic. These indeed, while canable of being used by themselves for terms. may also enter into a term as one of the words of which it is composed: thus man is a term in the proposition 'Man hath found out many inventions', but not in the proposition 'The heart of man is deceitful': the sea in the proposition 'The sea shall give up its dead', but not in the line 'She left lonely for over the kings of the sea. In this line the words italicized are syncategorematic: but see is not syncategorematic, because it can stand for a term, though here it does not do so. Terms composed of words of both kinds have been called 'mixed terms'. It is true that syncategorematic words, though signifying nothing about which anything can be asserted, or which can be asserted of anything, can vet as words be made the subject of linguistic or grammatical discussion, as when we say 'Of is a preposition', or 'is the sign of the cenitive case in English'. When words which signify no complete object of thought are made objects of our thought themselves as words, it is said to be by a expositio materialis.2

¹ With the acticles may be coupled words like sees and say; set, and on it was mean to recompensatio; so it be copula on as the sign of predication, though not when it means 'exista' and is itself the predicate. 'The doctrine of suppositio, so of divers other 'properties of fearns', has happily fallen into oblivion; but for the benefit of any one who wishes to an acceptance of the supposition of the sees of the supposition; then, as counds possessing signification, they sequired proparties which did not bong to them as mere sounds. These properties were not the same for every part of speech. Suppositio belonged to substantive denoting substantive and the supposition of the supposition of the same for every part of speech. Suppositio belonged to substantive denoting substantive and the supposition of the suppositio

Some logicians have preferred to speak of sames, rather than terms, or have been ready to apply to a term Hobbes's wellknown definition of a name. 'A name.' he says, 'is a word taken at pleasure to serve for a mark, which may raise in our minds & thought like to some thought we had before and which being pronounced to others, may be a sign to them of what thought the speaker had or had not before in his mind. This definition admirably expresses the function of a name though it covers many expressions that contain more than one word . but it is not equally appropriate to define a term. For the name not is but significal the term. A term is properly one of the elements into which the object of our thought is analysed when we break up the judgement: a name is the mark which serves to fix and recall these elements in the object of our thought. The name belongs to the expression of our thought in language; but thought itself is not made up of, and is not generally about, names. We shall therefore commonly speak of terms, and not of names. Nevertheless, by term will sometimes be meant the same which signifies the term. For example, when it was said that in the proposition 'The heart of man is deceitful' man entered into the subject-term as one of the words of which it is composed, it would have been more accurate to say that it entered into the name (or phrase) which signified the subject-term. But we may consult brevity by the other expression without serious risk of confusion : for the name and the object of thought which it signifies are obviously different, and it is easy to know in which sense 'term' is meant in any context. Usage has sanctioned the application of the word 'term' both to the object thought of, and to the verbal expression for it; this usage extends beyond Logic into common speech and more difficulties would probably be caused by departing from than by acquiescing in it."

or in respect of its matter, as in 'Homo est disyllabum', it was said to be or in respect or te matter, as in "count out they man, "it was man, in the same property of the property of th

[&]amp;c.; it is less natural to speak of the name of a quality, or to call a descriptive phrase, like 'the only man who escaped from the sizaghter of Caragnaria mission', a name; while verbe and adjectives, which can be

A term then may most properly be defined as whatever can be thought as the subject or predicate of a proposition. But if we mean the name or verbal expression signifying what is thus thought, we may define it as a mord or combination of mords capable of standing as the subject or predicate of a proposition. In order to mark the former sense more unambiguously, logicians where the subject or predicate is not an individual a speak sometimes of concents instead of terms the word 'concept' signifying always an object of thought and never the name of it. What the logician calls a concept is often in common speech called a conception : my concention of heaven is what I think of when I speak of heaven. But it is desirable to be able to distinguish between the act of conceiving of heaven, and what I conceive it to be: in nonular speech 'conception' may signify either the act of conceiving or what is conceived, as 'narration' may signify either the act of negreting or the story parrated and composition, either the act of composing or what is composed : we may say that a man is engaged in composition or that he has sent his composition to the printer. The Greek language distinguished these two meanings by different verbal terminations, the act by nouns in -our (like allothous and ponous), the object or product by nouns in -ua (like αίσθημα and νόημα). It is this distinction which Logic marks, by using the word concept for the object or product of the act of conception.8

(It has been said that a concept is an object of thought. But it may be urged that the objects of our thought are things themselves; are things then the same as concepts? When we make a judgement, it is possible to distinguish between (i) the object, reality, or matter of fact which we recognize, and (ii) our thought in recognizing it. If I say Gibraltar belongs to the British

predicates in a proposition, can hardly be called names at all. Nor would any one speak of the 'middle name 'in a syllogism, though it is words which are ambignous when we have an 'ambignous middle'. Hence it seems desirable to retain the word 'term' in both the senses mentioned in the next

destrains to cream use word.

**Rothing in a term except when it is no thought; but when we consider terms in isolation, the question is not whether anything is a term in a given judgement—for there is no judgement piers—but whether it is a term of a possible judgement. Hence in our definition we must say 'whatever can be thought, for, and 'copoble of standing'.

² Technically, in the case of concrete general or of abstract terms. Cf.

infra.
On the nature of concepts of, pp. 55-57 infra.

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[Crown'. I refer to a rock at the entrance of the Mediterranean. and a fact in its present history. These form the first intention' of my mind. But my recognition of this fact about Gibraltar is itself a fact, and the thought in which I recognize it may be considered, and will form the 'second intention' of the mind. If. I consider this recognition, i.e. my indocument, I find it involves a recognition of the union with Gibraltar of this relation to the British Crown. These therefore are the terms of my judgement. and its terms are objects or realities recognized; for 'belonging to the British Crown' is as real as the rock, though not visible or tanoible. But I might have thought Gibraltar to belong to the Spanish Crown; and that relation, though real-it is real for example of Algerias-is not real of Gibraltar. Again, I might have spoken about Atlantis, instead of Gibraltar; and Atlantis never existed except as an object of Plato's or other men's imagination. Inasmuch then as we may think about that which does not exist or think falsely about that which does exist, it is necessary to distinguish objects of our thought from objects existing. Terms therefore are always objects of our thought: but they are not always objects that exist 1: though in any true judgement they are both. Hence it is possible to say that a term is some reality. or element in the reality, thought of, and it is possible to say that it is merely something thought of ; the objects of our thought need not exist, and even if they do, we need not consider whether they do or not. When concepts, or-more generally-terms as the elements into which a judgement is broken up, are taken in isolation, we do not ask whether, in thinking of them, we are thinking of an existing object; it is enough that they should be objects of thought; for this purpose, they must not contain elements which cannot be thought of as combined (as in the term 'square circle'); but they may be incapable of being thought of as combining with what really exists, and yet be objects of thought just because we are ignoring the question of their combination therewith. A concept then is an object of our thoughtor our thought of an object, if that means what we think it to be. and not the fact of our thinking about it-as opposed to an object as existing irrespectively of our thinking about it : though of an individual, so far as its being goes beyond what thought can grasp, there is no concept.2 Whether any objects exist altogether irrespectively of the knowledge of them is a profound meta-

1 Or have existed or will exist.

[•] Ur have ensted or will exist. It would be possible in ordinary speech to talk of a man's 'conception' of Gibraltar, or his 'idea' of it, in distinction from the rock itself; but concept in Logic signifies properly something universal. The question however is this paragraph is a general one concerning the relation of what are sometimes called 'ideas in the mind', to things, whether or not these! are 'ideas of individuals'.

Inhyrical question; holding that they do not, we must still admit that they arist irrespectively of this or that man's knowledge of them. And existence is not necessarily material existence; the objects of mathematical knowledge exist, though they are not material, like Gibralza, and no one could mount a battery on; them. But there are objects thought of which certainly do not exist except as objects of thought to the individuals who think of them; these have their being only in and for thought, and are concepts which have to be distinguished from 'things themrelves'.1

Having considered what a term is in general, and distinguished a term as an object of thought from a term as the word or words signifying it, we must now consider the main kinds of terms that Logic has to recognize. The ordinary classifications of terms are classifications of them as words which signify objects of thought; but the distinctions are based on differences in what we think of and in our way of thinking about things.

Terms as objects of thought are divided first of all into abstract and concrete: terms verbal into abstract, concrete, and attributive. A concrete term (verbal) is the name of a person or thing, an abstract term the name of a quality or attribute; so that the distinction between the thing and its qualities, between substance and attribute, is the basis of the distinction between concrete and abstract terms. Attributive terms will be explained later.

Our notion of a thing involves two elements, which furnish the basis for a further division of concrete terms into those which are singular and those which are sommon or general. A thing is, first, an individual, having an existence distinct from that of other individuals; the page, for example, on which these lines are printed is a different page from every other in this book. But secondly, a thing has a character, which may be the same in other things; just as other pages in this book, though individually different, are equally pages. This character, which belongs alike to many individuals, is called sometimes an winereal; and they, as so many different cases or examples of it, are called particulars: particulars, as we often say also, of a kind.

Now the various particulars of a kind, so far as they have the same character, may be called by the same name: so far as

i.e. terms as - the word or words signifying an object of thought.

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they are distinct particulars, they will require different names to distinguish them. Their names as things of a kind are common or general names: for the name is common to all particulars of the kind or applies generally to any scorp sonirrel, file, metal, are general names. Their names as individuals, if they have any, are singular. like London Zoroester, the Matterhorn: such names as these we call proper names. A coneral term is thus one that is predicable of any number of individuals in the same sense: a singular term one that is predicable of one individual only in the same sense. Smith for example, as meaning one who works in metal, is a seneral term, because I mean the same by calling Dick or Thomas a smith : if I use it as a proper name, numerous as are the persons who hear it. I do not mean the same in each use of it. I may refer to the defender of Acre, or to the witty canon of St. Paul's. or to any of a hundred and one others, and in each case my meaning is different.

We are seldom at a loss for some general term by which a particular thing may be denoted: but comparatively few particulars have singular terms appropriated to them. Many particulars of a kind-for example, new pennies-are not distinguishable at all to our senses, except by each occupying (when we see them together) a different place : these will not have each a different name, for we should never succeed in calling each individual always by its own proper name. In other cases, though the particulars of a kind might be tolerably distinguishable—for example, lumps of chalk of varying shapes and sizes—we have no occasion to refer to them individually, nor to burden our memory with so many names. Weare content to employ a common or general name, and to specify the particular object (from among all those that bear the name) to which we wish to refer, by pointing, or the use of a demonstrative or possessive propoun, or some periphrasis. Thus we say the picture there', and point: or 'this year', or 'my great-coat', or 'the bust of Julius Caesar in the British Museum of which Froude used an engraving for the frontispiece of his life of Caesar'. Such expressions are indeed in a manner singular terms, for they serve to designate particular objects; they are not however proper names, and they have been conveniently christened designations.

But where particulars of a kind are distinguishable, and we are interested in them singly and wish to be able to refer individu-

discopie

ally to them, we give them 'proper names'. Thus every individual man has a name of his own, and every field in the country in named, because the farmer needs to tell his men which particular field to work in; and a railway company names or numbers its various engines and carriages. Though however many particular things have no proper names, all which have proper names have general names also; the 'four-acre' is a field, the 'Cornishman' is a train, William the Silent is a man; and on the other hand any particular thing might, if it were worth while, be distinguished by a proper name. The proper name and the common name thus recognize respectively the two elements in our notion of a thing noted above: the proper name recognize its distinct existence the common name its character that it shares with other things: nor could our thought about things express itself fully without concrete terms of these two kinds.

[This has not indeed been always admitted. Thus James Mill in his Analysis of the Haman Mind (vol. i. ch. viii. p. 260, London, 1869) writes that it is obvious and certain that men were led to class solely for the purpose of economizing in the use of names. Could the purposes of naming and discourse have been as conveniently managed by a name for every individual, the names of classes and the idea of classification, would never have existed. But as the limits of the human memory did not enable men to retain beyond a very limited number of names; and even if it had. as it would have required a most inconvenient portion of time, to run over in discourse as many names of individuals, and of individual qualities as there is occasion to refer to in discourse it. was necessary to have contrivances of abridgement; that is, to employ names which marked equally a number of individuals, with all their separate properties; and enabled us to speak of multitudes at once. The position here taken up by Mill is known technically as that of nominalism, the doctrine that things called by the same name have only the name in common; a doctrine frequently professed, but not often stated with such uncompromising clearness as in this passage. We do not however really call different individuals by the same name, except because they have or are believed to have the same nature; nor is it conceivable that we could name an individual by a proper name, without at the same time recognizing in it, however vaguely, some character that, as capable of existing equally in other individuals, might be marked by a general name. General names therefore are not a mere means of abbreviating discourse, but their existence arises from a necessary feature in our thought about objects. Aristotle's distinction at the Descinning of his Categories' between duspying, or things called by the same name having only the name in common, and συνώνυμα, er things called by the same name having also what is meant by the name in common may be mentioned here: the distinction is nowndays embodied from the side of names instead of things in that between equivocal and univocal terms (v. infra, p. 84).]

There are thus two kinds of concrete terms, viz singular terms. or names of individuals, and common or general terms; singular terms can be further distinguished into proper sames, i.e. names permanently assigned to one individual, and designations i.e. phrases which by a pronoun or what not serve to indicate an individual otherwise than by a name of its own. Now it has not been stated in the last sentence, what general terms are the names of (Are they also the names of individuals, or are they names of the character common to many individuals? The former view seems incomplete, for it does not take account of their difference from singular terms. The latter view seems inconsistent with calling them concrete: for the common character of many individuals. regarded by itself, seems like a quality-something considered in abstraction from the things possessing it.

The importance and difficulty of this problem can only be appreciated in a more advanced study of thought than this volume contains. Here the following solution must suffice : but we shall come upon the same issue again in other connexions.

A general term, being predicable of any number of individuals in the same sense, implies that though they are individually different they have something in common; in other words, that there is something the same in different individuals. This common character is only found realized along with the special differences that distinguish one individual from another; the common character of man is found in you and me concrete with all that distinguishes one of us from the other: and was is a concrete term. When on the ground of that common character we are called by the same name. the name is concrete: but when the common character is considered by itself, and a name is given to that, without regard to or is abstraction from the individuals who manifest it, that name is abstract. Thus immonity 1 is an abstract term, though it is what

¹ The term humonity has of course other meanings, viz. mankind collectively, and also kindliness; in the text it means the human nature common to all men.

makes each of us a man. The term gold, again, is concrete; we may say 'this gold' and 'that gold', and 'the gold in the cellars of the Bank of England'; but if we regard the common character of all these, in abstraction from any particular parcel of gold, we should call it 'goldness', which would be an abstract term. The readiest test whether a term is concrete is furnished by asking—

'Do I mean by it some person or thing (or some assemblage of persons or things), or only a quality or attribute of such?'

Thus assimal is a concrete term, but colour is not; society, when we talk about 'a society', is concrete; when we say men live together 'in society', it is abstract, for then we mean by the word not men living together in a certain way, but only the way in which they live together.

It was stated above (p. 18) that the distinction between concrete and abstract terms rested on the distinction between substance and attribute; and in the last paragraph it might have been said with more precision that the test whether a term is concrete was furnished by asking whether it could be used of a substance or assemblace of substances. And the difficulties often felt in determining whether a term is concrete or abstract spring from the difficulties lurking in the distinction of substance and attribute. If by substance we mean the fully determinate individual, then what we call the attributes of a substance are elements in its being, and it is not something to which they can be attributed as addenda, like an article of clothing: the individual is not substance + attributes, the attributes are rather factors in the substance. Any of these attributes, however, can be considered separately or in abstraction from the rest of the nature of the concrete substance, and so considered can be as it were replaced in thought in the concrete whole from which it has been abstracted, or be attributed to it. But while sometimes what we thus consider separately is only some comparatively simple feature of a thing, as its colour, or size, or price, at other times we consider in one notion or concept indefinitely numerous features, on the strength of which the thing is grouped with others in a 'natural kind' (cf. pp. 41-43 in/.). If we gave a name to these features considered in abstraction from what else characterizes the substance, such name would be abstract; but just because they constitute so much of its being, we give a name only to it as constituted by them, and such a name, like mas or gold, is concrete; they are not abstracted from and attributed to the remainder; and therefore we have no name for them considered separately, unless special reasons prompt us, as in the case of 'humanity'; but as a rule, where occasion demands abstraction, we use a periphrasis [like ' the nature of gold ', and have not abstract terms like goldness. It is perfectly justifiable to say one abstract term is less abstract -more concrete—than another, in the sense that though we are considering not any substance, but some part of the full and determinate nature of a substance, yet the part we are considering is more, and more determinate in one case than in another. Thus the properties of figure and number, which can pre-eminently be studied in isolation from all else about things, are pre-eminently abstract.

Language, unfortunately, is ant to mislead us in this matter. Many abstract terms are not commonly used in the plural: and when we find a term used in the plural, we are apt to think it concrete, as predicated of divers individuals. But this is not necessarily the case. Triguels is not really a concrete term because we can talk of triangles; 'triangles' is indeed concrete if it refers to things of wood or steel, and so is the singular in like case: but 'triangle' often means the triangularity of every individual triangle, and 'triangles' different modes of such triangularity. And colour is not concrete because we can speak of colours. 'Colours' is concrete if I mean certain slabs of pigment; but if I mean blue, green, and yellow, as qualities, it is abstract.

The distinction of concrete and abstract terms is therefore only

really intelligible if we ask ourselves what we are thinking of. If we took alone to terms verbal, it is impossible to tell whether a name is abstract or concrete; for many names are equivocal. being sometimes one and sometimes the other.]

Abstract terms then are the names of qualities or attributes: but we must understand this definition rather widely. It is not only single sensible qualities, like flavours or odours, whose names are abstract terms; all that goes to make the nature of an object, when it is considered merely as qualifying such object, is abstract, and its name (where it has any) an abstract term. Moreover, the object in question need not be a single thing (or person) such as a stone or an elephant: it may be an assemblage of what we regard as distinct things (or persons), like a forest, or an army; but if there are features belonging to this assemblage, though they are not qualities of any one object in it (as a forest may be extensive and an army skilfully or unskilfully disposed), these features considered in themselves are abstract, and their names, 'extent' or 'disposition', abstract also. Hence animality, discipline, civilization, paternity, are all abstract terms, though it is only by adoubtful extension of language that we could call any of them a quality, like fragrance or sweetness.

[The distinction of singular and general is not applicable to abstract terms. The calling a concrete term general rests upon a consideration of the many different individuals who being of the same kind claim the same name. But an abstract term is the name of that which is common to many individuals, considered without reference to its repetition in them all. It may be thought that abstract terms ought therefore to be called singular; but neither would that be correct. A singular term denotes an individual: but an abstract term denotes something common to many individuals. something therefore which is 'universal'

It is indeed true that whereas general terms are applied to many distinguishable individuals, certain abstract terms are predicated of many distinguishable attributes. Colour is used equally of blue and red and all the other colours of the spectrum : disease, of measles, whooping-cough, bronchitis, and many other ills that flesh is heir to: whereas we do not distinguish different examples of blue by different names 1, nor different cases of bronchitis. But 'blue' and 'bronchitis' are not for this reason singular terms; the true analogy of the relation of the terms 'blue' and 'colour' is the relation of the terms 'man' and 'animal', and not that of 'Socratee' and 'man'. Just as no one would say that 'man' is a singular term because it is one species of animal, so we ought not to say that 'blue' is a singular term because it is one species of colour, nor 'bronchitis' because it is one species of disease; for that would be to confuse the distinction of species and genus with the distinction of individual 2 and universal. 'Socrates' is a singular term because it is the name of an individual having attributes: 'blue' is not a singular term because it is not the name of an individual at all, but of an attribute that may belong to many individuals.

Besides abstract and concrete terms, a kind of terms has been recognized which cannot well be classed with either-viz, adjectives and adjectival terms. These are called attributive terms. e.g. red, beaten, insolvent. They are not the names of qualities, like redness, defeat, insolvency; on the other hand, it is those qualities which furnish their meaning, and not the nature of the various kinds of object to which the qualities may belong. Thus cloth may be red and so may silk, but we should not explain what is meant by calling them red if we were to explain the nature either of silk or cloth; and a man may be insolvent and

1 We may of course distinguish varieties of any one colour by special We may of course distinguish varieties of any one colour by special names, like sky-blue and peacock-blue. But this does not affect the argument in the text: it would only require us to treat, not blue, but sky-blue or peacock-blue as the abstract term that is applicable only to one attribute.

The individuals of one kind are sometimes also called porticulars (of. p. 18), in contrast with the universal or kind that characterises them all

so may a company, but to explain what is meant by calling them insolvent we must explain the nature not of man, nor of a company, but of insolvency.

J. S. Mill held that adjectives are really concrete, on the ground that white is predicated or is the name of snow milk or linen and not of their colour: it is an army and not a defeat that is heaten 2 But it is clear that the subjects of which an adjective may be predicated can as well be abstract as concrete; and if the adjective is concrete because it is predicated of a thing it should equally he shatract because it is predicated of an attribute an that if we say that cabbages are common sommon will be concrete while if we say that indolence is common it will be abstract. The fact is that the distinction of attributive terms from abstract and concrete corresponds to no further distinction in thought: if terms are objects thought of attributives are not terms at all : we may attribute a quality to a subject but that is an act of indeement: thing and quality, substance and attribute differ as objects thought of: thing or substance is concrete, quality or attribute abstract. and everything abstract is attributable; but there is no third kind of object thought of to correspond to the attributive term. In language however there are words which, though they can be used as predicates, and therefore satisfy the definition of a term verbal, are not properly names either of a substance or of an attribute. Adjectives are such words: but so also are verbs. Verbs however were overlooked by those who erected for adjectives a third class, along with abstract and concrete, in the division of terms verbal. For terms are the parts into which a judgement is resolved: in them, taken singly, the act of predication is not seen: they are as it were dead members, which could only have been taken apart because the life of judgement had fled and no longer bound them together. But in the meaning of the verb this life lingers, even if a verb be taken without its subject. Hence

¹ The meaning of attributives may, however, he incapable of explanation without reference to that in the nature of the subjects whereto the qualities belong which makes them succeptible of these qualities. Thus notiber substance in the control of the control of

logicians, anxious to effect the resolution of a independent into its terms, have often preferred to sunder, even in language, the word which expresses the predicate from that which expresses its prediaction to take the term as it were out of the work and say of Lear not, with the doctor !, that he 'sleens still', but that he 'is still eleeping'. Now in such a case the predicate is often adjectival in form : although not always, for the proposition 'He plays cricket' would become, if it were meant that he played habitually, not 'He is playing cricket' but 'He is a cricketer'. Such an adjectival predicate is one of the parts into which the proposition is resolved whereas the verb belongs rather to the unresolved proposition. The whole question of the separate character of the adjective, or adjectival word, belongs indeed rather to grammar than to logic. But when 'term' means name, or term verbal, as names are either substantival or adjectival, and concrete and abstract names are both substantival, some place is wanted for names adjectival, and so they are classed separately as attributive terms. If their form were to be ignored and they were to be referred either to concrete or to shetreet they should rather be considered shetract than (se J. S. Mill would have it) concrete: for their invention implies the consideration of some quality or character in the thing in abstraction from the rest of the thing's nature.

A special class of terms is constituted by those which are called collective. Like the other distinctions of terms recognized in Logic, this is based on a distinction in things. Individual things or persons may be considered singly: they may also, since there are many of them, be considered in groups; and the names of such groups are collective terms. Thus a group or collection of books forms a library; a group of human beings related in creatin ways forms a family; related in rather different ways, a tribe; in other ways yet, an army or a club. Any term that denotes a collection of objects, with certain resemblances or relations among them, is collective. Collective terms may be either singular or general; for we may wish to refer to a group composed of certain specific individuals

¹ King Lear, Act iv. 7 1. 18.

Adjective can indeed be used as subjects, e.g. Besti immaculati in via, where it is possible to take either term as predicate. In many languages the article is generally necessary in order to make an adjective do duty as a substantive.

(as when we say 'the family of King Henry VIII') or simply to a group of individuals, no matter who or what, that is composed in a certain way, such as a family or a regiment : but all collective \ terms are concrete for they are the names of the individuals taken together and not of the mode of organization among them. A general collective term is said to be used distributively of the different crouns that it can severally denote and collectinely of the individuals in any one group: thus if we speak of British regiments the term is used distributively of the Guarda the 60th Rifles the Sutherland Highlanders &c. and collectively of the men in each several regiment.

We may sum up what has been so far said of the kinds of terms as follows .- Terms as objects of thought are either concrete or abstract - as names or terms verbal, concrete abstract or attributive : concrete terms are either singular, and then either proper names or designations, or else general : abstract terms, having no reference to individuals, are not conveniently considered as either singular or general, but always signify something universal; and some of them are not names of one recognized attribute (or state or quality or relation) only, but include under themselves divers species thereof. It may be added that attributive terms are obviously general.

We pass now to a fresh division of terms, made from another point of view. As we may give a name to a group of objects taken together, which would apply to none of them by itself, so we may give to an object or quality, when we regard it in its relation to some other object or quality, a name which would not apply to it considered in itself. Such terms, attributing to one object or quality some definite relation to another, are called relative terms; and in contrast with them, terms that indicate an object or quality considered in itself are called absolute. It is clear that if one object or quality stands in relation to another, the latter must also stand in relation to the first; and the name applied to it to indicate this reverse relation is 'correlative'; or, since each is correlative to the other, the two together are called correlatives. Instances of relative terms are coval oreater subject, parent: with their correlatives equal, less, ruler, child; apple, sound, man are absolute terms. Relative terms are necessarily general 1, like attributive terms:

¹ Except so far as they are combined into a term whose whole meaning is singular : e. g. first is general, but the first Pharack is singular.

for the same relation may be exemplified in many particular instances, and therefore many objects may stand in that relation which the relative term is used of them to indicate. They have this further recomblence to attributive terms that though meaning a relation they are applied to a subject standing in that relation : as attributive terms are to a subject possessing the attribute which constitutes their meaning: they are not however themselves necessarily attributive—thus 'contemporary' is relative and attributive. but 'a contemporary' is relative and concrete. The existence of attributive terms is grounded in the fact that the various objects of our thought do possess distinguishable attributes : and that of relative terms in the fact that they do stand in distinguishable relations one to another. It has been contended that all terms are really relative because every shiest of thought stands in relation to other objects and nothing can be absolute except the totality of existence, beyond which there is nothing for it to stand in relation to. But though it is true that everything stands in relation to other things, things are sometimes considered rather in themselves. and receive names accordingly: and sometimes they are considered in definite relations to another thing, and receive names that indicate that particular relation. And this is sufficient ground for the distinction between absolute and relative terms, though there are cases in which it is hard to say whether a given term is one or the other. Man is clearly absolute, and father relative, though mountain might be disputed: for a mountain is so only by its elevation above the plain, and yet in calling it a mountain we have in mind many features besides this relation.

Terms have been further divided into positive, negative, and privative. A positive term is said to imply the presence of a quality of, e.g. preed, preedy; a negative term to imply the absence of a quality, e.g. colourless, unfit, unfitnees: a privative term to imply the absence of a quality where it has been or might be expected to be present. e.g. deaf. deafnees, desirected.

There is a certain difficulty in the notion of a negative term, and in the account of it just given; for no term can be purely negative, and imply merely the absence of a quality. The Irishman's receipt for making a gun, to take a hole and pour iron round it, is not more difficult to execute, than it would be to frame a term whose meaning consisted simply in the fact that a particular quality was not

meant. A term must have some positive meaning or content, in order to be a term at all.

It is indeed sometimes said that a negative term includes in its meaning whatever is not meant by the corresponding positive term According to this view there is no positive term to which we may not frame a corresponding peoplice: to man there corresponds notman, to book not-book to severe not sowere to colour not-colour: notman is everything which is not man, and includes therefore not only the other animal enecies, but plants and minerals, books and institutions, birth and immortality; sot-book includes all these but books and man besides; and so forth. The two 'contradictory' terms (as they are called) comprise between them all that is: nothing can be conceived, of which one or the other is not predicable; and they divide the universe between them. What the positive term is does not matter: for whatever it be, the negative term covers everything else and therefore it may be expressed by a symbol : let A represent any term, and not-A its contradictory: and we may then say that A and not A between them make up all that is or that there is nothing of which one or other may not be predicated. 'Everything is either A or not-A.'1

Such negative terms as these do not really floure in our thought : they are 'mere figments of logic's: Aristotle long ago pointed out that our-deflowres was not properly a name at all; and he

¹ This formula, 'Everything is either A or not-A,' is sometimes given as the 'Low of Excluded Middle'. The 'Low of Excluded Middle' means that of the contradictory propositions one or other must be true; they cannot both be false, and therefore any third or middle course between accepting both be false, and therefore any third or middle course between accepting ones and accepting the other is excluded. 4th has been asked whether either of such contradictory propositions as Virise is triangular and Virise is of such contradictory propositions as Virise in triangular and Virise is of triangular node to except the former is clearly false, but the latter does not seen true. The asswer: is that if any one went to assert that virites and according to the contradict him; but that no one who realizes virites to be incapable of any apatial character at all would were realizes virites to be incapable of any apatial character at all would every to binned the alternatives; is virites triangular or is it not! and that to one who, not realizing this, asserted it to be triangular, the proper contradiction is that it has no fligure. The case therefore trainible on acception to the truth of the Law of Excluded Middle, provided the alternatives are not as the other trainible as however the contradiction is the contradiction to the truth of the Law of Excluded Middle, provided the alternatives are such as the contradiction is the contradiction to the truth of the Law of Excluded Middle, provided the alternatives are such as the contradiction is the contradiction to the truth of the Law of Excluded Middle, provided the alternatives are such as the contradiction to the truth of the Law of Excluded Middle, provided the alternatives are such as the contradiction of the contradiction to the contradiction not at the outset realised as nonsense; but no one to whom they are nonsense would expect to set by them the visitility of the law of thought; for talking nonsense is not thinking. The objection to stating the Law of Excluded Middle in the form 'Everything is either A or not-A' is this, that it seems to sanction the formation of nonsennical contradictors, such as we have examined, no less than of contradictories that are rational. Of size Bradley, Logic, I. v. §§ 23, 24. 2 Stock, Deductive Logic, § 138.

perhaps extended his countenance too much to it, when he said that, if we were to call it anything, we must call it a 'name indeterminate' (δυρω άδρωτου) because, being the name of nothing positive and in particular, it had a purely indeterminate signification; it was annihable consult to thing existent and non-existent.

The invention of such terms however is explained when we remember the relation of a term to indeement. The latter, as we have seen, is the primitive and remains the complete act of thought, and terms are not by abstraction from it. Now the affirmative judgement 'All flesh is grass' may be resolved into the terms flesh (the subject) and grass (the predicate affirmed of it); but the perative indeement 'Man is not a fly's into the terms man (the subject) and fly (the predicate denied of it). But since we do therein affirm that man is not a fiv. it seems possible to say that the predicate. not a fly, is affirmed of man, as well as that the predicate fly is denied of him. This attempt to reduce negative and affirmative judgements to a common affirmative type, by throwing the negative into the predicate, is not really defensible, for the very reason that the negative term not a fly has no meaning; and hence, as we should not take the trouble to affirm of man nothing in particular, the only point of the judgement must lie in denving of / him something in particular; so that the meaning of the 'infinite' indocement (as it is called) 'Man is not a fly lies in the negative judgement 'Man is not a fly', and it is clear that we have not resolved the negative into the affirmative form, when such affirmative can only be understood by restoration to the negative. But it is out of such attempts that purely perative terms like 'not-fly' have arisen; and it is only by understanding that the term A has been the predicate of a negative judgement, that we can understand how the term not-A should ever have been formed.

There are however certain negative terms which are not such mere figments of logic as the 'infinite terms' which have been just considered. Where the positive is not a general concrete term but

¹ de Interpr. ii. 18º 80-83: the technical term in Latin is nomen infinitum, where the English phrase 'infinite form' is derived: but infinite means in this context indeterminate; and for the sake of perspiculty, the latter word has been used in the text.
8
Why hath not man a microscopic eye?

For this plain reason, man is not a fly.
——Popu, Essay on Man, I. 198.

is attributive, there the corresponding negative may be quite legitimate: indeed the distinctions of positive, pegative, and privative most premerly apply not to all but only to attributive terms. or to abstract terms founded mon these. For all attributive terms fromly by their very form a subject of which they may be predicated, and to which they refer that attribute which constitutes their meaning. Therefore even if the term be negative, it still supports a subject which, in the absence of the attribute which the negative term excludes, is positively conceived as having some other character instead. And here we have a basis of positive meaning to the negative term: for let A be a positive term: then . not-A will signify what a subject, which might be A, will be if it is not A. Thus intemperate signifies what a man, who might be temperate, will be if he is not that : sucress suggests what a line or surface, such as the surface of a road, will be if it is not even: not-blue suggests what a thing which might be blue (that is, an object which must have some colour) will be if it has not that colour. The definiteness of the positive meaning which a negative term thus conveys will vary greatly, according to the range of alternative attributes which we conceive possible to a subject that might conceivably have possessed the attribute denied of it; thus intemperate has a more definite meaning than not-blue, because when temperance is excluded, though there are many degrees of intemperance, yet they have more affinity with one another as contrasted with temperance than the different colours which remain when we exclude blue: were fied has a more definite meaning still. for a surface which is not in any way ruffled can only be smooth. It has been alleged that 'not-blue' does not necessarily imply

coloured in some other way than blue', nor 'not-even' a surface of another kind than even: that it is as true to say of banter that it is not blue as of a butteroup, and that larceny is as much not-even as Lombard Street. But such a contention misinterprets our thought. Just as privative terms imply the absence of an attribute from a subject that possessed or should have possessed it and therefore must convey a notion of what the subject consequently is without that attribute, so negative terms (at any rate when they are not

 Cf. next page.
 The old Greek proverb will illustrate the point here—docked μέν γάρ dullie, warrodunie di sasul.



mere figments of logio) imply the absence of an attribute from a subject that might conceivably have possessed it, and therefore convey a notion of what the subject is instead. The attribute which a negative term excludes belongs to a genus of attributes (as blue belongs to the genus colour, or prudence to the genus festure of human character, or square to the genus figure); and if a subject is unausceptible of any attribute within that genus, we should not be at pains to deny of it some particular attribute in the genus; since the soul for example has no figure, we should not say that it is not-square; since furniture has no feature of human character, we should not call a towel-horse imprudent. The negative term is only used of what must have some stribute within its genus; and this genus furnishes a substratum of positive meaning to the negative term; so-t-like does mean 'coloured not with blue' and set-ores having a surface which is usered.

The statement that the distinction of terms into positive, negative, and privative is only applicable properly to attributive or relative terms may seem 50 be contradicted by the fact that many negative terms, such as injustice, inequality, non-intervention, are not relative or attributive. But it will be found that all such terms are abstracts that presuppose the relative or attributive negative term; and are very positive in their meaning. Injustice does not mean whatever is not justice (such as 'accidence and adjectives and names of Jewish kings'), but the quality of being unjust; inocality means the relation of being unequal; non-intervention the conduct of the not-intervening. Abstract negative terms like not-equality or not-loolour are as unwest as concrete negative terms like not-Scorates or not-book.

It may be asked, if all negative terms (and the same is true of

¹ The genus within which any attribute falls, or the subjects susceptible
of some attribute within that genus, may be called with de Morgan [Formal
Logic, p. 41) s 'limited universe'; thus show is a predicate in the universe
Logic, p. 41) s 'limited universe'; thus show is a predicate in the universe
Logic, p. 41) s 'limited universe'; thus show is a predicate in the universe
Logic, p. 41) s 'limited universe'; thus the universe between
universe, but the limited universe or whole of things which constitutes the
genus to which they belong; the members of this limited universe have
a positive common character, which gives the negative term a positive
common character, which gives the negative term a positive
character common to all things included in it, except the character of being
which, as Aristed pointed out, considered in it isself and not as realized in
some special mode of being, is not a significant term. Cf. de Interp. iii. 16°2.
Such a 'limited universe' is sometimes called an 'universe of discourse'.

11] TERMS, AND THEIR PRINCIPAL DISTINCTIONS 88

privative) have a positive meaning, what is the use of the distinction between them? The answer is as follows. First with record to the distinction of positive and privative terms: there are some states which can only be understood as the principle of a positive state: deafness would have no meaning, but for our knowing what it is to hear: we cannot think of a hody as design cated, except we think of it as having first contained moisture.1

Secondly, with regard to the distinction between positive and negative terms: there is a real difference between a term which signifies one definite attribute, and a term which signifies any attribute within a genus except one: the latter is comparetively indeterminate and uninstructive: e. c. pertobrate signifies a definite anatomical structure: imperfebrate signifies a structure which is not vertebrate, but fails to characterize it further. Positive terms are positive directly and precisely, negative terms indirectly and for the most part vacuely. This distinction is imnortant, and we are therefore justified in calling attention to it: it will be seen for example presently to be one of the rules of definition to avoid, as far as possible, negative terms; and there is no way in which the point of this instruction could be so well conveyed as by the help of the distinction of negative and nositive tarma

The doctrine about negative terms impropried in the foregoing paragraphs furnishes a good example of the dangers that beset a purely formal logic. If we regard only the form of a proposition, A is not B, (in which the terms are A and B) we may 'permute' it to the form A is not-B (in which the terms are A and not-B); and we may formally regard A, B and not-B all equally as terms. But whether the proposition A is not B, and the 'perative term'

¹ These two examples are not quite parallel. The notion of deafness can be formed by any one who knows what hearing is. The notion of desic-cated 'cannot be formed by any one who knows what moisture is, but he must also know what dryness is. 'Desiccated' is a privative term, because it means a dryness due to the withdrawal of moisture previously present : but means a dyness due to the withdrawal of moisture previously present; but 'dry' is just a positive a term as 'moist'. It sometimes happens, with two motically exclusive alternatives like dry and moist, that mon dispute whether or not both any positive. Some place place that the moisture of the present of the present of good; cohen, that pain and o'll are just as positive as good and pleasure. In these cases, it will be also in disputs, whether or not pain and o'll are privative terms. But the dispute arises from our uncertainty how to think about the things; and so furnishes another illustration of what has been pointed out in the text, that logical distinctions of terms reflect and are based upon distinctions in the way we think about things.

[not-B, have any meaning or none will depend upon the matter of the proposition—upon what kind of a term B was. Looking at the form, B has a corresponding negative not-B; but whether such a form of thought, or notion, as not-B is possible cannot be told by considering the form alone.]

We have still to notice the distinction of reinscal equipocal and analogous terms. Univocal terms are terms with only one meaning. so that they are used in the same sense of every subject of which they are used at all acquivocal (or ambiguous) terms are terms with more than one meaning so that they may be used of different subjects in different senses e or fair as used of a complexion and of a harosin analogous terms are terms which have more than one meaning but the meanings have a certain degree of identity or correspondence—e.c. we speak of the foot of a man and the foot of a mountain, meaning different things, but in both cases that on which the object stands. We ought in strictness to regard this distinction as one not in terms but in the use of terms; for fair is used univocally of all fair complexions, and is only equivocal when we use it at once in different senses. All proper names helonging to more than one individual are used equivocally of such different individuals

[The history of the words univocal, equivocal, and analogous will illustrate the tendency to treat Logic from the standpoint of an affair of names. The Aristotelian distinction already alluded to (p. 20) between συνώρυμα and δμώνυμα was one of things. Unicocum and equicocum are merely translations of συνώνομου and φμώνυμου, and they were defined in the same way (cf. Crackenthorpe's Logic, Bk. II. c. i. 'Aequivoca ita describuntur: aequivoca sunt quorum nomen solum est commune, ratio vero illius nominis est alia atque alia, c. ii. 'Univoca describuntur in hunc modum : univoca sunt res vel entia quorum nomen est commune. et ratio illius nominis est una et eadem in omnibus quibus nomen convenit'). Similarly, it would have been not the word 'foot', but the man's and the mountain's foot that would have been called analogous. If we remember that terms are not primarily names, but the objects of thought intended by the names, we might still say that equivocal terms are different objects of thought with the same name, rather than the same name with different meanings. But in English usage the distinction of names has really displaced that of things; we do not even retain both like the Latin, when it was said that 'aequivoca' were either 'aequivocantia, ipsae voces aequivocae', or 'aequivocata, res ipase per illam vocem significatae'.]

CHAPTER III

OF THE CATEGORIES

Two distinctions between terms discussed in the last chapter are not primarily grammatical like the distinction between substantive and adjective (though here and there, as we saw, the forms of language have affected the mode in which they have been drawn) : nor do they belong to any special science, like the distinction in chemistry between names in -um, which signify metals and names in -oes, which signify pases. They belong to all sciences, and are based on certain features that reveal themselves to reflection about any subject whatever: and that is why they are logical. But these differences of form in our thought about things correspond to and involve differences in the manner of being of these things themselves. It is of special importance to remember this in considering the Aristotelian doctrine of Categories, out of which some of the preceding distinctions take their rise. The categories present a logical, but they present also a real distinction : i. a. a. distinction in the nature of the reality about which we think, as well as in our manner of thinking about it

The word category, xarnyopla, means predicate; and the categories may be described as a list of predicates, one or other of which defines the mode of being belonging to everything that exists. In the complete list there are ten, viz.

ούσία	substantia	substance
ποσόν	quantitas	quantity
ποιόν	qualitas	quality
πρός τι	relatio	relation
ποῦ	ubi	place
TOTÉ	quando	time
κεῖσθαι	situs	situation
Exect	kabitue	state
TOWN	actio	activity

πάσχειν passio passivity (being acted on)

Or predication: but the difference is here unimportant, and Aristotle cometimes uses carryopogal instead of corryopoga in the present sense: v. Bonitz.
Index Aristot, s. c. κατηγόρμο. The Latin equivalent is Procedicomentum.

These Aristotle calls both 'kinds of predicate', γένη τῶν κατηγοριῶν, and 'kinds of being', γένη τῶν ὅντων. We must examine the latter physics first if we wish to understand his doctrine

We have seen that propositions may be expressed ownerally in the form A is R. But the predicate does not seem sonally in all cases to declare what the subject is. A man is an animal, and a man is in the kitchen: Tray is a dog, and Tray is happy now: a musician is an artist, and a musician is breaking my hurdy. gurdy: if we look at these independents, we shall admit that the second does not tell us what a man is so much as the first : that the third is a fuller answer than the fourth to the question 'What is Tray?': and that the fifth is a fuller answer than the sixth to the question 'What is a musician?'. Now Aristotle would have said that the first, third, and fifth of them declared what their respective subjects were saff aird, or per se; the second, fourth, and sixth what they were gard guadefluxes, or per accidens. In other words, the predicate is in the one case of the essence of the subject, and the enhiert could not exist at all without it being predicable of him . in the other case it is an accident of the subject. What is predicated of a subject saff airro tells you what it is necessarily, and permanently 1; what is predicated of it sard συμβεβηκός tells you indeed something about it, but something less necessary, and nerhans unnecessary, to its being-something of which it could be divested, and still remain the thing it is,

The ultimate subject of predication is the concrete individual thing—you, Scorate, Bucephalm, or the stone in your signetring; and if you sak of this what it is, you will have to specify in your answer, some kind of sublestace; you are a man, Bucebulan is a horse, the stone in your signet-timp is an arate. All

¹ This is not a complete statement of the meanings in which, according to Aristotle, a predicate may be said to belong to a subject xof aird; but it is, I think, a sufficient account of the sense in which the expression is used in this connexion.

uses in this connection.

'This is the true meaning of the statement in Cat, iii. 19 10 free 'report and 'ripou carrypopras' is call 'decoupiero, for a ser's voi carrypopras' or New York and are's voi bourspapero beligherm—a statement sometimes correctionally quoted as equivalent to the Diction do Omai et Naido. Cf. infra. c. xir. p. 275 n. But there are concrete things denominated from predictors in some other category than that of rabstance; a.g. a threshold is a concrete thing, but in calling it a threshold to not give its rebetance: to do that, it should have to say that it was a stone. It is a threshold because it is a stone in a certain situation.

these—man, horse, agate—are so many different substances; in saying what you, Buoephales, or the stone in your signet-ring is seentially, or gor se, these are the answer I must give; their essential being, therefore, is to be some kind of substance. But II sak what is a substance, I cannot find any more general significant notion under which to bring that, as I bring Buoephales, in declaring what he is, under the notion horse, and horse, in declaring what he is, under the notion substance. Of substance I can say that it is a kind of being; for substances are one kind of things that are; but it is of no use to treat mere being as a genus, of which substances are species, for to being considered in itself, and not as a determinate way of being (a.g. being as the property of the substances are species, for to being considered in itself, and not as a determinate way of being (a.g. being a substance). I can attach no meaning.

On the other hand, there are a great many subjects, about which, if asked what essentially they are, I could not possibly say that they were substances. Large, loud, blue, heavier, here, yesterday, fever, horizontal, fighting, running, defeat, virtue—all these are something, or they could not enter into true predication: but what are they? Directly or indirectly they all presuppose substances; if there were no animals, there would be no fever: if no one fought, no one could be defeated. But they are something incident to substances, attributes and not things. To say that they are stributes, however, only declares their relation to something else, their dependence; it does not declare what they are in themselves. If we sak that, we shall find ourselves ultimately giving as an answer some one of the other categories.

Thus I may say that 'yesterday was web': but that does not tell any one the nature of yesterday in itself. But if I say 'yesterday is the day before that on which I am now speaking', I explain what yesterday in itself is. And if next I am asked 'What is that?'; I should reply that it is a certain date or time; and there I must stop. The kind of being then which belongs to yesterday is not being a substance, but being a time. Similarly blue is a colour, and colour is a quality; loud also is a quality; and virtue; so that their being is being qualities; that is what essentially they are. Large is a size, i. e. to be large is to be of a certain grantity; to be hewier is to be in a certain relation; here is a place; fever is a state of the body, horizontal a sissation; fighting and running are activities, defeat a being acted on.

There is nothing then, according to Aristotle, that exists or can he thought of which is not either a substance, or a quality, or a quantity, or in some other of the categories. One or other of them is predicable of everything and they cannot be further reduced or brought under any common head 1. A quality is not a quantity a time not a place, to do is not to be done to nor any of these a situation and so forth. It might be thought that state is hardly distinguishable from quality, nor situation from place. But the things are not really the same. A state is something which characterizes a whole through the condition of its parts. Thus we call a man short because he has shoes on his fact - or healthy because each part of his body is functioning rightly; but the healthiness of his body as a whole does not mean that each part of it is qualified alike nor his being shod that every part of him has shoes on. A quality, on the other hand, is comparatively simple, and if it characterizes a whole, does so through being present in the same way in its various parts: if a whole surface is blue, that is because the various parts of it exhibit the same colour, and if a trader's stock is sweet that is because the things it is composed of are severally awart. The concention of a state, therefore, is more complex than that of quality; and so it is with situation and place. 'Upside down', 'horizontal', 'sitting', 'standing', are in the category of situation-predicates which determine not where a thing is, but its 'lie' or position there. Without place there could be no situation : but you do not determine a thing's situation by assigning its place.

The categories, therefore, are a list of predicates, one or other of which must in the last resort be affirmed of any subject, if we

i as a matter of fact, however, the category of relation is not equally excluded by the others; and Kancorates is said to have reduced them all to Rubstance and Relation. In doing this he would not have effected a real simplification, any more than if they were all reduced to Hesing; for time, place, action, &c., all involve essentially different kinds of relation; and a conception as mere being. Arrivable probably necessed relational predicates into a separate class because they appear to tell us less than others what a subject in 'Slife for high's would be in the category of secder'; taller than his neighbour. The fact high would be in the category of secder'; taller than his neighbour in that of spde r_i ; it gives more information about what has neighbour. The latter predicts only changes in the man hisself, The former involves relation also; but the latter is more planify and prelly relational.

ask what in itself it is. They are your raw commonair, kinds of predicate, and equally when the duron-the kinds of being which we recognize, the kinds (if we may put it so) of what things are. In saving things here, however, we do not mean things as opposed to their attributes: we mean anything real, and attributes are as real as the substances to which they belong. Nevertheless, the distinction between substance and attribute is prominent in Aristotle's doctrine : for all the other categories are called by him incidental to substance. And terms in the other exterories while they may be subjects of predication (as when we say that blue is a colour, or that the wise are few), are not metaphysically subjects - are not independently existing, but exist in concrete individuals. There is no blue except the blue of the sea or the sky of a larkspur or a centian, &c. : no wise except wise men or women. In the category of substance come all concrete individual things, and these are substances in the strict and fullest sense. Of these in the but resort everything is predicated. But what is predicated of them is partly itself in the category of substance, and partly in the other categories. We have here that distinction between first and second substances which once occupied so much of the attention of philosophers and theologians.

First substances are individuals like Socrates or Cicero; second cubstances are predicates like man, horse, peopermint, paralley, which tell what kind of thing as individual is. The former are never properly predicates at all; Socrates or Cicero is a subject of predication, but not predicable of anything else; for what is predicable is universal, i. a. might be predicable of any number of subjects; but these are individuals, and singular. The latter are predicates of the former, and are universal; but they tell what an individual essentially is, and so are predicates in the category of substance.

Of Ar. Met. A. iii. and Apell, Beirdge nur Geschiebt der priechlichen Philosophie, III. Die Käntgerierdehre dar Arischen. In the expression yier rie varyopiars, 'kinds of predicate,' corpopia refers no doubt to the predicates of things, these predicates falling under the kinds enumerated, not to the heads or most general predicates under which these fall. Some interpreters have therefore held that the concrete individual is not in any category, since it is navar properly a predicate (cf. Cot. v. 3935 sirè unique pri spieries objects objects or largropis). But Met. I.e., seems to show, what the whole doctrins of that treatise implies, that the concrete individual is in the category of substance; it is creatingly one of the 'linds of being.' The account in the text accordingly follows the implications of the appression spieries for substances.

while all else that is said of an individual tells only some quality or state that characterizes him, his activity or situation, his relation to others, &c., and is therefore a predicate in one of the remaining extensive.

Undonhtedly it is here that the chief difficulty in Aristotle's conception lies. But the difficulties are not sought gratuitously: they arise naturally in our reflection upon the nature of things. We naturally incline to think, in considering an individual, that out of all that characterizes it some part is more essential than another, goes more to make it what it is. This we call its kind, and Aristotle called it also its substance; and language contains names that are evidence of this, kind-names like man, horse, gold. It is indeed very hard to say exactly what constitutes the kind: kind-names, as we shall see later, present special obstacles to definition - and a positive account of the substance of an individual seems beyond us. But negatively there is a great deal which we should say does not belong to the substance—the place where the individual is, what it momentarily does or suffers, all in fact that we can refer to other categories. All these we tend to think of as attributes which the individual has, but that it can exist irrespectively of them: whereas, irrespectively of its kind, it would no longer be at all. And yet the kind is universal: it is predicated of more things than one : Socrates, Plato, and millions more are men : the lumps of iron in the world are uncountable. Hence follow two lines of reflection.

First, because the kind, though universal, is at the same time more substantial than the other predicates of an individual are—more concrete, in fact, than they—the kind, or 'second substance', comes to be thought of as having some special claim to independent existence. Other modes of being, other predicates, depend on it; but it is thought of as depending on nothing else for its existence. True that we only find the kind realized in some connecte individual; nevertheless it is not a mere attribute of the concrete individual, as predicates in other categories are. And some have held that these 'second substances' are real, whether there be any concrete individual of their kind or not: while others have held that, though only realized in individuals, yet each is one and the same in all individuals of its kind—man in all men, iron in all ino—and so may be called one substance, in a different way from

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this or that man or lump of iron, but just as truly. Each of these doctrines was called by the schoolmen realism', as opposed to the sommisations which denied the real identity of anything in different individuals bearing the same kindname.

But secondly, because the kind is universal, it is predicated of the concrete individual as predicates in other categories are. And as the individual is something which sas them, so it is something to which its kind is attributed. It cannot be identified with its kind: for then there would be nothing to distinguish one individual from another. Man is predicated equally of Socrates and Plato, and if each as an individual substance were just man, Socrates would be the same as Plato. Therefore we must look elsewhere for what distinguishes them. If we find it in the other predicates of the concrete individual, and may that he is the kind plus all his particular attributes, we resolve the individual into an assemblage of universal predicates. If we do not do this, but suppose that his kind and all his particular attributes as well belong to the individual, we are yet quite unable to say what the individual is to which they all belong. For in saving what it is we should merely assign to it a fresh predicate; whereas we want to get not at its predicates but at that which 'has' them. This gives rise to a new way of considering the subject of predication. Originally it was the concrete individual. Socrates or Plato: but of what he is one part was distinguished as what he is essentially, and the rest reduced to be attributes or 'accidents' of him, not necessary to his being, and not to be included in an account of his essence. Now, what he is essentially is also reduced to the position of attribute and mere predicate, and the subject becomes a mere subject of which as such nothing more can be said except that it exists and is unique in each individual. This mere subject of predicates, which cannot in itself be described as specifically of this kind or of that, Aristotle called matter.2 We only know matter in coninnetion with form : bricks and timber are the matter or material of which a house is built, but a brick is in turn clay to which a certain form has been given; clay again is matter of a certain form; but matter by itself-that which is found in various forms, but has no

^{&#}x27;The former was said to maintain the existence of universalis onto rem, the latter of universalis in re: where the res is a concrete individual. 2 Cf. Ar. Phys. a. vii. 1918 6-12.

form of its own-is unknowable.1 It may be questioned whether Aristotle was justified in his use of the conception of matter. The material of anything is always something of a quite determinate character. Economists know in how many ways the products of one industry are 'raw material' to another. but the raw material which is rewest i a which has itself been least worked up is still matter of a perfectly definite kind. Timber is the raw material of the carnenter, but trees of the lumberman - nic iron of the ironmester, but iron ore of the smelter: and neither trees nor iron ore are any nearer being formless matter than lumber or pig iron. In the one relation, the matter (or material) is a concrete thing, in a different state no doubt from that into which it is worked up, but perfectly familiar to us as existing in that state: in the other, the matter is not a concrete thing at all, is in no state, is quite unfamiliar and indeed incapable of being known to us as such; and this relation of matter to form has no real analogy with the relation of matter to what is made out of it in the arts." It is true that in using the metaphysical analysis of the concrete individual into matter and form in order to find different subjects of the same form in different individuals. I may not at first sight seem to rely upon the conception of a quite indeterminate matter. The matter of a house, says Aristotle, is stones and timber: the form—what makes the stones and timber the matter of a house is 'to be a shelter for men and goods'. Stones and timber are determinate material, and different houses, however closely otherwise alike, are distinguished by being built of different material. But if we ask what distinguishes the material used in building one house from that used in building another, and do not find it in the kind of material, we shall have either to say that the materials are themselves made out of different material or that they just are different: in the former case we shall be assuming, in order to account for the difference between determinate materials that are the same in kind, other determinate materials the same in kind but individually different; in the latter, any further analysis into matter and form brings us to an indeterminate matter that furnishes different subjects for the same form in different individuals. The

¹ ή ΰλη άγρωστος κεθ αίτήν, Met. Z. x. 1086° 8.
1 In the foregoing criticism I am particularly indebted to lectures of Professor Cook Wilson.

proper onteoms of this line of reflection would seem to be that what makes receible different individuals of the same kind is the matter of which welst they are is predicated; and this at times Aristotle save ! and he admits that in one sense matter is substance. But the corollary, that the nature of Socrates, as predicated of this matter, is something that may be common to another, and universal. he does not draw : and it would seem to be his considered doctrine in the Melandweics (however hard to reconcile with some of his other statements) that what makes Socrates Socrates is his form. or what he is, and not the matter in which this form is realized. This form is his substance: and it is neither merely the specific. form of man, nor does it include all that can be predicated of him : but we are not told how to distinguish it from predicates in the other categories. We need not pursue the Aristotelian doctrine further: so much has been said in order to illustrate the difficulty of determining what is in the category of Substance. We may start with the concrete individual and draw a distinction amone all the things that can be predicated of him, between that which declares what he is essentially, and is his substance, or belongs to the category of substance, and that which declares about him something not essential and belonging to one of the other categories. But predicates in the category of substance seem universal, as in any other: and predicates in the other categories are not essential: hence the tendency to say that what individualizes is material substance, not universal, nor capable of figuring as predicate. If, to avoid this, we suppose that there is something about Socrates which makes him Socrates, less than the sum total of all his predicates, we shall find it impossible to say what this is. The attempt to distinguish what is from what is not essential to the individual leads us to distinguish the individual both from his emence and from his non-essential attributes; the 'first substance' is alternately regarded as the whole concrete individual and as what is essential in him; while the fact that the possibility of distinguishing the essential seems first possible when we look for the character which belongs to him as of his kind leads to the con-

¹ Cf. Met. M. viii. 1034° 5-8; and v. Bonitz, Index Arist. s. v. δλη, 786° 52-58.

[°] Cf. Met. M. x. 1085° 27-1086° 9, xiii, 1088° 8-15; H. i. 1042° 28-9. But one cannot really support any statement on the point except by reference to his whole discussion.

ception of an universal essence possessed of a sort of substantiality

of its own, a sort of 'second substance'. We shall be met later with the same difficulty, when we consider the doctrine of the Predicables, and the problem of definition. The metaphysical issue raised is fundamental. But for the present it is enough to have called attention to it. Logical and metaphysical problems have a common root. We cannot reflect upon the features that characterize our thought about things in general, without saking how things can be conceived to exist: for our most general thoughts about them are just our conception of their manner of existence. And it may readily be shown, with regard to the different categories in particular, that we could not use predicates in them, except so far as we conceived objects to exist in certain ways. Thus no predicates in the category of quantity can be used of the mind, because the mind is not extended; if it were, it might have a capacity of 8 or 80 cubic feet, and an area and maximum diameter : since it is not, we cannot apply such epithets to it at all ; and it is only because the existence of material things is existence in space, that we can call them large or small, three feet source or four feet long. In the same way, if it were not for the fact that the world is spatial, there could be no predicates in the category of place; and space also renders possible predication in the category of situation : for it contains the distinctions of up and down, front and back, right and left; and it allows the parts of a body to alter their relations to certain fixed points above and below behind and before, to the left and right of them, while the whole body remains within the same limits. This is what happens when a man lies on the sofa where he was formerly sitting, or when an hour-place is inverted on the table. And a perfectly homogeneous sphere, though it may change its place, can be situated only in one way; and if we are to distinguish a right and wrong way up in it, we must mark or single out some point in the circumference, whereby it ceases to be perfectly homogeneous; and this again illustrates how the distinction of categories arises out of the distinguishable modes of being in things. For it is because it is a figure of a certain kind,

tinction of categories arises out the distinguishable modes or being in things. For it is because it is a figure of a certain kind, that such a sphere does not admit of the same varieties of situation as a cylinder; and because it does not admit of these, they cannot be predicated of it; and if nothing could be perceived or imagined to admit of them, predicates in the category of situation, and

therefore the category of situation, would not exist. Again, there are predicates in worsh and warren because things act one on another: and the two categories are distinguishable because there are two terms erent and nations in all cancel interaction. And the different tenses of verbs which make a difference to a predicetion in time though it remains in the same category of warfin or who very, every or general. presuppose that things exist in time: otherwise how could we distinguish the meanings of incolver and incloses manufat and manufabit minit and mait site and rat? Of that which had no continuous existence through differences of time predication would be possible only for a moment in the present. But reciprocally, as we could not predicate in these categories unless objects existed in certain wave-as substances, with qualities, extended in space persisting in time &c __ en we cannot predicate about objects except in one or other category; in other words, not only are they contained in but they are necessary to our thought of any object. That which was not conceived as a substance, or a quality, or a state, and so forth, would not be conceived at all : and a concrete thing that was no substance, had no quality or state, and so forth. would be just nothing. And therefore the consideration of these distinctions belongs to logic, since they characterize our thought about objects in general; and though logic is not interested in the indefinite variety of existing qualities—blue, green, sour, shrill, soft, &c.—(because an object, in order to be an object, need not have any one of these qualities in particular, but only one or other) yet it is interested in the esterory of quality, or in noticing that an object must have some quality or other: in the category of relation or in noticing that it must stand in relations to other objects: and so on.

The idea underlying Aristotle's doctrine of Categories may be expressed thus—to discover the forms of existence which must be realized in some specific way in the actual existence of anything

predicate, we can refer them, considered separately, to different categories.

It is not necessary, however, to hold that Aristotle's list of categories is complete.

It is to be observed that the predicate of the same proposition may determine its subject in more than one category. In the proposition The other disciple did outron Peter the predicate is in the exceptly of time, for the past is a time and the event is referred to the past; and of action, for "faster than Peter is a relation. But of course, if we distinguish these different elements in the predicate, we can refer them, consolered squarket, by different categories.

whatevever. His classification may exhibit defects but the importance of his undertaking must be admitted. And many of the distinctions between terms insisted on by those who attach least importance to the Aristotelian doctrine of Categories express an attempt to colve part of the problem which he was attacking and are derived from his doctrine. Those distinctions as was pointed out in the last chanter rest upon certain fundamental features of the manner in which we conceive things to exist. The distinction between einemler and general concrete terms corresponds in the main to that between mourn and deprion obota 1; for the most noticeable of ceneral concrete terms are in the category of substance os man stone or heast though some (which might be called substantives of an attributive kind) are in other categories as for instance officer and organist. The distinction between concrete and shetreet terms corresponds roughly to the distinction between oligia and the other categories: for abstract terms formed from kind-names are as we saw, scarce and unnatural. That relative terms are predicates in the category of relation is plain. The attention paid to v collective terms reminds us that we can consider not only objects severally, but what they are in certain groupings or combinations: and the distinction between quality and state involves the same fact. The logical divisions of terms rest on differences in the being of things, as we apprehend them ; this is apt to be overlooked when the subject is approached from the side of names: Aristotle's doctrine of Categories has this advantage, that throughout it fixes our attention on things.

The Aristotelian doctrine of Categories bulks large in the history of Logic ; such conceptions are instruments of thought : the instruments forged by one generation are handed on to the next. and affect subsequent thinking. On that account alone therefore it is fair to give some attention to it; but it is still valuable as serving to express and distinguish certain important features in our thought about things. That a quality is not a quantity is a truth which those overlook who think that sound can be a wave-length in the vibration of the air; they forget that it is not possible to define terms of one category by another.8 Moreover a conception of categories not very far removed from that of Aristotle has, through

first and second substance.
 It is not meant that collective terms are in the category of State

^{*} Except as terms in a derivative category involve terms in those from which it is derived.

[Kant and Hegel, become one of the chief doctrines of modern

These admissions do not bind us to consider Aristotle's list as perfect. One important remark on it would perhaps hardly have been regarded by him as a criticism. The different categories are not all equally distinct or ultimate. Thus the distinction between mon and more is far more fundamental than that between more and minutes. A thing need not have a place because it has duration. nor can any one doubt under which category such predicates as 'at home 'and 'belated 'respectively fall. But to be acted on implies something setting: indeed, if action and reaction are equal and opposite, for a thing to be acted on implies that it acts itself; and it is often difficult to say to which of these categories a predicate is to be referred. A ship travels: are we to attribute the motion to the ship, and say that she acts, or to the engines, and may that she is acted on ? or shall we say that the engines in turn are acted on by steam? A ristotle in a measure recognized the mutual implication of these two categories, for in one place he includes them together under the single term signous. Language bears traces of it also. in deponent verbs, which have a passive form with an active meaning. and neuter verbs, which have an active form with sometimes a passive meaning. We cannot admit, as Trendelenburg and others have maintained, that the distinctions of categories were derived by Aristotle from the grammatical distinctions between parts of speech : but undoubtedly they are reflected (though in an imperfect wav) in grammatical forms. Again, as we have seen, the notions of Jyeur and selection are derivative; state presupposes the distinction of whole and part, which, in material objects at least, implies the category of more, and it presupposes also the categories of motein and marrew, and of more: for a whole is in a certain state through the interaction of parts having certain qualities, as when the body is well or ill; or through something done to certain parts of it, as when the body is shod or clad; a situation presupposes the distinction of whole and part also (a point can have place, but no 'situation'), as well as the categories of mon and moon re: for when a thing changes its situation, some part that was formerly above

another comes to be below it, and so on. On these two derivative categories Aristotel lays least stress; they are only twice includedly in his enumeration. But though derivative, they are peculiar, and contain something not in the notions from which they are derived; it is quita impossible to treat a state like health as being of the same nature with a-quality like sweetness, or place with situation that place. Kant made it a ground of complaint against Aristotle that he had included derivative conceptions in his list along with pure or underivative; but it would probably be a fairer

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1 Met. Z. iv. 1029b 25.

[criticism, that he had not taken account of all the derivative conceptions which call for recognition.

A word may perhaps be added upon Kant's doctrine of Categories. and its relation to that of Aristotle, though it is very difficult to put the matter at once briefly and intelligibly in an elementary treatise. Aristotle had sought to enumerate the kinds of being found in the different things that were : Kant was interested rather in the question how there come to be for us objects having these diverse modes of being. He maintained that in the apprehension of them we are not merely recentive and passive; on the contrary, all apprehension involves on the part of the mind the relating to one another in various ways of the elements of what is apprehended; if the elements were not so related they would not be elements of one object : and they cannot be related except the mind at the same time relates them since relation exists only for consciousness. Kant called this work of relating a function of synthesis; and he desired to determine what different functions of synthesis are exhibited in the apprehension, and equally in the existence for us, of objects. He noted in the first place, that the mere perception of anything as extended, or as having duration, involved certain peculiar ways of relating together in one whole the distinguishable parts of what is extended or has duration. These modes of synthesis we call space and time. There could be no permanent objects for me, unless I somehow held together past and future in an unity with the present : I should not be aware of my own existence as persisting through time, unless I realized myself as the same in moments which I distinguished as different: and I could not do this, unless I had an object which combined manifold successive states into the unity of one and the same thing : here then we have one function of synthesis. It is the same with any spatial whole. I must be aware at once of its parts as distinct in place, and yet related together in space; space is a system of relations in which what is extended stands. But these two modes of connecting in an unity the parts of what is manifold Kant attributed to sense, for reasons which we need not now consider : thinking, the use of general conceptions. did not enter into them; and therefore he did not include them in his list of categories, which were to be the most general conceptions by which in understanding we connect into an unity the manifold parts of an object, and so make it an object for ourselves. The perception of an object involved space and time; but perception was not enough. We think of it in certain ways, or conceive it, in apprehending it as an object. Now this conception of an object involved, according to him, four things: (1) its having quality: and quality can only exist in degrees, each of which is distinguished from and related to the other degrees of the same quality; heat only exists at a given temperature and blue must be of a given

[shade and saturation: (2) its having quantity, or being a whole composed of parts : (3) that it should be a substance kaving attributes. one or permanent through its changing and successive states, and that its changes should be determined according to laws by its relation to other substances with which it stood in interaction: (4) that every such object conceived to exist should be conceived as connected with every other existing object in a way that knowledge could apprehend and express in the form of necessary inference. The various peculiar relations involved in these requirements Kant called Categories: and he pointed out that, in all the material diversity of concrete objects as we know them, these categories or forms of synthesis exemplify themselves. Let something be presented to me: if there is nothing which I can call it, or regard it as being (for the question is one of thought and not of names), it is so far nothing for me; but if I call it sky-blue, I am thinking of it as qualified: I am using in a specific way that conception of quality which is one of the notions by which I relate together what different objects are. Of course it might have a colour unlike any colour I had seen hitherto, which I had no name to indicate : but I should still be recognizing it as coloured in a certain way, though I could not name the colour, and therein I should be using the conception of quality. If I call it a sky-blue tassel. I am using in a specific form the notion of a whole of parts: for to one who could not connect distinguishable parts in one whole a tassel would not be apprehensible as one thing; I am also using the conception of substance and attribute, when I regard it as a thing, one of whose qualities it is to be sky-blue. I cannot call it woollen, without connecting its existence and causality in a definite way with the life of a sheep; and so forth; the forms of space and time being presupposed in my apprehension of it throughout. It is not meant that these notions or categories are abstractly grasped, and guide us consciously in our apprehension and description of objects, as a doctor who had recognized that height, weight, chest measurement, and state of the teeth were important characters in determining the health of children at a given age, might use these headings in a statistical description of the children in London schools. only become aware of the part which these notions play in our apprehension of objects by reflection upon the use we have unconsciously made of them; just as we become aware in the abstract of using certain forms of inference, by reflecting upon the concrete inferences we have drawn in divers subjects. But as there would be no men if there were no animals, and no circles if there were no figures, so we should recognize no colours if we could not conceive qualities; we should never think that a horse pulled a cart. if we could not conceive a substance to have attributes and to determine changes in another substance; we should never call the movement

fof the cart necessary, if we could not think of the different real things in the world as so connected that we could infer one things from another. And in all these different ways, we are relating. or distinguishing and connecting, features and parts of what we apprehend: we are effecting a synthesis in what would otherwise be

Now it will have been seen that Aristotle also noted that what we recognized as existing were sometimes substances with attributes, sometimes attributes of various kinds: we recognize the existence of qualities; of quantities in things that are wholes or parts of such and such a size; of relations and positions in place and time; of what things do and have done to them; of their states and situations. But Aristotle approached the matter from the side of the object: he asked what modes of being we can distinguish in what we recognize to be. Kant approached it from the side of the knowing subject, and asked what were the modes of synthesis on the part of our thought, through which objects were apprehensible by us as being the sort of objects they are. If Kant is right in thinking that there could be no objects known to us, except through the mind's activity in relating according to certain principles their manifold differences, then we should expect that when we reflect upon the manner of being which what we recognize to be exhibits, we should find those modes of being which the mind by its synthetic or relating activity makes possible for itself. And if, while this in the main is true, there are certain differences between the two lists of categories, yet they can be readily explained. Aristotle's list we have seen. Kant recognized four classes of category, those of Quality, Quantity, Relation and Modality. Now Quality and Quantity appear in Aristotle's list as well (though in Kant's they are each analysed into three aspects, or 'moments'. which here need not concern us). But in Kant the category of Relation covers the three relations of Substance and Attribute, Cause and Effect, and Interaction (which last really involves the other two); the distinction of substance and attribute is present in Aristotle's doctrine. and in worsh' and wdovern' we have the recognition of the relation of cause and effect : but there is nothing in Kant corresponding to the Aristotelian category of πρός τι 3. The reason of this is that all predicates in the category of mpos really involve some other category as well: larger involves mogdy 4, earlier more 5, slave πάσχειν 1, farthest ποῦ , and loudest ποιόν 7; reciprocally, all categories involve relation, and Kant's whole point is that they are different relational functions. To Kant, who was interested in distinguishing these functions specifically, it would have been abourd to treat the function of relating generically as one of its

Passion. Place. Quantity. Action. * Relation. Ouality. • Time.

[own species 1; or to suppose that there was any other kind of relation involved when I say that Socrates was more scrupulous than Crito, or taller than Tom Thumb, than when I say he was acrupulous or four cubits high. All acrupulousness must be of some degree, and all height of some quantity, so that as far as the function of relating in the way of quantity or degree is concerned, it is equally present whether my term is positive or comparative. But from the side of the object, there are terms which relate it particularly to some definite other object; and these Aristotle placed under the category of moos re 2. It might perhaps be objected to him that all terms in the category of more TI " were also in mov " or more ", moidy" or every ", moieip " or madovery 8, ποσόν 9 or seiσθαι 10: but he would have replied that they were referred to the category of relation not because they involved qualitative or quantitative, spatial, temporal, or causal relations, but because they determined a thing as standing in some special relation (of any one of these kinds) to some other thing, and had their being not so much in themselves as in relation to something else 11. Again, terms in morey, like three-foot or vearlong', involve space or time as well as the relation of whole and part ; and Kant thought right to distinguish the perceptual syntheses of space and time from the conceptual synthesis of whole and part; hence also he objected to the presence of mov and more in the Aristotelian list at all. But Aristotle cared only to notice the modes of being that were to be found, the kinds of predicate that concrete things had, and was not interested here to distinguish the parts which sense and thought respectively play in rendering the apprehension of them possible. Once more, Aristotle included the 'derived' notions of ever and seconds with the rest, because they certainly are different modes of being; Kant, who thought them to involve only the co-operation of functions of synthesis already recognized, gave no place to them. The most considerable difference between the two doctrines is the absence from Aristotle's

¹ The reason why Kant gave the name of Relation to the three syntheses of Substance and Attribute, Cause and Effect, and Interaction was historical. He quite recognised that all his categories were really modes of relating and controlled.

a manifold.

Relation.

Place.

Time.

Quality.

State.

Vaction.

Passion.

Quantity.

Situation.

Ta spór re are defined first in Cat. vii. 6° 36 as 'what are called what

¹¹ To spok rs are defined first in Cat. vii. 9-3 Gs. what are called what hay are of another—"one one's deep rioris prings also keyren, and more closely later in 9-32 as that for which to be is the same as to be related in some way to aspide.—"one the same of the control of the control

for anything at all corresponding to the Kantian categories of or anything at all corresponding to the Mantain categories or modality, i. e. to the notions of actual, possible, and necessary as determinations of our thought about things; but their absence will not surprise us if we consider that to the question, what essentially a subject is, no one would ever answer that it was actiful tially a subject 1s, no one would ever allower. We may put the relation of the two doctrines in this way, that whereas Aristotle had classified the products, Kant distinguished the processes of that synthesis or relating, through which (as he held) objects in all their manifold variety, however much they may materially differ one from another, are all alike objects of knowledge and so far formally the same. Merely to be, said Aristotle, is not possible : ou is not a significant predicate; what is must be in a particular way, and thereby fall under one or other of the yeur rap Karnyopian which he enumerated; and all the modes of being characterize in the last resort some concrete individual thing, which exists in and through them. An object, said Kant, cannot be an object of knowledge, and therefore for us cannot exist, except through being perceived and thought in certain ways: the general ways in which an object is perceived or thought, the forms of percention and conception involved (one or another of them) in every predicate through which an object is known, are the 'forms of the sensibility -viz. space and time-and the 'categories of the understanding'."

Unless indeed it is equivalent to elois or Substance; but that is one of

the categories.

If Kant was wrong in supposing that the formal characters in an object, whose presence there he ascribed to the synthetic activity of the mind, are not merely recognized in it, but are there to be recognized through the mind's activity, yet what has been said will still express the relation which, from his point of view, subsits between Aristotle's doctrine and his own.

CHAPTER IV

OF THE PREDICABLES.

Tun distinctions to which one attention was directed in the last chapter are distinctions of terms according to the nature of their meaning: and if we understand what a term means, we may know to what category to refer it, without waiting to learn the subject of which it is predicated : large, for example is in the category of mantity, whether it be predicated of a triangle or of a gooseberry. and just in the category of quality, whether it be predicated of Aristides or his actions. Such difficulty as may exist in determining the category to which a term is to be referred arises through defect in the list of categories (i.e. of the conceptions under which we are to classify all possible predicates), or through the complexity of meaning in the term itself, whereby it involves more than one category at once, like a verb with tense; but not through the fact that we are considering the term by itself and without reference to the enhiert of which in a particular proposition it may be affirmed or denied. And the Aristotelian treatise called the Categories indicates this when it puts forward the list of ten categories as a division of terms out of syntax.1

In the present chapter we have to consider another division of terms, based upon the relation in which a predicate may stand to the subject of which it is predicated. Aristotle recognizes four such relations, and one of them he subdivides, obtaining five in all; later logicians give five, but their list is in one important respect different. According to Aristotle, in every judgement the predicate must be either the definition (δροι), the genus (γίνοι), the differentia (διαφοιά), a property (διοιο), or an accident (συμβιβηκόι) of the subject. The later list? longing night of the principle on which the division was

The mark uphysics suprisonly keyepiese leaves from chains squaise, it woods founds to point it foul is over it suched to four it seems in the Topics, at it. 19 25. "The Aristoticalin list is given in the Topics, at it. 100 11-755 the later list passed into motion. Europe through the medium of a little work to the later list passed into motion. Europe through the medium of a little work to the later list passed into motion. Every list of the later list passed in the l

made, omits definition, and includes instead species (elbos), running therefore as follows—course, species, differentia, proprism, accidens.

The distinctions are known as the Five Predicables, or more strictly as the Five Heads of Predicables. The words have passed into the language of science and of ordinary conversation; we sak how to define virtue, momentum, air, or a triangle; we say that the pany is a species of viola, limited monarchy a species of constitution; that one genus contains more species than another; that the crab and the lobster are generically different; that man is differentiated from the lower animals by the possession of reason; that quinine is a medicine with many valuable properties; that the jury brought in a verdict of accidental death; and so forth. The fact that the employment of the words is not confined to any special science suggests that the consideration of them may belong to Logic, as expressing features in our thought about all kinds of subject.

A predicable is merely that which can be predicated: viz. that

which is universal, not an individual; all kinds, qualities, states, relations, &c. are predicable, and they are universal, as was explained in Chapter II, because they may be exemplified in and belong to more than one individual subject. All names, therefore, except proper names are classified under these five heads of predicables, but proper names are not included here though they would come in the division of categories as denoting a substance The Parthenon, for example, is not the name of the genus or species of anything; nor is it that which differentiates any species from another species; nor is it a property or accident of anything. It is a particular building; and the name denotes that building, with all that it is-a temple. Doric, of Pentelic marble, beautiful by the simplicity of its proportions and the magnificence of its sculptures. the work of Pheidias and his assistants, the glory of Athens. All these things are predicable about it, and they are universals; for might not another building be a temple, in the same style, of Pentelic marble, and so forth? It, however, is not predicable: nothing else can be the Parthenon. We may ask what kind of thing is the Parthenon, but not of what things is it the kind 1

¹ To use a phrase of Mr. F. H. Bradley's, it is the 'what' and not the 'that' of things which we have to consider.

The distinctions which we have to consider, therefore, do not afford, a classification of things, but of concepts: and (unlike the categories) corresponds considered not in themselves but in their relation one to concept.

But things are known to us through concepts; and an enquiry into the relation of concepts is an enquiry into the nature of things, as we conceive them to be.

The statement that things are known to us through concepts needs a little explanation. It has been frequently pointed out that the English language uses only the one verb, 'know,' to represent two different acts, which in some languages are distinguished by different verbs 1: the knowledge of acquaintance with a thing, and the knowledge about it. In Latin, the former is signified by companies the latter by soirs: French uses remoctively the cornete words consolire and espoir : German the words demon and eviseen Knowledge of acquaintance does not come barely through concents: however much may be told me about Napoleon, and however clear a conception I may have been enabled to form of his character. I never knew him, and never shall know him, in the sense of being acquainted with him; such knowledge comes only by personal intercourse, and separate intercourse is needed with each individual that is to be known. But knowledge about a thing comes y by concepts; and without this there is no acquaintance, though this by itself does not amount to acquaintance. I may know a great deal about a man, without having ever met him; but I may in fact once have met him, without knowing who he was or anything about him; and I am no more acquainted with him in the latter case than in the former.

Now most of our knowledge is knowledge about things; things are useful and important to us for the most part not because they are such particular individuals but because of what they are; this is not equally the case with persons; and yet with persons too it is very largely the case. 'Wanted, a good coat-hand': it is not Smith, who is taken on, that is wanted, but only the coat-hand; and was the master-tailor is satisfied to know that he has engaged a coat-hand, and very often does not desire his acquaintance: if he knows about

¹ Cf. e. g. J. Grote, Exploratio Philosophics, Pt. I, p. 60 - a work and by an author less known than they deserve to be; the expressions 'knowledge of acquaintance' and 'knowledge about' are borrowed thence.

V

Rapided districts by angular ly angular ly angular ly alphanet

Smith, he can regulate his business accordingly, without knowing

It will now be understood in what sense we know things through concents: we are not thereby acquainted with them windividually but we know and think and reason about them thereby. And a concept may be said to differ from a thing in being universal not individual an object of thought and not of sense fixed and not changing completely knowable and not partially 1 Take for example the concept of a timeniece a timeniece is a machine in which the movement of wheels is so stimulated and reculated as to cause a hand or hands to move at an uniform rate (usually twice in twenty-four hours) round a dial, and by pointing to the divisions marked upon the dial to indicate the time of day. That is the concent of a timepiece: it is clearly universal, for it applies to all timenieces: it is an object of thought, and cannot be seen or felt, like the wetch in my nocket: it is fixed and unchanging, while my watch wears out or gets broken : and it is completely knowable or intelligible, whereas there is a great deal about my watch which I do not know or understand : where the metals of which it is made were quarried, and by what series of events they come into the hands of the maker: why it loses 10" to day and gains 18" to-morrow, and so forth. No one knows the whole history and idiosyncrasy of any particular timepiece, but he may have a satisfactory concept of what a timepiece is for all that.

It may be asked, in a concept merely an object of thought, with ne existence in things (as it is put, outside our minds)? or does it exist in things ?? Much ink, and even much blood, have been spilt in disputing over this question, to which some reference has already been made in speaking of the opposition between Realism and Nominalism. An elementary treatise must be content to be brief and dogmatic. Concepts, it must be maintained, have existence in things, as well as in our minds. The thing which I can pull out of my pocket, and see and feel, and hear ticking, is titself a machine wherein the movement of wheels causes hands to

¹ Concepts do not necessarily realize this last requirement; but whereas the individual cannot be completely known, a concept might be understood

completely.

Description of the complete completely.

One of the completely.

Supra, p. 41.

tall the time of day in the manner set forth in the concent of a timeniece. What I conceive a timeniece to be that (if my concept is a right concept) every particular timepiece is : what I know about things is the nature of the things, nor would it otherwise he they that my knowledge dealt with. But though concents have existence in things as well as in our minds the manner of their existence in the two cases is different in an important respect. In our minds, each is to some extent isolated : my knowledge of an individual thing is expressed niecemeal in many predicates about it: each predicate expressing a different concent, or a different feature in the nature of the object. But in the thing these features are not isolated. The individual object is at once and together all that can be predicated of it separately and successively (except as far indeed as predicates are true of it successively). In thinking of my watch, for example, I may think of it as a timeniace as an heirloom as being two inches in diameter and en on thetween these concents there is no connexion thought of they are as it were separate from one another . but they and much besides are united in the thing 2. The individual object is all that can be predicated of it (and there is no end to what might be predicated, if we knew its whole history); but one thing that can he predicated of it is not another.

An object comes into the room, which I call Tray: what is Tray? it is a dog, an animal, yelping, at my feet, mine; Tray is all these: but is a dog all these? A dog (that is, any dog) is an animal, and dog yelps; but I cannot say that a dog (meaning any dog) is mine, or at my feet; and though a dog is an animal it is not equally true that an animal is a dog, or that what is at my feet is mine, or that what is mine is at my feet.

What, then, is the relation of those various concepts to one another, which can all be predicated of the same individual? Are they united in it like stones in a heap, where the stones together are the heap? or like almonds in a stewed pippin, where the pippin

¹ This does not of course mean inside our skulls.

[&]quot;The word thing here is used first of the individual, the subject of predication, then of the universal, the character predicated. It has been used already in both these sames. The English idion allows both uses—we may say, for example, "shout that thing I know nothing"; and it may be worth while to use the word closely together in both senses, in order to direct notice to the subject of the prediction of the continuous states.

is not the almonds? or like links in a coat of mail, where the links in deed are the coat, but only because they are pseculiarly looped one into another? It is easily seen that none of these analogies is appropriate. According to Aristotle they are related in one of five ways. Take any proposition, '\(d \) is \(\begin{align*}{c} \) where the subject \(\delta \) is not a proper name, but a general concrete term, or an abstract term. The predicate \(B \) must be either definition, genus, differential, property or accident' of \(d \): one or other of these relations must subsist between the two concepts \(A \) and \(B \), in any individual characterized by them.

The statement just advanced clearly concerns the nature of our thought about objects generally: the technical terms have yet to explained, but it is the actual procedure of our thought which they profess to indicate. Logic invented the terms, but it discovered the relations denoted by them.

If we take any term that is an universal, and not an individual. and make it the subject of a judgement, then the predicate must he either commensurate with the subject, or not. One term is mid to be commensurate with another, when each can be predicated of everything whereof the other can be predicated 2: equilateral triangle and cominnoular triangle are commensurate terms, because every equilateral triangle is equiangular, and every equiangular triangle equilateral: but the term conignoular is not commensurate with conilateral, for there are figures equilateral which are not equiangular. It may be pointed out (for it is important to bear in mind that we have to deal now with the relation between the different 'universale' predicable of the same individual, and not the relation between them and the individual of which they are predicated-with the relation of 'animal' and 'mine', &c., to 'dog', and not with the relation of these terms to Trav)-it may be pointed out that when the subject of a judgement is an individual, the predicate is hardly ever commensurate 3: for the predicate is an universal, predicable of other subjects besides this individual; mise is predicable, for example, of other subjects than Tray : whereas

¹ But cf. p. 62, n. 1, inf. The Porphyrian list of predicables will be con-

sidered later.

And therefore, of course, neither of anything of which the other cannot be predicated.

Only if it is a predicate which from its nature can belong to no more than one individual, as e.g. the attributes of God.

this individual is predicable of none of those; nothing else that I can call mine is Tray. Now where the predicate of a judgement is commensurate with the subject, there it is either the Definition or a Property of it . where it is not commensurate there it is either part of the Definition is a Genus or Differentia or an Accident

The definition of enviling is the statement of its essence ! . what makes it that and not comething else. In the following judgements, the predicate claims to be the definition of the aphiest. 'An organism is a material body, of which the parts are reciprocally ends and means': 'a church is a building erected for the service of God according to the principles of the Christian religion': 'momentum is quantity of motion ': 'wealth is that which has value in exchange': 'a triangle is a three-sided rectilinear figure'; 'a line is the limit of a superficies'. The predicate states what it is that makes anything an organism, a church, a line, a triangle: what constitutes momentum or wealth, as distinguished from everything else, such as another or architecture. In these judgements it is clear that the predicate, in claiming to be a definition, claims to be commensurate with its subject; if an organism is a material body of which the parts are reciprocally ends and means, then my dog Trav, being an organism, must be that, and whatever is that must be an organism: for to be such a body is to be an organism. If wealth is that which has value in exchange, then gold, having value in exchange, is wealth, and so forth.

The genus is that part of the essence of anything which is predicable also of other things a differing from it in kind a. Each of the definitions above given begins by declaring the subject something, which other and different subjects are besides; an organism is a material body-so is a machine, or a block of stone; a church is a building-so is a stable; a triangle is a rectilinear figure-so is a square : a line is a limit—so is a point, but of a line : wealth is that which has value-so is honesty, but not in exchange, for

^{1 &#}x27;Operade uir van von vi tore sal obrias, Ar. Anal. Post, B. iii, 90° 80. We **Operate we yet out of fore an obvious, Ar. Anal. Foot. S. 11, 309 30. We may ask the question ridon;—what is it?—of an attribute (like momentum) as well as a substance (like a man or a lobster); and the answer will be a definition. In strictness we can define the obvis of an individual, if at all, only as meaning the kind to which it belongs; of the previous ch.

at all, only as meaning the kind to which it belongs; cf. the previous ch., pp. 40-44.

Thing' here again does not mean a particular thing.

Thing of devi it send a thefees and budpheres very didt. if very it sent anaryposiumen, Ar. 72p. a. v. 102° 31. The notion of a kind is here presupposed. Some discussion of it will be found below, pp. 77-98.

you cannot transfer it 1 · momentum is quantity - of motion but not of matter. These (building, rectilinear figure, limit, &c.) are the genus, in each case; and the genus, being predicable of other subjects is clearly not commensurate \$ Genus is sometimes explained as a larger class including the class defined within it : fours for example as a class including triangle square and many other anhordinate classes besides : Avilding as a class including churches. stables barracks and so forth. This explanation cannot be considered a good one for reasons to be presently stated : but it may nut some into the way of grasning a better.

The differentia is that part of the essence of anything-or, as we may say, of any species, which distinguishes it from other where in the same genus; it is the differentia of an organism that its parts are reciprocally ends and means—in this it differs from other material bodies : it is the differentia of a church, to be for the service of God according to the principles of the Christian religionin this it differs from other buildings; and so forth. The genus and differentia (or differentiae a) between them constitute the species. or make up the essence of that which is defined. The differential like the genus, need not be commensurate with its subject. The Book of Common Prayer is for the service of God in accordance with the principles of the Christian religion, but not being a building, it is not a church. On the other hand the differentia is commensurate with the subject of which it is predicated in cases where no genus except that to which the subject belongs is susceptible of the particular attribute which serves as differentia; thus a vertebrate is an animal of a particular structure which cannot exist except in an animal so that the differentia of vertebrate is commensurate with it. And it is only where this is the case that the ideal of definition is attained.

Those who sneak of the genus as a larger class containing the species or smaller class within it sometimes explain the differentia as the attribute, the possession of which marks off the smaller from the rest of the larger class. If squares and rhomboids, triangles and

¹ The honest man, however, commands in many situations a higher price, and so far some economists would reckon honesty as wealth.
¹ This must be received solypect to modification from what is said below as to the genus being in itself indeterminate, and actually different in each of its species. Cf. pp. 69-78, less.
¹ In the plumi if the genus has divers determinable points that have to be specified differently intee different species. Cf. istf., p. 85.

pentagons, &c., are all placed in the class of rectilinear figures because they have that character in common, triangles, on the hand are differentiated from the remaining classes included within that of rectilinear figure by possessing the attribute of being three-sided. Provided it is not supposed that the differentia is added to the common character of the 'larger class' in the same extraneous way that sugar is added to tea, there is no fresh harm in this mode of expression conself.

A property is an attribute common and peculiar to a subject! (and therefore obviously commensurate with it), but not part of its essence, and so not included in the definition of it. An organism, for example, is contractile, irritable, assimilates food, reproduces itself after its kind: these are attributes of every organism, and of nothing close, and therefore common and peculiar to the subject organism; but they are not in its definition. A triangle, again, has its interior angles equal to two right angles, and is half the area of the parallelogram on the same base and between the same parallels; a line is either straight or crooked (here the alternatives together are common and occuliar); and as forth.

All other attributes of any subject are accidents. An accident may be defined as non-commensurate predicate not included in the essence: or as an attribute which equally may and may not belong to a subject. The latter is the better definition, because it tells us what an accident is, whereas the former only tells us what it is not. It is an accident of an organism to be used for food; for it may be so used, but need not. It is an accident of a church to be a cathedral; some churches are cathedrals, and some are not. It is an accident that a contractor should be an honest man, and an accident that the should be a rogue; for reguery and honesty are both commatible with being a contractor.

^{&#}x27;The subject being, it must be remembered, an 'universal', not an individual. I cannot speak of rejuing as an attribute common to Tray, but I can speak of it as an attribute common to the dogs i. a belonging to the dog nevery instance. Artistoils sometimes spoke of an attribute positiar to an bate speculiar to one out of a certain definite number of kinds, and therefore serving to distinguish it from them (though found perhaps again outside their number) as relatively properties; thus it is a property of man relatively to any quadraped to go on two legs; but as also does a brief. He given in the text, and not (in his view to proper a use. Cf. Top. c. i. 'G. A.r. Pop. a. v. 102° 4.14. C. Top. c. i.

The doctrine just illustrated presents many points for consideration, of which the following are perhaps the most important :-

- 1. how to understand the analysis of a definition into genus and differentie .
- 2. the ground of the distinction between the essence of anything and its properties.
- 8 the entitlesis between enrident on the one hand and all the other heads of predicables on the other.
- It will be most convenient to consider the third of these points first

When we classify the members of a genus or class, we sometimes. after specifying as many distinct species as we can think of, add another to include anything that does not fall within any of these : I may arrange my books, for example, into historical, philosophical, philological, scientific, and miscellaneous-the last division being merely added in order to receive any book which does not fall within the others, though the miscellaneous books have no common character that distinguishes them all alike from the rest. Now accident is a head of predicables which includes any predicate that is neither definition, genus, differentia, nor property of its imbiect! but it is not a heading like 'miscellaneous' there is a very definite and important difference between the relation of those predicates to their subject which are classed as accidents, and that of those which fall under the other heads; the latter belong to their subject necessarily and universally, the former do not

Of any individual, as we have seen, an infinity of predicates may be asserted. Some of them are seen to be connected, or (as we may express it) have a conceptual connexion: i.e. if we rightly conceive one predicate, we see how it involves another. Trav. for example, is a dog and an animal; and these predicates are concentually connected, because the concept of a dog involves that of animal. My watch has hands, and there is a conceptual connexion between having hands and being a watch, since without hands a watch could not fulfil the task of telling the time, which is part of the concept of it as a timepiece. But there are also many predicates which coincide 2 in one and the same individual, without being conceptually connected. Besides being a dog, Tray is mine,

¹ Συμβιβηπός δέ έστιν δ μηδέν μέν τούτων έστί, μίτο όρος μίτο ίδιον μήτο γένος, Ar. Top. c. v. 1020 4.

Coincident is really a better translation of grouf Gracie than accident.

and was born at Bishop Anckland : now there is no reason in the nature or the concent of a dog, why it should belong to me, nor in a thing being mine why it should be born at Bishon Auckland, nor in being born at Rishon Auckland, why it should be mine, or be a doe. No doubt in the case of this particular doe Tray, there is a reason why he is mine and a reason why he was born at Bishon Auckland : but the reason for the first fact (which may be that he was given me) has nothing to do with the reason for the second (which is that his mother was there at the time) - nor has the reason for either anything to do with his being a dog: he would have been a dog still, if he had never been given to me, or if he had been born at Bishop's Lydeard. Of course with sufficient knowledge the presence of all its attributes in any individual might he explained . but the explanation would be largely historical . we should need to know the history of that individual, in order to see how it was that so many different and apparently unconnected things all came to be predicable of one and the same subject. On the other hand, where two predicates are concentually connected. there it is not by knowing the history of an individual that we determine whether, if one is predicable of it, the other will be,

We have here the great difference between science and history: science consists in tracing the connection of universals; history intending their coincidence in individuals. The two no doubt utilize one another. It is by noticing how attributes are historically found conjoined or disjoined in divers individuals that we learn which are really connected together; while again the discovered connexions of attributes, or the 'laws' which science establishes, help to explain the history of individuals. And when the assemblage of historical events is resolved into instances of the connexion between matters which, if we understand their nature, we can see to be involved one in another, bistory becomes scientific.

That the accidental should be opposed to what is necessary and universal conforms to the usage of common speech. Sir Robert Peel was killed by a fall from his home, and we say his death was accidental. Why? he was a man, and for a man it is necessary to die, and for any one who falls in that particular way it may

¹ The illustration of this forms a considerable part of what is called Inductive Logic; we shall find that many connexions are inductively established whose necessity remains unconceived.

be necessary to die; but it is not necessary that a man should fall in that way; that is not predicable universally of man. We sometimes dipute whether there is such a thing as chance in the world, or whether everything has a cause, and happens necessarily. Few people really believe that anything happens without a cause; but chance is not the negation of cause; it is the coincidence of attributes in one individual, or events in the same moment, when each has its cause, but not the same cause, and neither helps to keccont for the other.

If we been in mird this fundamental contrast between the accidental and the necessary, we shall not be inclined to think that Aristotle was engaged in a trivial pursuit when he attempted to classify the various relations in which a predicate might stand to its subject. Discussions as to what we mean by cause occupy much space in many modern treatises. Now the causal relation is also a relation between universals: my dog Tray velps not because he is this individual Tray, but because he is a dog, and unless any dog velned it would not be because he is a doo that Tray does so But when we call one thing I the cause of another, the real relation between them is not always the same; just as when we say that A is R the relation of R to A is not always the same. It might be supposed that if one thing X is the cause of another Y, then you could not have X without Y, nor Y without having had X. And vet we say that molecular motion is the cause of heat, that the heat of the sun is the cause of growth, that starvation is sometimes the cause of death, that jealousy is a frequent cause of crime. We should in the first case maintain that the cause and effect are reciprocally necessary: no heat without molecular motion, and no molecular motion without heat. In the second, the effect cannot exist without the cause, but the cause may exist without the effect: for the sun shines on the moon, but nothing grows there. In the third, the cause cannot exist without the effect, for starvation must produce death, but the effect may exist without the cause, since death need not have been produced by starvation. In the fourth case, we can have the cause without the effect, and also the effect without the cause; for jealousy may exist without producing crime, and crime may occur without the motive of jealousy. It is plain.

¹ Thing being here again thing of a kind, or universal, not individual.

then, that we do not always mean the same thing by our words. when we say that two things are related as cause and effect : and any one who would classify and name the various modes in which two things may be causelly related would do a great service to clear thinking. Now that is the sort of service that Aristotle attempted in distinguishing the heads of predicables. Many predicates are asserted of the subject A. Those are accidents, whose cause does not lie in the nature of A as such, or which, when they belong to any individual of the kind A do not belong to it because it is A. The rest are in some way or another connected causally with A. and are predicable of any individual because it is A. Whether Aristotle's account of the different modes of causal connexion between a subject and a predicate is satisfactory is another question, involved principally in that of the value of his account of 'property'. But that the theory of predicables is closely akin to the question of the various senses in which one thing can be the cause of another may be seen by this; whenever science tries to find the cause not of a particular event, such as the French Revolution (whose cause must be as unique as that event itself is), but of an event of a kind, such as consumption, or commercial crisis, it looks in the last resort for a commensurate cause. What is that exact state or condition of the body, given which it must and without which it cannot be in a consumption? What are those conditions in a commercial community, given which there must and without which there cannot be a commercial crisis?

The kindred nature of the two enquiries will be further seen, by looking at certain cases where it is disputable whether a predicate should be called an accident of its subject or not; for an exactly parallel difficulty may arise in determining whether one thing shall be called the cause (or effect) of another or not. An accident is a predicate, the ground for whose existence in the subject does not lie in the nature of that subject as such. Hodge drives a plough; and a full knowledge of his history would show me why be drives a plough, and the ground for it therefore lies in the history of the subject Hodge; it is not of him that driving the plough is predicated as an accident. But a man drives a plough. That is an accident; for the subject now is not Hodge, but man, and it is not in the nature of man as such that the ground or reason of driving a plough lies; else should we all be at the plough.

And yet no animal but man can drive a plough : so that it is partly because he is a man that Hodge drives it: and therefore. when it is said that a man may drive a plongth, the relation of the predicate to the enhiest seems not completely socidental Contrast the statement that a cow may be knocked down by a locomotive. There the nature of the subject as a cow contributes nothing: it is in no wise necessary to be a cow, in order to be knocked down by a locomotive 1; and the relation is nursly eccidental

If we consider these two examples, we see that our account of an accident, just given, may be interpreted in two ways. A predicate may belong to the subject of which it is predicated accidentally either

- (1) when the ground for its existence does not lie completely in the nature of that subject as such 2 or
- (2) when the ground for its existence does not lie at all in the nature of that enhiert as such 2.

The first interpretation would rank as accidents of a subject all predicates that are not either part of its definition, or else common and peculiar to that subject, i. e. properties in the strictest sense; and such, if we take him at his word, is Aristotle's view. But we are then required to say that it is an accident of money to be valuable, since it would have no value if there were nothing to buy with it: or of coal to burn, since it would not burn in a vacuum. The second interpretation would refuse the name of accident to anything that could be said about a subject, however rare and disconnected the conjunction of circumstances through which it came about. where the nature of the subject as such a contributed anything at all to the result. Thus we could hardly call it an accident that an animal should die of overesting itself, since it must be an animal in order to eat. In practice we make a compromise between these

So far as a cow is a body, and only a body can be knocked down, it must be allowed that the nature of a cow contributes something to the accident; but the second sentence will stand without qualification. See it will be a supported to the contribution of the second sentence will stand without qualification. See it wises that it is not the individual, but the subject as something of a sheaf about which we ask whether its nature contains in any degree the ground of the prodicate. To be knocked down by a loomotive may be an accident, as regards a cow as each, i.e. as cow; but it would be about to my that the particulator ow contributed nothing to the societient, since it could not have been knocked down if it had not been there.

¹ So far as a cow is a body, and only a body can be knocked down, it

extreme interpretations. We call it a property rather than an accident of belladonna to dilate the pupil, though the result depends as much upon the nature of the muscles as on that of belladonna : we call it an accident rather than a property of the plough to be a favorrite sign for country inne though its necessary familiarity to countrymen accounts for its selection. The further pursuit of these difficulties does not concern us now - but it remains to be shown that they arise in regard to the relation of cause and effect. Is the cause of an effect that, given which and without anything besides the effect follows? in other words must it contain the whole ground of the effect? then a smark is never the cause of an explosion, for it will produce no explosion without powder. Is the cause anything, however slight, without which the effect could not have occurred? in other words is that the cause which contributes anything whatever to the effect? then are cooks the cause of health, since there would be little health without them.

The antithesis between accident and the other heads of predicables needs perhaps no further illustration. We may return to the first of the three points enumerated on p. 63, viz. how to understand the analysis of a definition into renus and differentia.

It should first be noticed that definition is never of an individual. but always of what is universal, predicable of individuals—whether it be what we call their 'kind', or some state or attribute of them, or relation in which they stand. For what is defined is thereby marked off and fixed in our thought, so that we have a determinate concept of it : but the individual is made the individual he (or it) is by an infinity. of attributes; he is as it were the perpetual meeting-place of concepts; we can neither exhaust what is to be said of him, nor make a selection, and declare that this is essential to a true notion of him. and that unessential. Moreover, even if we could, we should still only have got a notion of what he in fact is, but a second person also might be: for every notion is universal. What makes him this individual and not another we should not have defined, nor could we : for there is something which makes me me over and above what can be predicated of me : else, what makes me me might also make you you; for what can be predicated of me might be predicable of another; and then why does the same character make me me and you you, and not rather make me you and you me, or each of us both?

We can only define then what is universal, or a concept. But

we have already said that concents express the nature of things: and therefore in defining concents, we may define things, so far as they are of a kind but not as individuals. It is sometimes maintained that definitions are not of thines, but only of names 1: that they set forth the meaning (or, as it is also phresed, the connectation 1) of a name, but not the nature of a thing. Yet names are only used to convey information about things; and to explain what the name means is to explain what the thing is said to be. Definitions then are not really of names : but we shall see later the difficulties which drove men into saving so.

Now when we define we analyse: and the elements into which we analyse that which is defined are called, as we saw, genus and differentia. These might be called attributes of the subject : it might be said, for example, that rectilinear fours and three-sided are attributes of a triangle. But the expression is not quite appropriate : for an attribute implies a subject beyond itself, to which it belongs: but the parts of a definition themselves make a whole. and coalesce into the unity to which they belong. This may be best explained by a contrast. We may take any attributes we like-say far, sour, pink, soft and circular-and we may give one name to the aggregate of these. But they do not form one notion ; they remain obstinately five : nor by considering a thing as far. sour, pink, soft and circular, can we construct the concept of one thing. If we took a single name to signify the possession of these attributes, we could explain the name as meaning that assemblage, but we should feel that in so doing we were merely explaining a name, and not defining anything. But when we analyse into genus and differentia, this is otherwise; then we feel that the two together really make a single notion. They have such a connexion in their own nature as makes one fit the other, so that they constitute the essence of ose thing, or state, or quality, or relation. And the reason for the parts of a definition being one s is this: that they are not attributes independent but coincident, but the genus is the general type or plan, the differentia the 'specific' mode in which that is realized or developed. Let us take again the

e.g. Mill, Logic, I. viii. 5.
On 'connotation' of. infra, c. vi.

That the parts of a definition are one is a thing on which Aristotle frequently insists and mays that the main problem about definition is to show how that can be. Cf. e. g. Met. Z. xii, H. vi.

definition of a triangle. It is a rectilinear figure: but that by itself is an incomplete notion. There cannot be a rectilinear figure without a definite number of sides, though any definite number will do : and if the number in a triangle is three then three-sidedness is the specific mode in which the general plan, or as we may say the potentialities, of rectilinear figure are realized in the triangle. We may say that the genus and differentia are one, because they were never really two. Three-sidedness can only be realized in a figure, rectilinear figure can only be realized in a definite number of sides. The genus therefore never could exist independently of a differentia, as soft may of sour : nor the differentia of the cenus. It may be said perhaps that though three-sidedness can only exist as the form of a figure, rectilinear figurehood exists independently of three-sidedness in the square, the pentagon, &c. But it is not quite the same thing in the square or pentagon as it is in the triangle. So intimately one are the differentia and the genus, that though we refer different species to the same genus, yet the genus is not onite the same in each: it is only by abstraction by ignoring their differences, that we can call it the same. Triangle and square and pentagon are all rectilinear figures; but in the sense in which they actually are such, rectilinear figure is not the same in them all. Thus the differentia modifies the genus, and the genus also modifies the differentia. It might be said that three-sidedness is not confined to the genus figure: for a triangle is a three-sided figure, and N is a three-sided letter. And doubtless, so far as the penus is the same in two species, the differentia may be the same in the species of two genera. But three-sidedness is plainly different in the figure, where the sides enclose a space, and in the letter, where they do not: and the genus as it were fuses with the differentia, so that each infects the other through and through.

For this reason the genus is not well described as a larger class including the smaller class or species within it. For the word class suggests a collection, whereas the genus of anything is not a collection to which it belongs but a scheme which it realizes, or a unity connecting it with things different from itself. It may seem first plain-speaking, without any metaphysical nonsense, to say that a genus is a class of things that all have certain features in common; and that its species is a smaller class composed of some of those things, which all possess not only the features common to the

whole groups but others not belonging to the other members of it. But what is really meant by being included in a class? The phrase is sometimes not forward as if it were simple and presented no difficulty : but such is not the case. The words 'to be within' or to be included in ' have many meanings, and we must know what meaning they bear in the phrase 'to be included in a class', before we can know what that phrase signifies. We may distinguish in particular two meanings, which are quite inapplicable to the relation between a genus and its species; but they are more easy to green than the meaning in which the species can be said to be included in the genus because they can be in a manner represented to the menses: whereas the relation of evenus to species can never be represented to the senses, but only apprehended by thinking. Because one of these inapplicable meanings is readily suggested to the mind. when we are told that the cenus of a thing is a class in which it is included, we fancy that the expression helps us to understand what a cenus is: for these inapplicable meanings are easily understood. But as they are inapplicable, they help us not to understand but to misunderstand the logical relation of genus and species.1

In the first place, one thing may be included in an envelope, or as Mr. Pickwick and the wheelbarrow were enclosed in the pound. In this case, all that is included may be removed, yet that in which is was included will be left. Such is clearly not be sense in which species are included in a cenus:

for there would be no genus left if the species

vanished. Yet the logical relation is often represented by a diagram, which inevitably suggests this sense. Two circles are drawn, one enclosing the other; the genus being represented by the outer and the species by the inner circle. It is not impossible to use such diagrams without being influenced by their obvious suggestions; yet their obvious suggestions are false, and to avoid them is difficult.

Secondly, a thing may be included in an aggregate, which is constituted by that and all the other things included along with it.

¹ Though the relation of a species to individuals is not the same with that of genus to species in all respects, yet what is said here upon the vice of calling the genus a class in which species are included applies equally to the habit of calling the species a class including individuals.

In this sense a cannon-ball is included in a heap, and a particular letter in the pile on my table. We do actually use the word class on some occasions to indicate a total formed in this way; in a school, for example, a class is a cortain number of boys taught together, and when a boy is moved from one class to another, he is sent to do his work with a different set of boys. Here we have a notion which is so far nearer the logical notion!, as that the class would disappear upon the disappearance of what is included in it. But a little reflection will show that the logical relation of genus to species is no more like that of an aggregate to its members than it is like that of an earelope to its contexts.

If Tom Smith is in the first class in his achool, I should look for him among the boys in a particular class-room; but if a triangle is in the class figure, or a Red Admiral in the class lepidopters, that does not mean that I should look for either in a collection of figures or of lepidopters; it is true that a collection of these objects would include specimens of the triangle or the Red Admiral; but they do not belong to their respective genera because they are in the collection; specimens of them are placed in the collection because they belong to the genera. Were it otherwise, I could not say that a triangle is a figure, or that a Red Admiral is a lepidopteron, any more than I can say that Tom Smith is the first class; I could only say that as Tom Smith is is the first class, so a triangle is is the class figure, and a Red Admiral is the class lepidoptera; whereas it is characteristic of this to be a lepidopteron, and of that to be a figure.

The 'class' to which species (or individuals) are referred is apt not to be thought of as something realized in its various members in particular way; but the genus is something realized in every species (or, if it is preferred, in the individuals of every species) belonging to it, only realized in each in a special way. The differentia carried out as it were and completes the genus. Individuals are not included in one genus because agreeing in certain attributes, and then in one species within the genus because agreeing in certain other attributes that have no connexion with the first; as you

¹ i.e. the notion which the phrase 'to be included in a class' must bear in logic, if it is to be used in any applicable some at all. But even a class at school is not a chance collection, but a collection of boys supposed to share the same level of attainments.

might include in one island all men who had red hair and then rail off senarately within it those of them who had wooden legs: wooden-legged could not be a differentia of the genus red-haired : it must be some modification of red hair itself, and not of the man having it, which could serve as a differentia to that genne. It is therefore a phrase that may mislead, to say that the differentia added to the genus makes the species, or makes up the definition. For adding suggests the arbitrary juxtaposition of independent units: but the differentia is not extraneously attached to the genus: it is a particular mode in which the genus may exist. And hence, when we distinguish the various species of one genus, in what is called a logical division 1, assigning to every species the differentia that marks it off from the rest, our several differentiae must be themselves homogeneous, variations, as it were, upon one theme and, because each cognate with the same genus, therefore cognate with one another. If triangle, for example, is regarded as a genus. and one species of it is the equilateral, the others will be the isosceles and the evalence, where each differentia specifies certain relations in the length of the sides: if one species is the right-angled, the others will be the obtuse, and the sente-angled; where each differentia specifies certain relations in the magnitude of the angles. The principle that the differentiae must be thus cognate is technically expressed by saving that there must be one fundamentum divisionis: this, however, has its proper place of discussion in the next chapter.

To define anything then per genus et differentiem is to put forward first a relatively vague notion and as it were the leading idea of the thing, and then to render this definite by stating in what way the leading idea is realized or worked out. And the differenties are of the enseme of the things, because they belong to the working out of this leading idea. In the definition of organic species (inorganic kinds we will consider later) this is what we aim at doing. We start with the general notion of an organized body, and classify its various forms in such a manner as to show how this scheme is resliked in successively more complex ways. Our first division is into unicellular and multicellular organisms (protozoa and metazoa): the former obviously admit of no composite cellular structure; in a multicellular organism there must be a method of constructing the system of parts. Hence we proceed to differentiate of the first of the constructing the system of parts. Hence we proceed to differentiate

these according to the principal modes of structure which they exhibit on this basis is founded for example the division of the metazoa in the animal kingdom into coelenters and coelomats: of coelomata into a number of 'phyla' (dûla), the platyhelmia or flat-worms, annelida or worms, arthropoda, mollnaca, echinoderma and chordata; of chordata, according to the form which the nervecord assumes, into hemichords, prochords, cephalochords and vertebrata; and of vertebrates, according to the different forms which the general principle of vertebrate structure may assume, into fish. dipnoi, amphibia, reptiles, birds and mammals. When it is said that we start with the general notion of an organized hody it is not of course meant that historically, in our experience, that is what we first become acquainted with. We first become acquainted with individual plants and animals and we are familiar with their various species-with horses, dogs, and cattle, oak and apple and elm-long before we have settled with correlves what is the leading idea, and how it is developed and worked out in them all so as to make them the kinds of things they are. The cenus is that with which, when we have acquired an insight into the nature of these various kinds, we then start : it is first in the order of our thought about them when we understand them, not in the order of our acquaintance with them when we perceive them. According to the Aristotelian formula, it is divers nootrecon, or how nootrecon, not hule woorscov: first or fundamental in the nature of the thing, and in the order of our thought, but not what strikes us first. And Aristotle also expressed its function by saving that the genus is, as it were, the matter, fan, of the species or kind.

In saying that a genus is related to its species as matter to form,

The extent to which, in subordinating species and genera to a superior genus, a common type or plan can be definitely traced through them all, may vay different stages of a classification. The same functions of saimal life stages of the same stages of the same stages of the same traces of saimal life time complarity of metanos, in coelecters and coelemata; but it would difficult to give any one diagrammatic representation of the structure of all these, or evan of all metanos. Such representations are given for coelecters in general, and coelemata is general, yet they are a neare ostiline, in which even the principal organ of many important types are sacrificed. On the other hand, for each separate phylim among the coelemates conjected can give a representation, in which a place is found for every principal organ development, also more stages of life or other skills exhibit; and for the subdivisions of the vertebrata this can be done more adequately than for the subdivisions of the chordata.

the relation of matter to form is conceived as that of the less developed to the more developed, the potential to the actual, A word of caution is necessary here. We often compare two particular chiecta one a 'hone-shaker' and a modern hicycle and observing that one carries out more completely certain features imperfectly present in the other call them respectively more and less developed. The same thing may be observed in the arrangement of a picture gallery, where the pictures are placed in such an owler as will exhibit the oradnel development of an artist's style. or of the style of some school of artists and in a museum, where the development of the art of making flint implements is illustrated by a succession of specimens each more perfect than the last. Now in all these cases, the more and the less developed specimens are all of them concrete individuals: each has an actual existence in space and time. But with genus and species it is otherwise. They are not individuals, but universals; the cenus does not exist side by side with the species, as the bone-shaker exists side by side with the best bicycle of the present day : and you cannot exhibit evenus and species separately to the senses. It is our thought which identifies and apprehends the generic type, say of vertebrate, in the different species, man and horse and ox : and in thinking of them. we may say that the single type is developed in so many divers ways: but genus and species do not exist in local or temporal succession, the less developed first, and the more developed later. like the specimens which illustrate the development of a type or style. Obvious as these remarks may seem, they are not superfluous, if they help to guard against the idea that a genus is something independent of its species.

[It would be travelling too far beyond the limits of an elementary work to enquire into the meaning of arranging individuals in an order of development: whether (like plants and animals) they proceed one from another in a true genealogical series, or are manifactured independently, like bicycles or arrowheads. A criticism of the conception of development is however of great importance; for the complacent application of the notion to disparate subjects, and the third process of the complacent application of the notion to disparate subjects, which was not the subject of the complacent application of the notion to disparate subjects. When the content of the con

(by the conception in the relation of genus and species. We cannot throw any light on the relation of genus and species by comparing it with what subsists between individuals at different stages of 'evolution': but we may get some light upon the conception of evolution from reflection on our conception of the relation of genus to species. For the 'evolution of species' is generally supposed to be not mere change, but development; vet it is often supposed also to involve nothing of the nature of purpose, or design.

Now unless we find, in considering individual objects, that there is a plan, purpose, or idea suggested to us in what we call the less developed, but not adequately exhibited there as we conceive it, and that this same plan, purpose, or idea is more adequately exhibited in what we call the more developed object, we have no right to call them more and less developed at all. The relation therefore is not between the objects as individual, but between their characters: we cannot identify with the less developed individual the plan. purpose, or idea which is less developed in it: there is the same plan at different levels of development in each individual : and the plan at different levels of usvelopment in each mutration; and we evolutionary history of individuals must be a manifestation of a plan or of intelligence in them, unless we are to say that there is no real development in them, but only change, and that to call this change development is to read into things a fancy of our own.]

[In the first chapter, the antithesis of form and matter was employed in explaining how a common character might belong to divers objects. Two shillings, for example, may be said to be of the same form, while the matter in them is different: and two propositions to be of the same form, or far as each sacrate a predicate of a subject, while their matter—i.e. the actual subject and to species as matter to form, it is implied, as between two species as matter to form, it is implied, as between two species, that their common genus, the 'matter', is that in which they agree: while the specific form assumed by this matter in either is the basis of the distinction between them. Indeed, the phrase 'specific differences' implies that their differences constitute their form. It may seem strange that whereas in one sense matter is that which is different in things of the same form, in another is that which is different in things of the same form, in another is that which is different in things of the same form, in another is that which is different in things of the same form, in another

it is that which is the same in things of different form.

A little consideration will show that the common notion in both
these uses of the term matter is the notion of something undeveloped,
With regard to the phrase that calls the genus the matter of the
species, this point has already been illustrated. And when we
contrast, in a builing, the matter (silver) with the form, this is still
the case. We regard a shilling as an object having a certain form
(that might also be stamped in gold or copper) impressed upon

is certain matter, silver: and say that both are necessary to its heine a shilling. Now the matter here is really silver as of no shape. A disk of silver may be put into the die and stamped : but such disk is not the mere matter of which a shilling is made: it is the matter in a different form . but because the silver may have the form of a shilling, and may have the form of a plain disk, it is possible for us to distinguish between the silver, which is present alike in the disk and in the shilling, and the form which the silver assumes in the minting. The matter of a shilling is thus not silver in another shape, but silver without regard to its shape : the metal as it is present equally in the disk and in the shilling : now silver does not actually exist except in a particular shape; and in thinking of it in abstraction from its shape, our thought of it is incomplete. As the genus only exists in the species, so the matter, silver. only exists in some form. It is however true that there is no special relevance between the nature of silver and the shape of a shilling whereas the specific form of man can only be realized in the genus vertebrate : and hence the conception of development applies more closely to the relation of genus and species, than to the relation of matter and form in a concrete object.

Many controversies have been waged over what is called the principies is individual to the what is that makes one individual distinct from another individual of the same species? Some of the schoolmen held that, being of the same species or form, they were no matter, that every angel is of a different species: except their species, there is nothing by which they can be distinguished from each other. We may be less ready to dogmatize with confidence about angels than were the schoolmen; but the fashion of deriding their speculations because they were exercised in solving that kind of questions is fortunately in diminished vogue. The problem of the principium individuations is a serious philosophical problem. It may throw some further light on what has been said of the

It may throw some further light on what has been said of the antithesis between matter and form, to point out that matter cannot really be the principium individuations. Two shillings which have the same form are said to be of different matter. Now their matter is silver: but it is not because it is made of silver that one shillings agree; it is because they are made of different masses or pieces of silver that they are different shillings. But if so, it follows that to be of nilver is a character common to both pieces (quite apart from their being of the same die); and though we say they differ in matter, we mean that though of the same matter, they are differents pieces of it. The problem of the principium individuation is not therefore solved by the distinction of matter and form; the shillings are different, though of the same form, because in each that form (is stamped upon a different piece of silver; but the pieces of silver themselves present the same problem, of a common form (the nature of silver) in different inividual objects. Matter is indeed, strictly speaking, not a particular thing or an aggregate of particular things, but a generic conception. We recognize various species of it, which we call elements: the elements are different forms of matter; pad in calling them so, we imply something common to them all, as we imply something common to man and or calling them both animals; though we are less able in the former case than in the latter to form any conception of the common conservice character in abstraction from its assection from the section of the common of t

It hardly needs now to be pointed out, that where the predicate of a proposition defines the subject, it is related to its subject far otherwise than where it is an accident. We realize (or we should realize, if our definitions were what we aim to make them) that the genus, modified or developed in the way conceived, is the subject; the definition and that which is defined am not two but one. Of course, when a green thing is equare, the same particular thing is obth square and green; the green thisg and the equare thing are one thing; but here the subject is not an universal, and we have only to recognize the coincidence of attributes in the same individual. Being green and being square are not one, as being a triangle and being a three-aided rectilinear figure are '; there is a conceptual unity between these; between those only an accidental.

It follows that there is a conceptual counsaion between any of the subject sees that it must be what is predicated of it as its genus or its differentia. What belongs to the essence of anything sust belong to it; for else it would not be that kind of thing, but something different.

We may now take up the last of the points raised on p. 62—the second in the order in which they were there stated viz. the ground of the distinction between essence and property; since the last paragraph suggests the question, What do we mean by the essence? If the essence of anything be what makes it what it is, of course it would be something different, were any element in its essence wantine: but what makes it what it is?

Aristotle would express this by saying that το χλωρόν may be τντρόγωνον, but το χλωρόν είναι is not το τντρογώνεν είναι—the green is square, but green is not squareness; whereas triangularity is three-sided-rectilinear-figurehood.

Those who hold the view, already mentioned, that definition is of names only and not of things, have an answer ready here agreeable to that view. They say that we cannot tell what makes anything what it is, but only what makes it what it is called : and that the world might have been spared much useless controversy, if men had realized that by the essence of anything they meant no more than the attributes which they agreed should be signified by a general name: or, as Locke called it 1, the nominal essence. Pushed to its logical conclusion, such a doctrine makes all the distinctions of predicables arbitrary; for if the nature of the thing denoted by a general name X is not to determine the signification of the name. we can attach to the name what concent we please and it will rest with us whether the concept shall be one with which a given predicate is conceptually connected or not, and therefore whether it shall be an accident of X, or stand in some other relation to it. And if we were to regard only the definitions of geometry, it would appear a gratuitous paradox to maintain, that men determined arbitrarily what to include in the definition of circle or triangle. and what to omit. Every one recognizes that you declare better what a triangle is by saying that it is a three-sided rectilinear figure than by saying it is a rectilinear figure whose angles are equal to two right angles; or a circle, by saying that it is the figure generated by the revolution of a straight line round one of its extremities remaining fixed, than by saving that it is a figure having a larger area than any other of equal perimeter. What has led men to suppose that definition is a matter of fixing the meaning of names is the difficulty found in defining natural kinds, i.e. the various species of animal, plant, or inorganic element; in demair they have looked to the mignification of the name for the only meaning of the essence of the object. The definition of abstract notions like wealth or crime or liberty has lent some support to the same view. In these cases, the object defined cannot be presented to the senses in an example, as can gold, or the holm-oak, or the buffalo; we cannot be sure therefore that different men intend to define the same thing, when they offer definitions of such notions; and instead of settling first by its appearance that a given act is a crime, or an object wealth, or a state one of liberty, and then

1 v. Essau, Bk. III. c. iii. § 15.

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arguing to its nature from our definition, we have rather to determine whether it is to be called a crime, or wealth, or a state of liberty by considering whether its nature is such as mankind, or particular writers, have agreed to signify by those names. Hence it might appear that in the case of abstruct terms 1 at any rate, convention settles what the essence of them shall be; in the main it is not really so, even with them; for the understanding of facts would not then be facilitated as it is by the substitution of 'better' for 'worse' definitions of abstract terms; but the plausibility of the view here adds weight to the arguments which are drawn, in the manner we must now proceed to show, from the definition of matural brinds.

Suppose that we wish to define the natural substance dog, or gold. The forms of language recognize a difference between a substance and its attributes; for we say that Gelert is a dog, but not that he is a faithful; and speak of a piece of gold, but not of a piece of heavy. Yet when we define a substance we can only enumerate its qualities or attributes and leave out of account what it is that has them. What attributes of Gelert then are we to enumerate, to explain what we mean by calling him a dog? or what attributes of a wedding-ring, to explain what we mean by calling it gold? In each case a certain fixed nucleus, as it were, of attributes, holding together in repeated instances and through great varieties of circumstance, is included in our concept of an object called by such a general concrete name. But which attributes are to form this nucleus, and on what principle are we to make our selection? If it be said that we are to include every attribute common to all door, or all gold, two difficulties arise. The first is that we

Such complex abstract notions were called by Locks 'mixed modes', which he said we could define, because we had first made them by putting together simple notions (or in his language, simply most was perfectly acquainted. The expression and well despited that not established the second of the contract of the same of

theful to have an appropriance capressor.

We have, however, seen, in discensing genus and differentia, that those cannot well be called attributes. But it might be urged, that although they cannot be attributed to another the tribute of the called attributed to another the cannot be attributed to another the called attributed to the called a called as having such other attributes as mangy or fine-drawn; cl., however, pp. 41-44, supp. 41-44, supp. 41-44, supp.

should include in our notion of dog or of gold all the properties, as well so the attributes that are to constitute the definition: for the properties of a kind are the predicates common and peculiar to all the individuals of that kind and hence we should still lack a principle upon which to discriminate between property and essence. The second difficulty is more serious. We are to include in our definition of a kind every attribute common to all individuals of that kind : but until we have defined the kind, how can we tell whether a particular individual belongs to this kind or another? Let the definition of cold be framed by collecting and examining every piece of gold, and noting down the attributes common to them all: the task is impossible in practice, but that might be overlooked: it is however, vicious in theory: for it implies that we already know what cold is, or what makes a particular object a piece of gold, and can by that knowledge select the objects which are to be examined as specimens of gold, in order to determine the nature of that substance. Thus we seem to be moving in a circle; what is gold is to be settled by an examination of the things that are gold: what things are of gold is to be settled by knowing what gold is.

Hence our selection must be arbitrary; for we have no principle to make it on. We may take a particular specific gravity, the power to resist corrosion by air, ductility, malleability, and solubility in aqua regis; and say these constitute gold, and are its essence. And in that case its colour is a property, or for all we can tell, an accident; for we can see no necessary connexion between a yellow colour and all or any of those attributes, and if we found a white metal with those five attributes we should have to call it gold. But if we chose to include yellow colour with them in our definition, then nothing could be gold that was not yellow; yellow would be of the essence of gold; but only because we had decided to give the name to no metal of another colour; it would be the meaning of the name that fixed the essences, and the essence would be only 'nominal'.

It has been assumed in the above that the attributes included in the definition may be not only arbitrarily selected, but without any perceivable connexion among themselves; so that any attribute omitted from the definition should drop at once into the rank of accident; the essence is only a collection of attributes comprised in the signification of the same name and there are no properties at all. And some logicians have maintained that we can never see any necessary connexion between different attributes; and that when we meak of them as universally connected, we really mean no more than that they have been very frequently found accompanying one another. Without for a moment agreeing with this opinion (which denies any sense in the distinction between a connexion that is necessary and universal, and a conjunction that is accidental) it may be admitted that we often regard attributes as necessarily and universally connected, because we believe that with fuller knowledge we might see into the necessity of the connexion, when as yet we cannot actually do so. This is markedly the case with the various properties of an inorganic substance; and the kinds of plant and animal also present us with many instances where different peculiarities in a species are inferred to be 'correlated', because the same conditions seem to affect them both, without our being able to understand the connexion between them.

The difficulty of determining what attributes are essential to a substance, and therefore of discriminating between essence and property, does not however arise entirely from the seeming disconnexion among the attributes of a kind. It arises also, in the case at least of the organic, from the great variation to which a species is liable in divers individuals. Extreme instances of such variation are sometimes known as border varieties, or border specimens; and these horder varieties give great trouble to naturalists, when they endeavour to arrange all individuals in a number of mutually exclusive species. For a long time the doctrine of the fixity of species, supported as well by the authority of Aristotle and of Genesis. as by the lack of evidence for any other theory, encouraged men to hope that there was a stable character common to all members of a species, and untouched by variation; and the strangest deviations from the type, excluded under the title of monstrosities or sports or unnatural births, were not allowed to disturb the symmetry of theory. Moreover, a working test by which to determine whether individuals were of different species, or only of different varieties within the same species, was furnished, as is well known, by the fertility of offenring: it being assumed that a cross between different species would always be infertile, as in the case of the mule, and that when the cross was uniformly infertile, the species

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were different. But now that the theory of organic evolution has reduced the distinction between varietal and specific difference to one of degree, the task of settling what is the essence of a species becomes theoretically impossible. It is possible to describe a type; but there will be hundreds of characteristics typical of every species. Who is to determine what degree of deviation in how many of these characteristics will make a specimen essentially or specifically different? Will it not have to be decided arbitrarily at the last? so that here again our use of names will settle what is essential to the species. Everything will be essential that we require in a specimen nower to call it by a certain specific name.

Such are the reasons for saving that the essence of anything is settled by the meaning that we give to names, and if the essence is thus arbitrary, the distinction between essence and property is similarly infected. But that distinction is obnoxious to another objection, already noticed on p. 80: that if the property is common and peculiar to the kind, it ought to be included in the essence, because connected with it universally and necessarily. It is as little possible for a triangle not to contain angles equal to two right angles, as not to have three sides; as little possible for a line not to be straight or curved, as not to be the limit of a superficies. If the property of a subject is grounded in the nature of that subject alone, why is it not reparted as a part of its nature? if it is grounded in part in the nature of the subject, in part in the fulfilment of conditions extraneous to the subject, then the subject only possesses it in a certain conjunction, and it ought to be called an accident.1

Having thus presented our difficulties, we must endeavour their solution.

The inexpugnable basis of truth in the theory of the predicable lise first in the distinction between the necessary and the accidental: secondly, in the analysis of definition into genus and differentia. The first underlies all inference; the second, all classification. But the notion of essence, and the distinction between essence and property, are not applicable in the same way to every subject.

They present at first sight no difficulty in geometry. The essence of a figure includes so much as need be stated in order

1 Of supra, p. 86,

to set the figure as it were before us: whatever can be nowed of such a figure universally is a property. Thus the definition is assumed, the properties are demonstrated; and that is the true Aristotelian distinction between essence and property.

But how are the properties demonstrated? Only by assuming a great deal else besides the definition of the figure of which they are demonstrated. We assume for example the postulates and that means that we see that we always can produce a straight line indefinitely in either direction, or join any two points, or rotate a line round one extremity. We assume the axioms: and that means that we see, e. c., that any two right angles must be equal: and that if a straight line AB falling on two other straight lines CD. EF makes the angles CAB. EBA

equal to the angles DAB, FBA, CD and EF must be parallel, and if not, not : and vice verse · we seemme also in one propo-

sition all that we have already proved

in others. It is not from the mere contemplation of a figure as defined, that the perception of its properties follows ; we must set the figure into space-relations with other lines and figures, by an act of construction: and the truth of our conclusion is involved not solely in the essence of the figure as set out in its definition, but in that taken together with the nature of space; for it is really the nature of space which we apprehend when we realize that the sum of the interior angles made by two particular parallel straight lines with a line that cuts them is equal on both sides of it, or that a given straight line can be produced to meet another with which it is not parallel. Another point must be noticed. It was said that whereas the properties are demonstrated, the definitions are assumed; but that does not mean that they are arbitrarily taken for granted. They are assumed, because they are what we start with. But they are not arbitrarily taken for granted, because it is self-evident to us that the existence of a figure as defined is possible; and this is selfevident, because in the process of defining we bring the figure into heing before us. We know that three straight lines are enough to make a figure, because we make it of them in imagination : we know that a figure may have five sides, because we see the pentagon before us. It is this power which geometry possesses of creating instances of the objects of its own study that distinguishes it from the

non-mothematical ecianoss. And it creates its objects by constructing them-i.e. by drawing lines; and in this possesses a natural principle upon which to distinguish between property and essence. For though in geometry properties are commensurate with their anhierte and may be reciprocally demonstrated, yet everything depends upon the power mentally to see the lines : thus the angles of a triangle determine the position of its lines as much as the position of the lines determines its angles; but it is only through dividing space by lines, that the angles can be realized. The visible figure is therefore our necessary starting-point. A definition which fails to determine that waits for application until the figure can be nictured. Let a circle be a figure having a larger area than any other of equal perimeter : that does not set a circle before us : an infinity of figures can, we see, be made by a line that returns upon itself and is flexible at will; and the property specified will not. previously to demonstration afford us any means of selecting the figure intended. But my that a circle is the plane figure generated by the revolution of a straight line about one of its extremities remaining fixed, and then we have it before us: then we understand what it is about which the property of having a larger area than any other figure of equal perimeter is affirmed. Once again, in geometry there are no happenings, no conjunctures. It is true that in order to geometrize we have, actually or in thought. to draw the figures: but our process of drawing only renders visible space-relations which we conceive are eternally present everywhere in space. Therefore the circle or the triangle is not subject to mutation on different occasions; there is nothing to prevent it at one place or time from being the same as at another: and the conditions under which it exists do not vary; the general nature of the space in which it is is uniform and constant. Hence the properties of any geometrical figure, though, as we have seen. we must take the general nature of space into account, as well as the definition of the figure, in order to realize their necessity, may yet without risk of any false deduction be regarded as if they were grounded in the essence of that figure alone. For the general nature of space is a 'constant': it is everywhere the same, and conditions every figure alike; it is not because that ever changes, that different figures have different properties, but because the figures are different.

Geometry therefore deals with subjects canable of definition : in which the definition serves to set the subject before us; and in which the distinction between essence and property, though from one point of view questionable is from another sound. It is questionable, so far as the properties of a figure do ideally belong to it always inst as much as the figure always exists . they are as necessary to it as its definition, and do not really any more depend on the definition than the definition on them. But it is sound so far as the essence is that which we must start with, in order to have the figure before us and my anything about it, while the properties are what we can demonstrate. The process of demonstration may require that we should make a further construction than what the figure itself demands: but this further construction is not necesmary in order that we may see before us the figure itself - and hence the definition, which as it were constructs the figure, gives us what is essential, the demonstration what is necessarily bound up therewith 1

Now the science of geometry, both in Aristotle's day and since. has been ant to seem the model of what a science should be ; and that deservedly, so far as its certainty and self-evidence go. But though we may desire an equal certainty and self-evidence in other sciences, we must not ignore the differences between their subjectmatter and that of geometry; nor must we assume that the distinction of essence and property will have the same applicability to concrete bodies as to figures in space. The subjects which we study in chemistry, in botany, or in zoology, are not constructed by us: they are complex, and for all we know may differ much in their construction in different instances; and they exist under conditions which are not constant (like the nature of space) but infinitely various. Under these circumstances, we cannot expect to find the determination of the essence of a kind, and the senaration between that and its properties, as soluble a task as in geometry.

Let us consider first the definition of inorganic kinds. Here, since a compound may be defined by specifying its composition.

Yet where there are alternative modes of constructing a figure (e.g. an ellipse) it will be arbitrary which of them we select to define it by; we can only say that the definition must enable us to construct the figure.

our problem deals with the elements. It will be instructive to look for a moment at the Greek treatment of this question. There were two main attempts to define the famous four elements of Empedocles, earth, air, fire, and water. Plate supposed that they differed in the geometrical construction of their particles those of earth being cubic of air octohedral, of fire tetrahedral, and of water eicosihedral. If these were their differentiae, what was their cenus? We can only reply, solid.1 They were something filling space, of different figures. In assuming the concrete things which he defined to fill space. Plate did what every one who defines a natural substance does. We do not always mention it in our definition : we might define a spake, for example, as a certain kind of vertebrate: but the notion of a vertebrate involves it: and it is necessary if the definition is to furnish us with the concept of a material object at all. In taking geometrical figures as his differentiae, he attempted to gain in physics the advantages which geometry derives from our power of constructing its objects; but he failed to show how the sensible properties of the different elements were connected with their respective figures. Aristotle preferred the method of those who distinguished the elements not by the figure of their particles, but by the mode in which they combined certain fundamental sensible qualities, heat, cold, moisture, and dryness. Fire he thought was the hot and dry substance, water the cold and moist, earth the cold and dry, air the hot and moist. These definitions have the disadvantage of using terms that possess no very precise signification. How hot is unmixed fire, and how moist is pure water?

Modern science recognizes in each element a whole legion of common and peculiar attributes. Some of these, such as its atomic weight, or its specific gravity, are conceived to be constant or to characterize the element in all conjunctures; others it only exhibits upon occasion; this is the case, for example, with its reactions towards other bodies. We have very little insight into the interconnexion of the various attributes thus characterizing each element; but unless we are to regard everything in nature as accidental, we are bound to believe them interconnected. It is impossible to

Or perhaps, regular solid, On what kind of evidence particular attributes are held to be connected, it is the business of the theory of the inductive sciences to show.

include in its definition all that is known to be characteristic of an element: and for the mere purpose of identification, many of the attributes of an element would serve equally well. But we prefer to select as differentiae and include in the definition such attributes as appear, in some form or another, in all or a large number of elements: because we are thus able to exhibit the divers elements as related to one another upon a scheme, or in other words to classify them. Thus the specific gravity of a substance is more suitable for defining it than some peculiar reaction which it exhibits. although nerhans less useful for identifying it . herause all elements must have some specific gravity, but no other need exhibit the same sort of reaction. If, however, a reaction is common to a number of substances, it may serve as a ground for collecting those into one class like the salts: the common reaction being a generic character; especially when for any reason, such as the number of attributes that are commensurate with it (i.e. are found where it is found, and not where it is absent), such reaction seems to be of importance in the substances to which it belongs.

Such considerations may guide us in choosing what to include . in our definition : and we shall also cateris paribus prefer for differentiae those attributes that are continuously exhibited to those that an element only exhibits in a rare conjuncture. Nevertheless it is plain that our procedure is in great measure arbitrary; and the distinction between essence and property is not applicable as it was in geometry. For among the constant attributes of an element we cannot start with some and demonstrate the remainder; and those which it exhibits in particular circumstances are not properties in the full sense. We may indeed regard it as the property of an element to exhibit a certain reaction in certain circumstances 1: but whereas the 'circumstances' under which geometrical figures exist and possess their properties are in every case the same (being the general nature of space), the circumstances relevant to the manifestation of the several properties of an element are different : hence we cannot afford to omit the statement of them in stating its properties; and since they are often very numerous and complex. and involve many other substances, it may be more natural to refer the property to a compound, than to one element. Nevertheless.

¹ Cf. Ar. Top. ε. i. 1285 16 ἀποδίδοται δε το ίδιαν ή καθ' αυτό και δεί ή πρός έτερον και ποτέ.

since causal connexion is the root-idea of the notion property, we rightly regard these attributes as properties rather than accidents. For although the subjection of an element to any particular conditions rather than others is strictly speaking accidental, since it depends upon historical causes that are independent of the nature of that element, yet its behaviour when subject to those conditions is not accidental: so that it is fairly called a property of gold to be soluble in aqua regia, though very little gold be so dissolved: but an accident to lie in the cellars of the Bank of England, for that belongs not to gold, but only to particular masses of gold, and why those masses should lie there instead of any others cannot be determined essentifically nor by any reasonings and/pring to gold universally.

The use of the singular without the article (as in a proper name) when we say that gold is malleable, or iron rusts, or silver tarnishes, is worth remark. It implies that we think of gold, or silver, or iron as one and the same thing always: that we are looking to the unity of kind, and not the particular specimena. The very idea of an element negates the possibility of any difference between different specimens¹; and when we investigate the properties of a compound, so far as the composition is really known with accuracy, we have the same confidence in attributing to that compound universally the properties discovered in a particular sample. In organic kinds, though we may know the chemical composition of the parts, we cannot know with the same accuracy the composition of the heterogeneous parts into the whole.

Indeed the problem of distinguishing between essence and property in regard to organic kinds may be declared insoluble. If species were fixed: if there were in each a certain nucleus of characters, that must belong to the members of any species either not at all or all in all: if it were only upon condition of exhibiting at least such a receift nucleus of characters that the functions of

¹ This may seem incomisiont with the occurrence of the so-called 'alloringic forms of elements; but as matter of fact, the speculations as to the arrangement of the atoms in a molecule, to which the phenomena of alloretyp have given rate, confirm the remark in the text. It is found allorety have given rate, confirm the remark in the text. It is found to the confirmation of the confirmation of the confirmation indistinguishable in their own nature are capable of divers combinations; it is not the elementary substance, but the combination of atoms of the elementary substance, to which the properties are allottopic forms, though the elementary substance, the man in the allottopic forms, though the elementary rubstance is seed the same in the allottopic forms, though the elementary rubstance.

life could so on in the individual at all: then this nucleus would form the essence of the kind. But such is not the case. The conformity of an individual to the type of a particular species depends on the fulfilment of an infinity of conditions and implies the exhibition of an infinity of correlated peculiarities, structural and functional many of which so far as we can see dike keenness of scent and the property of perspiring through the tonene in does), have no connexion one with another. There may be deviation from the type to a greater or less degree in andless directions: and we cannot fix by any hard and fast rule the amount of deviation consistent with being of the species, nor can we enumerate all the points, of function or structure, that in reality enter into the determination of a thing's kind. Hence for definition such as we have it in permetry, we must substitute classification . and for the demonstration of properties the discovery of laws. A classification attempts to establish types; it selects some particular characteristics as determining the type of any species; these characteristics must be (a) of the same general kind for each type, or, as it was expressed on p. 72, variations upon the same theme, in order to exhibit the mutual relations of agreement and divergence among the various types : (6) important, or, as one might say, pervasive: that is, they must connect themselves in as many ways as possible with the other characters of the species. It will be the description of the type, drawn up on such principles as these. that will serve for definition. It is avowedly a mere extract from all that would need to be said, if we were to define (upon the supposition that we could define) any species of plant or animal completely.

The full nature of an organic species is so complex, and subject to so much variation in different individuals, that even if it could be comprised in a definition, the task of science would hardly consist in demonstrating its properties. To discover the properties it in demonstrating its properties. To discover the properties of binds poor zoology. Science asks rather what it is about any kind on which a particular property belonging to it depends. Herein we break up or analyse the complex character of the kind, in order to determine what we call the lesse of organic life. If a species, for example, is keen-scented, that must depend upont conditions that are but a small part of what would be included in

a complete account of its nature. In order to find the commensurate subject of which a property is predicable, we must abstract from all in the species which is not relevant to that one property: and our subject will not be the concrete kind, but a set of conditions in the shetreet. The property whose conditions we have found is of course the property not of those conditions, but of anything that fulfils those conditions : keen-scentedness, for example, is not a property of a particular construction of the olfactory organ (though we should call it an effect of this), but of an animal in whom the olfactory organ is thus constructed; the laws of organic life suppose of course that there exist organisms in which they are exhibited. We may still speak therefore of properties of kinds : but the demonstration of them considers the nature of the kind only so far forth as it concerns the property in question. The property is not common and peculiar to the kind, if other kinds, as may well be the case, agree with it in those respects on which the property depends; or if it depends on conditions which cannot be fulfilled except in an individual of that kind, but are not fulfilled in every individual thereof.

Such reflections led the schoolmen to distinguish four senses of the term property—

- 1. id grod perfised omsi ed son soli: thus it is a property of the cow to give milk; but other animals do the same; and to give milk is the commensurate property not of a cow but of a mammal; being causally connected with a feature which though present in a cow is present in other species besides.
- id quod perlinet soli sed non omni: thus it is a property of
 man to write poetry, but not universally; for the writing of poetry
 requires powers which no creature but man possesses, but which
 also one may not possess and yet be a man.
- 3. id quod pertinat omni et goli, sed non semper: in this sense it is a property of the male officery to grow a certain kind of feather, much used by ladies in their hats; but only at the pairing season.
- 4. id qued pertinet omsi et soli et semper: in this sense it is a property of a triangle to have its angles equal to two right angles; but it is difficult to find an example of such a property among organic kinds, for a feature so constant and universal would be regarded as part of the essence: unless like the schoolmen we call it a property in this sense to be capable of exhibiting a property

in sense 3; they often gave it as an illustration of property in the third sense that man laughs; and in the fourth sense, that he is capable of laughter; for the capacity is permanent, but the exercise of it consistent

In all these uses of the term property the notion of a necessary or causal connexion is retained; but commensurateness with the subject is not insisted on in all. No doubt a commensurate subject for every predicate is to be found; but only by specifying the precise conditions (in an organism or in whatever it may be) on which the property depends; but the concrete thing is the subject about which we naturally make propositions, naming it after its kind; and kinds being complex may agree together in some points while differing in others with intricate variety; so that when we have distinguished the species to which objects conform, and the attributes which they possess, we cannot divide the latter among the former without overlanding.

Many general and abstract terms, which form the subjects of

propositions, designate neither natural substances, nor mathematical entities. There are names of qualities and states of thines, like softwas or sutrefaction: of psychical states and processes, like pleasure, anger, polition: of the material products of human or animal skill, like pump, umbrella, bridge or nest: of natural features of the earth's surface, like beack or paller: of determinate parts of an organism, like cell or evapathetic serve: of forms of human association, like army, university, democracy, bank. It would be tedious to proceed further with such an enumeration. About all of these terms it is to be observed that the notion of them involves a certain abstraction. Bridge and pump are concrete terms, but they are names given to material objects because they serve a certain purpose, or exhibit a certain structure : and all else in the nature of the object is disregarded, in considering whether it is a bridge, or whether it is a pump. In attempting to define an element on the other hand, or an organic species, we have to wait upon discovery, in order to know the nature that an object must possess as gold, or as a crab; the whole nature of the concrete object forms the subject of our enquiry. It is the abstract character of the terms which we are now considering, or the limited extent of their signification, that renders them more capable of satisfactory definition: they are least definable, where that which



they denote is most complex: thus it is easier to define army than democracy, and rigidity than putrefaction. The more complex any subject, the less is it possible to exhaust its nature in any brief compendium of words, and the greater also are its caracities of various behaviour under varying conditions; all these are part of the notion of it, and no definition will really be worth much to any one who cannot realize how different the thing defined would be in different circumstances. Thus a definition of democracy means most to him whose mind is most fully stored with a knowledge of history and of institutions and of human life . he can realize what government of the people by the people for the people (if that were our definition) really involves. But comparatively little knowledge is needed in order that the definition of a bridge may be fully understood. It will be readily seen, that what has been said of the difficulty of determining either property or essence in regard to natural kinds applies also to such terms as we are now considering in proportion to the complexity of the notion to be defined: the more complex the subject, and the overter the range and variation of the modes in which it manifests itself, according to the conditions under which it exists the more arbitrary becomes our choice of characters to be included in the definition, and the less can properties be commensurate attributes.

We have now reviewed the theory of predicables as it was first propounded; we have seen that the scheme of knowledge which it implies cannot be realized upon all subjects; that it is best exemplified in mathematics, and in other sciences which deal with abstractions. But we have also seen that it contains distinctions of great value and importance. These are

- 1. the antithesis between an accidental connexion (or coincidence) and a necessary or conceptual connexion:
- 2. the conception of the relation of genus and differentia, and of the unity of genus and differentia in a single notion:
- 3. the resting the distinction of essence and property upon the distinction between that which we start with and that which we demonstrate therefrom; though this use of the term property cannot always be adhered to in practice.
 - It remains to say a few words upon the Porphyrian doctrine.

It differs to appearance in one point alone; the Porphyrian list of predicables substitutes Species for Definition. But that difference

implies a change in the point of view. The problem now is not as to the relation between two universals predicated one of another but as to the relation in which the various universals predicated of an individual stand to their subject for it is of individuals only that a species (such as man, or home, or parrot_tulin) is predicated 1 And various inconveniences arise from this change. First and foremost we have to determine what is a true species and what only a cenns within a wider cenns. Do I predicate his species of Cetewayo when I call him a man or when I call him a Zuin? if Zulu he a species man is a genus, though included with the wider cenus of mammal, vertebrate or animal: but if man is the species. Zulu is an accident. The question thus raised is really insoluble: for species, as is now believed, arise gradually out of varieties. It gave rise to many great controversies, as to whether a species were something one and eternal, independent of individuals, or on the other hand no more than a name. These opposite views were indeed older than Pornhyry or the mediseval thinkers who discussed them so earnestly; nor can any philosophy refuse to face the controversy between them. But it was a misfortune that the theory of predicables should have got involved in the controversy: partly because it led to a mode of stating the fundamental issue which is not the hest - partly because the true value of the theory of predicables, as a classification of the relations between universals predicated one of another, was lost sight of in the dust of the dispute between the realists and the nominalists.

A second inconvenience in the Porphyrian theory is that while beginning by distinguishing the relation of its predicates to an individual, it cannot continue true to this standpoint. Species is properly predicated of an individual; we sak what is the species not

¹ There is a suggestion in Aristotle's Topics of this point of view, for he allows that 7800s may mean a peculiarity that distinguishes an individual from others; cf. the passage quoted p. 87, n. 1 supra and s. i. 129* 8-5. But his doctrine as a whole implies that the subject term is general.

his doctrine as a whole implies that the subject term is general.

In technical language, what is an infime species and what is a proper species and what is a proper species and what is a proper species and infime species. The differentibles removed a proper species are infine species. The differentibles removed that the species are infine species. The differentibles removed that the species are infine species are infine species, an infine species to species and the species are infine species; but it is no estate that the species are infine species; being in fact the same problem restated. Looked at from the other side, the species for the species are infine species; being in fact the same problem restated. Looked at from the other side, the species (Looked to prove about 100 per species).

of man, but of Cetewayo; and if the species can be analysed into comus and differentia, it is possible to record these as predicated of the individual belonging to the species. But we cannot distinguish between property and excident so long as the subject whose predicates we wish to refer to these heads is an individual A property is necessary to its subject, and an accident is not; but all the attributes which belong to Category are equally necessary to him as Cetewayo : on what oround then are some to be called properties and others accidents? An accident is an attribute which coincides in an individual with another general character, or universal . its socidental relation lies towards that other universal. and not towards the individual, in which its presence is historically. necessary. A property is an attribute found in an individual. but grounded in certain general characteristics of that individual: and it is proper not to the individual as such, but as having those characteristics, and therefore to everything which has them, or to that kind of thing universally. It is only therefore in reference to a kind of thing as subject that we can ask whether a given predicate is to be ranked as accident or property. If it is asked whether it is a property of Cetewayo to talk, or fight, or be remembered. we must demand, of Cetewayo considered as what? Considered as a man, it is a property of him to talk; considered as an animal perhaps it is a property of him to fight; but considered as a man. or as an animal, it is an accident that he should be remembered. though perhaps a property considered as a barbarian who destroyed a British force. So long as we consider him as Cetewayo, we can only say that all these attributes are predicable of him.

Thirdly, the Porphyrian doctrine gave rise to a division of accidents into separable and inseparable which, if an individual be the subject, is confused, if an universal, self-contradictory. An inseparable

¹ If sometimes translated what λαρρεπε (συμβοίνα) to an individual, yet it is mid to happen, just because it need not belong to him socording to the conception we have so far formed of him; and it is therefore only coincident in him with the characters included in that conception. Cf. supra. 89 n 2

p. 68, p. 2.
1 'llius d'à ludojous h'yerus irepor tripou, orar à papture ought florder, rò irrpor voi irejou ludojou. à piagnero di ought florie coir y haudern à youriern à ouis ir propurer o trespostion, Porpl. log. c. iii, rist. (One thing is sud lo differ peculiarly from another when it differs by an inseparable accident. And an inseparable accident is unch as grupers of the ore, hockoneciness, or the exar of a would. Forphyry indeed says that accident in general budst primary in individual—and of pir oughtforfore de irvé drépuse

accident of an individual is an accident of the species under which he is considered, but inseparable in fact from him. Thus it is an inseparable accident of a man to be born in England, but a separable against to mean long hair; because he can out his hair short but cannot alter his birthplace. Now this notion of an inseparable accident is confused, because the attribute is called an accident in relation to the species as subject, but inseparable in relation to the individual: the whole phrase therefore involves two standpoints at once. And the distinction between sensuable and insensuable socie dents thus understood has really nothing to do with the doctrine of the predicables as a classification of conceptual relations between a subject and its predicates. There are, properly speaking, no accidents of an individual as the complete concrete individual. The Old Pretender might have been born elsewhere than in England. and might have cut his hair shorter : regarding him as the son of James II, each of these things is an accident : but regarding him completely as the man he was, there was reason for each, and neither could have been otherwise without certain historical circumstances being different, though history does not usually concern itself with tonsorial incidents in the lives even of princes. That one thing was alterable while he lived and the other unalterable leaves them equally accidents from one standpoint, and equally little accidents from the other. If however the subject of which a predicate is said to be an inseparable accident be an universal, then

representation delication, the ext and also that they are predicated primarily of individual—white representations are represented by the content) and betrapes \$\tilde{\text{\$k\$}}\$ is the content) and betrapes \$\tilde{k}\$ is the representation to the individual that they are called accidents. For his account of the distinction between separable and inseparable accidents, \$\tilde{c}\$, \$\tilde{c}\$ we employed a content of the individual that they are called accidents. For his account of the distinction between separable and inseparable accidents, \$\tilde{c}\$, \$\tilde{c}\$ we will also also accidents. For his account of the distinction between separable and imparable accidents are \$\tilde{c}\$, \$\tilde{c}\$ which are also accident of \$\tilde{c}\$ and \$\tilde{c}\$ in the subject. It is if such a subject are in a subject in the subject. It is of two limits, separable and into the subject. It is of two limits, separable and in a scident of a crow or an Ethiopian it acrow can be conceived to be white or an Ethiopian to have lost his colour without the destruction of the subject. It has been a regarded integrands accident to a crow or an Ethiopian; a crow can be conceived to be white or an Ethiopian to have lost his colour without the destruction of the subject. That he regarded integrands accident to a crow or an Ethiopian is acrow can be conceived to be white or an Ethiopian to have lost his colour without the destruction of the subject. That he regarded integrands accident to a crown and pict (sc. course, present), being an insense and of individuals as subject is clear from c. vi object has deposite the deposition and of crows severally, being an insense parable accident, and to move of man and honey, being as superable accident, and to move of man and honey, being as superable accidents.

the expression is a contradiction in terms. It is sometimes said that blackness is an inseparable accident of the crow. But if it is an accident at all, then it is a mere coincidence that all crows are black and there is nothing in the fact that a hird is a crow requiring it to be black . it cannot therefore be inconsrable however constant in our experiences the conjunction may have been. Per contra, if it is inseparable, that must be because the nature of a crow as such requires it, and then it cannot be an accident. The so-called insenarable accident of a species is really an attribute which we find to characterize a medies so far as our experience extends, without knowing whether its presence depends on conditions necessary to the existence of the energies, or partly on conditions in the absence of which the species may still exist. That amounts to saving that we do not know whether it is an accident or a property; and so a phrase is adopted which implies that it ie both

It would be well therefore to shandon the division of accidents into separable and inseparable; and it would be well to abandon the Porphyrian list of predicables in favour of the Aristotelian. Rither list raises very difficult questions: but those which have been discussed in this chapter are questions that must be raised. whether we attach little value or much to the use of the terms Genus, Species, Differentia, Property, and Accident. The attempt to think out the connexions between one thing and another is so vital a feature of our thought about the world, that Logic may not ignore the consideration of it. Abstract terms, and general concrete terms, signify not individuals as such, but attributes and individuals of a kind. We do regard attributes as connected with one another, and with the kind of a thing, sometimes necessarily and universally, sometimes through a conjuncture of circumstances in the history of an individual. We need a terminology in which to express these differences. We do form complex conceptions of objects, and of attributes or states, that cannot be analysed into a mere assemblage of simple qualities, but only per genus et differentiam. These are the facts which justify this somewhat difficult part of logical theory.

CHAPTER V

THE RULES OF DEFINITION AND DIVISION. CLASSIFICATION AND DICHOTOMY

In the last chanter the nature of Definition was discussed at some length . but nothing was said of the technical rules in which the requirements of a good definition have been embodied. The process of dividing a genus into species was also mentioned, but neither were the rules given which should be observed in that. It seemed better to defer to a senarate discussion these and one or two cognate. matters. Treated first, they would have been less intelligible. But what has been said about the relation of genus and differentia. shout the practical difficulties that lie in the way of adequately defining many kinds of terms, and the homogeneity which queht to characterize the differentiae of the several species in one genus. should serve to render the present chapter easily intelligible.

The rules of definition are as follows :-

1. A definition must be commensurate with that which is to be defined: i.e. be applicable to everything included in the species defined, and to nothing else.

2. A definition must give the essence of that which is to be defined.

The essence of anything is that in virtue of which it is such a thing. It is in virtue of being a three-sided rectilinear figure that anything is a triangle; in virtue of being an institution for the education of the young, that any place is a school: in virtue of having value in exchange, that anything is wealth. We have seen. however, that in the case of natural kinds, and in some degree of highly complex abstract notions, the essence cannot be comprised in the compass of a definition, or distinguished very sharply from the properties of the subject. In these cases one must be content to do the best he can : remembering-

(a) That the attributes included in the definition should be always such as are the ground of others rather than the consequences. Thus an animal is better defined by the character of its dentition JOHETE

than of its habitual food; since the kind of food that it can eat depends on the formation of its testh, and not vice versa.

- (b) That we must not give only some comparatively isolated attributes of the subject, but also indicate the kind of subject which these attributes quality. This is done by giving its genus 1, and hence out third rule is:
 - 3. A definition must be per genus et differentiam (sive differentias).

The better the definition, the more completely will the differentia he comething that can only be conceived as the modification of the genus: and the less appropriately therefore will it be called a mere attribute of the subject defined. Thus a lintel is a piece of timber forming the top of a doorway; it can hardly be called an attribute of a lintel that it forms the top of a doorway, for that implies that having already the concept of a lintel, I notice this further as a characteristic of it; whereas really, until I have taken this into account, I have no concept of a lintel. On the other hand, if sodium be defined as an element exhibiting line D in the spectrum, the differentia here may fairly be called an attribute. For one may have a pretty definite notion of sodium without knowing that it exhibits this line in the spectrum. The complexity of the subject under definition is in this case such that whatever be taken to serve as differentia can be only a small part of the whole notion; we have in our minds a pretty substantive concept (if the phrase may be allowed) without the differentia; and therefore this appears as a further characteristic, which is really selected because it is discrepatic.

4. A definition must not be in negative where it can be in positive terms.

The propriety of this rule is obvious. A definition should tell us the thing defined is, not what it is not. A scalene triangle, for example, should be defined, not as one containing either a right angle nor an obtuse angle, but as one containing three scute angles. In this case it is true that a very little knowledge of geometry would enable any one to extract from the negative information of the former definition the positive characterization of the latter. But a negative definition is in itself inadequate, and it would in most cases leave us quite uncertain what the subject positively

¹ Cf. Ar. Top. (. v. 142^b 22-29. But properties, according to Aristotle (Ass. Post. S. z.), are defined by specifying the subjects in which they inhere, and the cause of their inherence in their subjects.

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ferred from place to place, we should not necessarily realize that it was property in land. If anger he defined as an impulse not directed to obtaining for angualf a pleasure who is to understand that it is an impulse to repay an imagined hurt? A definition in negative terms is, with one exception, always faulty : its futility depends on the precision of the positive meaning which the negative terms may happen to convey !

The one exception to the faultiness of a definition in negative terms is furnished by concents that are themselves privative or negative. A backelor is an unmarried man and the very meaning of the term is to deny the married state. Injustice said Hobbes is the not keeping of covenant. A stool is a seat for one without a back to it 2 But it must not be assumed that because a term is negative in form it need be negatively defined : intemperance is the excessive indulgence in strong drink

5. A definition must not, directly or indirectly, define the thing by itself.

A thing is defined by itself directly if the term itself or some evnonym of it enters into the definition. The sun might, for example, be thus defined as a star emitting sunlight : or a bishop as a member of the episcopate. Such error is a little gross : but in the indirect form it is not uncommon. It arises with correlative terms, and with counter-alternatives 3, where one is used to define the other. A cause for example, is ill defined as that which produces an effect, or an effect as the product of a cause : for correlatives must be defined together, and it is the relation between them that really needs to be defined: this is the ground of applying both the correlative terms, and in defining this, we define them. The objection to defining a term by help of its counter-alternative is that the latter may with equal right be defined by it. If an odd number is a number one more than an even number, the even is similarly that which is one more than the odd. It sometimes happens, however, that counter-alternatives cannot be really defined

Cf. the discussion of positive and negative terms, supra, c. ii, pp. 28-33.

From Wattis Logic.

Where a subject occurs in two forms and every instance must exhibit either one or other, then these forms may be called counter-alternatives. Thus in number, the counter-alternatives are old and even; in a line, straight and curved; in an animal, male and female; in property, real and personal, &c. Contraries and opposites generally may be wrongly used to define one another in the same way.

at all; if a man does not immediately understand that number is either odd or even, there is no other knowledge to which we can appeal in order to explain to him the nature of the distinction, for it is unique; and in the same way there is no defining the difference between straight and curved. In such cases, to explain one counter-alternative by the other, though not definition, is the best course we can adopt; for their mutual contrast may help a man to apprehend them both, and he may be more familiar with one than with the other.

There are subtler modes of defining a thing indirectly by itself. We may use a term into whose definition that which we profess to be defining enters. Aristotle illustrates this by a definition of the sun, as a star that shines by day; for day is the period during which the sun is shining. J. S. Mill's definition of a cause as the invariable and unconditional antocedent of a phenomenon errs in this particular; for seconditional cannot really be explained without presupposing the conception of cause.

It should be noticed that where the thing defined is designated by a compound word, it may be legitimate to employ in its definition the words that form parts of the compound. Thus a ball-race is the hollow way between the axie and the wheel in which the balls run that are used to take the thrust of one against the other. The term ball, used in this definition, is not of course what had to be defined.

6. A definition should not be expressed in obscure or figurative language.

The use of obscure words where plain and familiar words are available is a fault in definition, because it militates against the object of definition—viz. that one may understand the nature of the thing defined. The use of figurative, or metaphorical, language is a graver fault, because metaphors, where they are intended to do more than merely to embellish speech, may suggest or lead up to a right understanding of a subject, but do not directly express it. Memory, for example, is ill defined as the tablet of the mind; for though knowledge is preserved in memory, so that we can recover the again, and writing is preserved in tablet for future reference, yet the two things are very different, and the actual nature of what we call memory is as little like a tablet as possible.

1 Top. C. iv. 142ª 84.

* Logic. III. v. & 6.

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It must be remembered that language is not necessarily obscure because it is technical. Every science is bound to use 'terms of art' which will be obscure to the laymen, but may express the ideas belonging to that science clearly and precisely. The obscurity forbidden is that which would be acknowledged by those acquainted with the field of study to which the definition belones.

In the process of Definition, we take some species, or other concept, and distinguish in it its genue and differentia. The wealth is that which has value in exchange. There may be things which have value, but not in exchange—the air, for example, which have value in use; these are not wealth, and with them, in defining wealth, we are not concerned; though they belong to the same genus. But we might be interested in distinguishing the different species which all belong to one genus; and the process of distinguishing or breaking up a genus into the species that belong to it is called towards Division.

Logical Division is a process of great importance in science. Things belonging to one genus will be studied together; and toolject of our study will be to discover all the general propositions that can be made about them. But though there may be some statements that will apply to everything contained within the genus, others will only be true of a portion. If we rightly divide the genus into its species, the species will be parts about which we shall find that the largest number of general propositions can be made.

Division is closely allied to Classification; and both to Definition. The difference between Division and Classification seems to be principally this: that when we classify, we start with the particulars of a genus, and throw them into groups, according to their resemblances and differences; when we divide, we start with the genus, and distinguish the species within it by the differentias of which the genus is susceptible. In other words, Division moves downwards from the more general to the more special, Classification upwards from the more special to the more special. This, at least, is the difference which one would intend to indicate if he contrasted the two operations; but in actual practice our thought may move in both directions at once; and the process of dividing a genus is at

^{&#}x27;In Logic, if Division is spoken of without any qualification, Logical Division is meant; though there are other operations of thought, to be mentioned later, to which the name Division is also applied.

the same time one of classifying the things in the genus. If, for example, one were saked to divide the genus score, he might engagest a division into the novel of adventure, of character, and of plot; but he would at the same time run over in thought the novels that he had read, and sak himself if they could be classed satisfactorily under these three heads.

The close connexion between Division or Classification and Definition is obvious. If we divide a genus into spocies, it must be by the help of differentias, which serve to define the species we are forming. If the genus rectifineer figure, for example, be divided according to the number of a figure's sides into those with three, with four, and with more than four sides, we obtain the definitions of triangle, quadrilateral, and polygon. In a classification also, the classes established must be distinguished by characters that will serve to define them.

A division may be carried through several stages, i. e. the species into which a genus is first of all divided may themselves be subdivided into species: and this may be continued until the species reached no longer require subdivision. The species with which a division stops are called infimae species : the genus with which it starts, the summum senus ; and the intermediate species, subaltern seners, i.e. ceners (for they are genera in respect of the species next below them) subordinated to another genus. The proximum ganus of any species is that next above it in the series; and the words superordinate, subordinate, and co-ordinate are used to indicate respectively the relation of any genus to those below it, above it, or standing on the same level with it (i. e. having the same proximum genus). These terms are also used in reference to a classification : for a classification when completed may be regarded as a division and vice versa. The co-ordinate species into which a genus is divided are sometimes called its constituent species 2, as together composing or making up the genus.

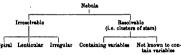
A division, or a classification, may be set out in a scheme, somewhat after the manner of a genealogical tree. The following is an example:—

p. 81, supre.

11 Latin, membra dividentia, as the species are conceived to share the genus amongst them.

¹ Cf. p. 92, n. 2, supra. According to one doctrine, nature has determined where division should stop, and infimae species are fixed by nature. Cf. p. 81, supra.





The following are the rules which should be observed in a logical

1. A distinct must be exhaustive: i.e. there must be a place for everything belonging to the genus in one or other of the constituent species into which it is divided. This rule may also be expressed by saying that the constituent species must be together equal to the 'telem divising'.

The necessity of this rule hardly needs indicating. The object of division is to set out in orderly relation whatever is included within a certain genus; and if the division is not exhaustive, this is not done. Suppose that an income-tax is introduced: it is necessary that the Act imposing it should state what forms of wealth are to be recarded as income, and taxed accordingly. The rent of land and houses is clearly a form of income, and would be included in the division of that genus : but if the owner of a house lives in it instead of letting it, he receives no rent. Nevertheless, he enjoys an income, in the shape of the annual value of the house he lives in, just as truly as if he had let that house, and received for it a sum of money sufficient to hire himself another; and he ought to be taxed if he lives in his own house as much as if he lets it. But if the incometax Act omitted to include among the species of income the annual value of houses occupied by their owners, he would escape payment on that head altogether. Such is the practical importance of making a division exhaustive.

2. The constituent species of the genus must exclude each other.

Unless we secure this, we do not properly divide; for the parts of that which one divides must be separate from each other.

There are two ways in which a breach of this rule may come about. We may co-ordinate with a species another which ought properly to be subordinated to it; as Dr. Johnson is said to have divided the inhabitants of the country north of the Tweed into Scotchmen and Damned Scotchmen; or as the proverb dis.

tinguishes 'fish, flesh, fowl and good red herring'. In these instances the logical error points a sarcsam; but in itself it is comparable to the procedure of the philosopher, who cut two holes in his door, a large one for the cat and a small one for the hitten

The second mode in which this rule is broken is by a crossdivision; the nature of this will be explained in connexion with the rule now following.

3. A division must proceed at every stage, and so far as possible through all its stages 1, upon one principle, or fundamentum divinionis.

The fundamentum divisionis the principle or bests of a division. is that aspect of the genus, in respect of which the species are differentiated.2 Let the genus be soldier: in a soldier we may look to the mode in which he fights, the military rank which he holds or the conditions of service by which he is bound. Procooding upon the first basis, we should divide into artillery, cavalry. infantry, and engineers : perhaps staff and commissariat ought to be added. Proceeding upon the second, we should divide into officer and private officer being again divided into commissioned officer and non-commissioned. Proceeding upon the third, into reculars, vecmenry and militia, volunteers, and reserve. When the division is carried further than one stage, the same fundamentum divisionis should be retained in the later staces which was used in the first. If the division of soldier into artillery, cavalry, infantry, and engineers be prolonged, we might divide artillery into horse-artillery, field-artillery, garrison-artillery, and mountainbattery: cavalry into light and heavy dragoons, lancers, and hussars: infantry into mounted and unmounted. But it would not be proper, after beginning with the mode of fighting as our fundamentum divisionis, to proceed with that of military rank, and divide artillery into officers and privates; for that is a division of soldier generally, and not of artillery any more than of cavalry. infantry, or engineers; so that if it is applied to one of these species, it must equally be applied to the others.

A division which proceeds on more than one fundamentum divisionis at once is called a cross-division; as if one were to divide soldier into artillery, cavalry, privates, and volunteers. It is called a cross-division, because the grouping required by one basis onts across that required by another; in distinguishing privates, for

¹ Cf. infra, p. 116.

² Cf. supra, c. iv. pp. 72, 87.

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example, from other soldiers, we disregard the distinction of cavalry and artillery, taking all members of both those arms who are not officers. A cross-division is worse than useless; for instead of assisting to an orderly arrangement of things in thought, it introduces confusion.

It is plain that in a cross-division, the constituent species will not exclude each other. The only possibility of their being mutually exclusive lies in their being formed upon one basis; for then they are distinguished by the different modes in which they exhibit the same general character. But if different characters A and B are taken, both of them belonging to the genus, everything within the genus will exhibit some mode of both these characters; and the same individuals which are included in a species that is constituted by the particular mode b' in which it exhibits the character A may also be included in a species constituted by the particular mode b' in which it exhibits the character A may have be not offer.

There are two apparent exceptions to be considered here: one to the statement that the employment of two or more fundament districtions at once produces a cross-division, the other to the statement that the members of a cross-division are not mutually exclusive.

The ancient division of matter into the four elements, already alluded to as having been adopted by Aristotle 1, proceeds (or appears to proceed) upon a double basis, of temperature and of humidity. Matter is either hot or cold : matter is either moist or dry ; and hence four species were established, the hot and dry, the hot and moist, the cold and dry, the cold and moist. But there is not really a cross-division here. We do not, while professing to divide upon the basis of temperature, at the same time introduce species founded upon the basis of humidity (as if we were to distinguish the hot, cold, and moist elements); our real basis is neither humidity nor temperature, but the combination of the modes of temperature with the modes of humidity. And such a basis offers a necessarily favourable opportunity for a good division. For given a certain number of characters in a genus, each found in so many different modes, and granted that every member of the genus must exhibit each character in some mode, and no character in more 1 Cf. supra, c. iv. p. 86.

modes than one, then the possible alternative combinations are discoverable with mathematical precision. But it is only where the combination of certain characters happens to be of primary importance, that such a basis of division can be profitably adopted. There would be no advantage in applying the method in such a case as the division of the genus soldiar, where, if we took the three bases of mode of fighting, military rank, and conditions of service together, assuming four alternatives under the first head, three under the second, and four under the third, we should obtain a division into forty-night members. These would be mutually explusive; yet such a result would for most purposes be valualess; for the three bases of division are not such as it is useful to attend to together; though in a particular connection, as, for example, in dawing up a scale of rates of pay, it might be advisable to proceed

In our first exception, a cross-division seemed to be employed when it was not: in the second it might seem not to be employed when it is. It may happen that in respect of the individuals belonging to them, the constituent species into which a genus is divided mon one basis coincide with those into which it is divided upon another. Thus flowering plants may be divided according to their method of fertilization into exogenous and endogenous; and according to the mode of germination in the seed into dicotyledonous and monocotyledonous. It happens that all exogens are dicotyledonous, and all endogena monocotyledonous; so that if the genus were divided into exceens and monocotyledons, there would not in fact be any plant that fell within both members. Nevertheless, the division is logically a cross-division, for there is nothing that we can see to prevent the existence of such a plant, and we can imagine endogens. which are dicotyledonous: and therefore that our constituent species do not overlap must be regarded as our good fortune, whereas it ought to arise out of the necessity of the method on which our division proceeds. And even if we came to understand the connexion between these differences in mode of fertilization and of germination, such a division would still be vicious; for it would not exhibit our species as necessarily excluding each other; and this because (what is more important) it would not exhibit them as alternative developments of a single, or common, notion.

There is a form of division called Dichotomy, which is of neces-

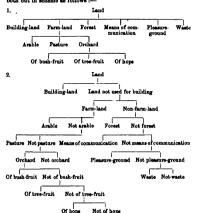
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sity exhaustive, and the species yielded by it of necessity exclude each other; for it divides the genus at every stage into two members (as the name implies), which respectively do and do not possess the same differentia; everything in the genus must therefore belong to one side of the division or the other, and nothing can possibly fall into both. Animal, for example, may be divided into vertebrate and invertebrate, body into animate and inanimate, substance into corporal and incorporeal; each of these divisions is exhaustive, and its members mutually exclusive.

Some logicians have held that in order to secure these advantages all divisions ought to proceed by dichotomy. But the 'truth seems rather, that when a division is undertaken with the view of classifying or arranging all that is contained in the genus, dichotomy should never be used. Its use is in analyzing or defining some one subordinate species. It may, however, sometimes be used to show that a division which is not dichotomous is necessarily exhaustive, and the constituent species exclusive of each other.

The reason why dichotomy is out of place in a classificatory division is that we desire in a division to exhibit our various species as alternative developments of a common notion; at every stage the cenns is further particularized by the differentiae which we introduce in constituting its species; thus the division of the genus soldier. according to mode of fighting, into artillery, infantry, cavalry, and engineers, was carried further by particularizing the way in which the artillery may be constituted for different fighting purnoses, or the cavalry armed, &c. But one side of a dichotomy is always characterized negatively, by the non-possession of the attribute which characterizes the other side; and there is therefore no positive notion which we can develop in the subdivision of this side. The land of a country may be divided, according to the use to which it is put, into building-land, farm-land, forest, means of communication, pleasure-ground, and waste; each of these 'subaltern genera' may be subdivided, farm-land for example into arable, pasture, and orchard : orchard again according as bush-fruit, tree-fruit, or hope are cultivated. But if we were to proceed by dichotomy, we should divide land into building-land and land not used for building: the latter into farm-land and non-farmland : non-farm-land into forest and not forest, and so forth. Now such a division would not only be far more cumbrous than one

unhampered by the method of dichotomy, as may be seen by setting both out in scheme as follows:—



but it fails entirely to exhibit its species as alternative developments of a common notion, or (as it was put in the last chapter) variations on a common theme. To build on it, to farm it, to let it grow timber, &c., are so many ways of using land; to plough, to graze, and to raise fruit from permanent stocks on it are three ways of farming, and therefore of using it; to grow bush-fruit, tree-fruit, and hope on it are three ways of raising fruit on it from permanent stocks, and therefore of farming and therefore of turing it. But

¹ Perhaps orchards (if they may be held to include all ground used for raising fruit from permanent stocks) should be divided according as they

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to farm land is not a way of not building on it: a forest is not a form of not being a farm : roads and railways, which occupy land that is used as a means of communication, are not modes of not being a forest : to mee land as pleasure ground is not a particular way of not making a mad or a milway along it to leave it weste is not a particular way of not using it as pleasure-ground. Neither again is grazing a particular way of not plonghing land nor growing tree-fruit a particular way of not growing bush-fruit on it. A negative concention affords no basis for further subdivision and a division which attempts to classify by dichotomy is for ever subdividing negative concentions.

IThis is the main objection to a classificatory division by dichotomy; which is strangely defended by Jevons, Principles of Science, and ed., c. xxx, pp. 694-698, and Elementary Lessons in Logic. Lesson XII. Other objections, which it seemed unnecessary to add in the main text, since the first is fatal, may nevertheless be pointed out. Such a division does not proceed on a single fundamentum divisionis. In the proper division of land, the basis taken was the use to which land is put, and that was retained throughout : but in the division by dichotomy, the basis taken was first the use of land for building, by which it was divided into building-land and the rest; and the rest was divided on a different basis, viz. the use of land for farming: and so on. Again, the proper division co-ordinates concepts of the same degree of speciality; but the division by dichotomy subordinates them in several stages; so that waste-land is placed level with orchards of bush-fruit. The order in which the subaltern genera are placed (except where a positive concept is divided) is also quite arbitrary; building on it might as reasonably be called a mode in which land is not farmed, as farming a mode in which it is not built on. Lastly, it is claimed for division by dichotomy that it is the only method which secures us from possible oversight of a species; if man be divided into Aryan, Semitic, and Turanian, a race may turn up that is none of these : whereas if it be divided into Arvan and non-Arvan, non-Arvan into Semitic and non-Semitic, and non-Semitic into Turanian and non-Turanian, we have a class ready (non-Turanian) for any new race that may turn up. But it must be observed that to say that a race is non-Turanian does not characterize it; that the Arvan and

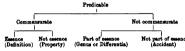
grow bush-fruit, tree-fruit, or bines; and bine-orchards might be subdivided grow bush-fruit, tree-fruit, or bines; and bine-orchards might be subdivided injo hopy-rate and viney-rate. Even then it is not clear where strawberry, gardens would come. Such are the practical difficulties of making a perfect division. In the text something has been surficed to compendiousness, else nursery-grounds, brick-fields, and other varieties of land distinguished seconding to use would need to be included. [Semitic races are also non-Turanian (so that the constituent species are not mutually exclusive), and that if the last objection is considered captions, because the non-Turanian is expressly made a branch of the non-Semitic, and that in turn of the non-Aryan, then it means what is neither Aryan, Semitic, nor Turanian; now if we are uncertain that our division is exhaustive, and wish to reserve a place for things that may fall within none of the species we set up, it is easy to do that without the pains of all this dichotomy; we may divide man into Aryan, Semitic, Turanian, and asysting that is some of these; this last theading expresses what non-Turanian means in the dichotomy, and stands, as it should, upon a level with the rest.

For this reason, a classificatory division should never use dichotomy: the numbers of species into which a summum or subaltern genus is to be divided can be determined not on any general logical grounds, but solely with reference to the nature of the senus in question. Even where as in the case of the four elements the basis of division is the combination of attributes the number of possible species that can be formed by different combinations is determined not by logic but by mathematics. Of course, if a genus falls naturally into two species, it ought to be divided in two: as number is divided into odd and even and line into straight and curved. But this is not mere dichotomy: for it is not the same to divide number into odd and even as to divide it into odd and not odd. The claim made for dichotomy is that its branches exhaust the genus and exclude each other in virtue of the mere form of the division 1; since everything in a genus must either be or not be, and cannot at once be and not be, characterized by any differentia that can be taken. And this is true: and we need realize no more than this, in order to see that number is either odd or not odd : but in order to see that it is either odd or even we need to understand the peculiar nature of number, and not merely the general laws of

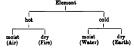
¹ Cf. S. H. Mallons, Introductory Text-book of Logic, c. v., § 10, who points out that although division by dichotomy: has been adopted by the mediaterial and formal logicians became it appears to provide a theory of division which does not make the process depend entirely on the matter of our knowledge, control of the control of t

thought', as they are called, that hold of every subject. The completeness of the division of number into odd or even is not therefore vouched by logic, any more than the completeness of the division of triangle into equilateral isosceles and scalene; nor in the fact that it is twofold does the first possess any guarantee which the second lacks in being threefold. And if a genus is seen to fall into thirteen species instead of three, it should be divided into thirteen; just as triangle should be divided into three and not two. Unfortunately there are few subjects where we can see at once that a genus contains necessarily so many species and no more; and that makes our divisions precarious, but there is no remedy in the new of dishetony.

It may, however, occasionally be possible to show by dichotomy that a division which is not dichotomous is exhaustive or its species mutually exclusive. Aristotle thus supported his list of predicables.



But there is no particular logical interest attaching to this mode of establishing a division; it is in principle the same as where our basis is the combination of certain attributes, and we show the division to be exhaustive by showing that no other combinations remain, as in the case of the four elaments already given.



Dichotomy is really appropriate when we are seeking not to divide a genus but to define a species. There are two contrasting ways in which we may attempt to construct a definition. We may take instances of that which is to be defined, and try to detect what they have in common, which makes them instances of one kind, and on the strength of which we call them by the same name. This is the 'inductive' method. We might thus define 'anch' comparing those of our acquaintance to whom we could apply the name, or those whom Thackersy has drawn for us: and if we thought that among all their differences they agreed in prizing rank or wealth above character, we might accent that as our definition. The other method is that of dichotomy, and in this we try to reach our definition rather by working downwards from a genus, than upwards from examples. Some yenus is taken, to which the subject we wish to define belongs. This genus we divide into what possesses and what does not possess a certain differentia. The differentia taken must be something predicable of the subject to be defined; and if genus and differentia together are already commensurate with that subject, the definition is reached: if they form only a subaltern genus predicable of it, this subaltern genus must be again divided in the same way : until we reach a commensurate notion. At every stage of our division, the differentia taken must if possible he a modification of the differentia next before it : it must at least be canable of combining with those that have preceded it in the construction of one concept in such a way that we are throughout specifying the general notion with which we started 1: and there should be so many steps of division as there are stages which our thought recognizes as important in the specification of this concept. At every stage also we proceed by dichotomy because we are only interested in the line that leads to the subject we are defining: all else contained within the genus we thrust aside together, as what does not exhibit the differentia characterizing that subject. Had we further to consider and subdivide it, we could not be satisfied with characterizing it only negatively; for a negative notion furnishes, as we have seen, no basis for any further specification. But we may disregard, or cut it off : a step to which the technical name abscissio infiniti has been given, i. c. the cutting off of the indeterminate.

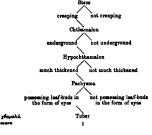
The following example of definition by dichotomy will illustrate what has been said. The term to be defined is tuber; the genus to which it is to be referred is stem.

¹ Cf. infra, pp. 115-116, 118-120.



In this division, we reach as our definition of a tuber 'a stem creeping underground, much thickened, and possessing leaf-buds in the form of eyes.' At every stage by an abscine in spatis we rajected from further consideration a large part of the genus we had so far reached: first all stems not creeping, then all creeping stems not underground, then all underground greeping stems not much thickened, do.; and at every stage we subdivided that part of the genus which we had retained by a differentia that specified further the form to which we had or stage the brought it.

It might have happened, that creeping stems had a name to denote them, say Chihamala 1; and that underground Chthamala had a special name, my Hypochthamala; that these when much thickened had again a different name, my Pachymata; and that theers were pachymants that possessed lest buds in the form of eyes. In this case, the division would be set out in somewhat different form, as follows—



This mode of setting out the definition of envthing implies a classification, in which names have been given to every wider and narrower genus, and the differentia which distinguishes each within its proximum genus has been settled. It may indeed be regarded as an extract from a classification, made for the nurpose of exhibiting the nature of a single species. And this is more or less the character of all definition by dichotomy though the classification may be only in the making in the very process by which we seek for our definition. It is only after considerable study of the parts of flowering plants enabling us to group them by their less superficial characters, that a tuber would be referred to the cenus stem at all instead of root: by that time, the distinction between creening and other stems, between those that creen shove and those that cresp below the ground, would have been already made; so that the method of dichotomy does not so much help us to discover, as to set out and arrange what we know of, the definition of a tuber. There may, however, be cases where the method will guide us in the construction of a definition of that whose nature has not yet been carefully investigated: the genus to which a term is to be referred may be clear, but the appropriate differentiae unconsidered : snob. for example, belongs clearly to the genus man; but even here, the process of finding a differentia, by which to distinguish spobs from other men, is classification in the making. Let us take the prizing of rank or wealth; if that by itself does not constitute a snob, we need some further differentia, to distinguish snobs from other men who prize rank or wealth; say they are distinguished by prizing these beyond character; we then have a definition of a snob, but in getting it, we have taken note of a wider class of men within which they are included

There are three things which Aristotle I says that we must look to, in reaching definitions by the division of a genus. All the terms (the summum genus and the successive differentiae) must be of the essence of the subject defined, they must be placed in their right order, and none must be omitted. These are requirements also of a good classification; but just as a study of the logical form of classification does not enable us to classify any particular order of phenomens, so we are not enabled to define any particular subject, merely

¹ Anal. Post. β. xiii. 974 28 sq.

by familiarizing ourselves with the scheme of a definition of dichotomy.

[A definition of man, displaying the series of subaltern genera to which he may be assigned below the summum genus substance, and the differents by which each subaltern genus is successively distinguished within the genus next above it, was long known in logical textbooks by the name of Arbor Porphyrians. I may be transcribed here. That of taker given above on p. 113 is in the same

The material for the scheme is to be found in Porphyry's Lasgore, iii; where the writer points out that the same differentia which is divisive (hauperusi) of one genus is constitutive (www.rusn) of that immediately below it. The scheme has the advantage of exhibiting the series of differentias by which the definition of the species is reached from the summun genus. Aristotic in Med. Z. iii, discusses how many differentias there really are constitutive of the species; and decides that if each differentia is itself a true differentia of the one before it, then the species has only one differentia, namely the last. For example, if assimate is divided into footed and footless (furforces and favory) and if the footed are divided into before and quadraged, the latter differentia biged is a differentia of footed as such;

Ifor to be a hined is a particular way of having feet. In the species animal hines therefore the correct analysis is into animal and hined and not into footed animal and biped, and though we may proceed through successive stages to biped, there is nothing in the object corresponding to the serial order. If, on the other hand, at any stage we introduce a differentia which is not merely a further specification of that which we have used before (as a c if we were to divide hined into feathered and featherless, or rational and irra-(ional), then we are really introducing a new differentia. In such a case, if we take animal again as the genus, the species man, defined as a featherless or rational biped, would really be constituted by two differentiae. We might endeavour to avoid this conclusion by calling biped the genus and featherless or rational the differentia : but that ignores the fact that biped is obviously not summum genus of man. And if we select a fresh basis of differentiation at more than one stage we are each time adding to the number of differentise that must be recognized in the species. In doing so we ignore the precept, to proceed throughout any division upon one basis; and Aristotle certainly speaks of the introduction of a differentia which is not continuous with that before it as dividing rand τὸ συμβεβηπός and not κατὰ τὸ ὁρθόν. We may notice too, that whereas a differentia which is a continuation of that before it is never applicable to the other member of the preceding genus (e.g. sized is not applicable to footless, the other member along with footed of the genus animal), a differentia which is not of that nature might, for all that we can tell a priori, he applicable to both membern (e. g. feathered and featherless might be applicable to anadruped no less than to biped). The fullness and complexity of natural kinds is, however, such that we cannot always avoid the introduction of fundamentally new differentiae, especially where, as in the classificatory sciences often happens, our differentiae are intended as much to be diagnostic—i. e. features by which a species can be identified—as to declare the essential nature of the species. Cf. pp. 118-120.1

Before distinguishing Logical Division from the other processes to which the name Division is applied, it may be well to emphasize that it deals entirely (like the doctrine of Predicables) with concepts or universals. The geans which we divide is divided into kinds; it itself a universal, the specification of it by various differentiae can only give rise to more determinate universals. The division of it stops therefore with infimae species, and never proceeds to the enumeration of individuals. For if the infima species could be logically divided into individuals, we must apply some fundamentum divisions; and that means, that we should have to distinguish indiv1

viduals according to the different modes in which the common character of the species appeared in them; and to do that would be to distinguish these modes themselves, which are not individual but universal, for many individuals might exhibit the same mode. But individuals of any species are in fact distinguished from each other by the coincidence of innumerable attributes; it is not any attribute singly, but the particular combination of them, that is unique in each instance; and whether or not they are sufficient to constitute 'individuality, unique combinations of innumerable attributes cannot be exhibited in a locival division as differentiate of one smooth.

Three are two processes which have been called division, besides the division of a genus into its species. They are known as physical and metaphysical division. In Physical Division, we distinguish the parts of which an individual thing or aggregate is composed: as in a man head, limbs and trunk: in a knife blade and handle. This process is also called Partition. It is still a process of thought that is meant—not the actual tearing of a flower to pieces, or quartering and beheading of a man; it may be applied to the distinction of the parts composing either a determinate individual, or any individual of a kind: as Orest Britain on the one hand can be divided into England, Scotland, and Walse, a plant on the other into root, stem, leaf, and flower, or a forest into its component trees.

In Metaphysical Division, we distinguish in a kind its genus and differentia, or the various attributes predicable of it, and included in our notion of it; thus we may divide man into animality and rationality, or sugar into the colour, texture, solubility, taste and so forth that characterize any piece of sugar. This is low iously a division that can be earried out in thought alone. In Physical Division, the parts of an individual man or plant may be physically separated; and in Logical Division, when the genus is concrete, individual specimens of the infinae species may be

¹ Thus in the Arber Porphyrione the enumeration of the freez Scornker, Plato, &c., in the infima species some is no part of the logical division. Cf. Porph. Large. ci drays di Arpera vircusire, for if liberipas revierages fearers, or if Showpin and a bril Dave review over de deal private review of the private of the freeze of the private review of the private of the freeze of the private review of the private of the freeze of the private condition of the private

exhibited in different cases in a museum. But in Metaphysical Division, though the colour of sugar may be exhibited without its taste in a thing of another kind—e.g. in a sample of salt—it can seem be achibited by itself.

It should be further observed, for the better distinguishing of these different kinds or senses of division, that in Logical Division the whole which is divided can be predicated of its parts—saised, e.g. of mss, oe, &c.—and indeed unless it is so predicable of all its can be predicated (paronymously, to use the Aristotelian expression 3, or attributively) of the whole—e.g. whiteness, sweetness, &c., can each be predicated of sugar, in saying that sugar is white, is sweet, &c.; in Physical Division, the parts can neither be predicated of the whole or the whole of the part—we cannot either say that a leaf or stem is a plant, or that a plant is a leaf or stem.

[A few words may be added on the relation of Logical Division, and its rules, to Classification. Just as the theory of Definition, with its sharp distinction of essence and property, breaks down smidst the complexity and variety of concrete things, so it is with the theory of Division. Ideally when a genus is divided into species. whether once or through several stages, we ought at each stage to see that just such and so many species are possible in that genus; we do see this in geometry, in the division for example of conic sections into hyperbola, parabola, and ellipse; but in other sciences for the most part we must wait upon experience. Now we do not in experience find that things fall into kinds which fit into any perfect scheme of logical division. Any actual division that can be made therefore of animals, or plants, or forms of government, would exhibit many logical defects; it would be the skeleton of a classification, and every classification involves compromise: the things, which it puts into the same class from one point of view. from another claim to be placed in different classes; all that was said in the last chapter about the difficulty of defining concrete natural kinds might be repeated to show the difficulty of classifying them; and the same reasons which prevent our satisfactorily continuing a division down to a point at which it would find a separate specific concept for every individual prevent our satis-

l'expérieux di Aéyrus seu dest sues bacéforers s'il resieux s'ès unes tradiques pour pour pris, note sui s'il sycapaturis s' apoquentis s' ai oris s'il debjuin de desperie, Cari, il 19. (That is parconymous which receivre its designation from something with a difference is infection, as a grammarian from grammar and a courageous man from courage). The Latin for expérieux s'il demonstration or d'emonstration no d'emonstration no d'emonstration no attribute is demonstration of d'emonstration no attribute is demonstration no attribute is destinations and a superiori desperieux s'emplement des l'emplement de la constraint de la con

[factority classifying them at all. Classification is, as Jevons called it.], a tentative operation; its results are provisional; discovery may reveal new species, and show that characters which have been supposed always to go together may be separated, or those hitherto considered incompatible combined in the same individual; there are limits indeed to this, for there are 'laws of nature' with which all particulars must be consistent; but many of the 'laws of nature' themselves rest on the same evidence on which our classifications are

constructed

Thus the ideal which Logical Division sets before us is very different from anything which Classification achieves. The first is or would be an a priori process: by which is meant that it would fain develop specific from generic concents not indeed prior to any experience of those objects which belong to the various species of the genus divided, but with a perception that the species revealed in experience are such as must necessarily have existed in that genus. Classification is an a posteriori process; it appeals for support to the facts of the order of phenomena which we are classifying, and argues that the facts could only be thus on the assumption of connexions of attributes such as the proposed classes imply; it does not attempt to show that attributes could be connected in individuals of the genus in no other wave than these. Logical Division again is exhaustive, and the constituent species which it establishes are not to overlap: but a classification may have to acknowledge that there are individuals which might with equal right be referred to either of two co-ordinate classes, or seem to fall between them, or outside them all. For these reasons, Division, as treated in a textbook of Logic, is apt to seem unreal and fanciful to any one familiar with the work of scientific classification; its rules seem framed to suit not the world he has to deal with but a fictitious world of the logician's imagination; the consideration of a process which, outside geometry, can scarcely be illustrated by examples except by mutilating facts, is denounced as a barren pastime. And there is justice in the denunciation, when Division, or Definition, is studied without reference to the recalcitrant facts, and on its formal side alone. But if we realize with what great abatements the rules of Definition and Division can be fulfilled in the actual classification of concrete facts. we may yet profitably study these rules, as counsels and not precepts. That is the best classification which conforms to them most closely. The case of the logician may be compared with the case of the geometer. The geometer studies such figures as he conceives, and he believes that his conclusions are true of the squares or triangles that exist eternally in space, bounded by the distances between points therein: but he does not imagine they would apply without qualification to a square table, or a triangular lawn. The figures

¹ Principles of Science, C. EEE, p. 689, 2nd ed.

for these concrete objects are much more complex than a simple square or triangle. So (though the cases are not identical) the square or triangle. So (known the cases are not mentical) the logician studies the problem of classification as it presents itself to thought; but is prepared to expect that concrete things are cross-related to each other in far too complicated a manner for any single and simple scheme of classification to embrace them as they stand. We must consider aspects of them, and attempt to ascertain what various forms some particular property may assume, and under what conditions. In tracing a property through all the phases in which it appears in different instances, we are in a sense pursuing a genus into its species: we are realizing its generic identity under divers forms, and this is part of the business of a logical division. The things themselves which we have to classify, if we take them in their completeness, cannot be cared in a neat logical arrangement: yet even so, the ranking of them in genera and species at all. which is not the work of logic, but the natural bias of our thought (for the distinction of man and animal is older than that of species and conus), implies an effort at such arrangement: the logician does no more than render explicit the aims which underlie all classification : except that the form of his theory takes too little account of the modifications which are imposed by the particular nature of the subject-matter with which we have to deal.]

CHAPTER VI

OF THE INTENSION AND PATENSION OF TERMS

It was observed by Aristotle 1 that in one sense the genus is in the species, in another sense the species is in the genus, 'Animal' is in 'man' in the sense that you cannot be a man without being an animal so that being animal is included in being man. 'Man' is in 'animal' in the sense that among the forms of animal nature man is included

In the technical language of later Logic, this distinction may be expressed by saying that in intension the species includes the genus, in extension is included in it.

The intension of a term verbal is what we intend by it, or what we mean by it when predicated of any subjects: the extension is all that stands subordinated to it as to a genus, the variety of kinds over which the predication of the term may extend.3 If by term we mean the concept, or what is thought of, the extension is the variety of species in which a common character is exhibited the intension the common character exhibited in this variety. The distinction may be more readily apprehended, if it is noticed that we analyse the intension of a term in defining it, and break up its extension in dividing it.

It is clear that as between two terms subordinated one to the other in a classification, the higher, or superordinate, must always have the greater extension; animal, for example, is a term of wider extension than man, and conic section than ellipse; for the concept 'animal' extends or applies to much besides man, and that of

Phys. 5, iii. 210* 17-19. Cf. p. 118, sepro.
? I do not wish to imply that we may not 'intend' the same by a term when it is spicious of a proposition, as when it is predicate. But as in the subject the extension may be more prominent than the intension, while the predicate is always understood primarily in intendent, the expression in the text is less ambiguous than if I mid 'What we mean by it in a proposition.' Cf. 870.0. c. 13.

For another use of, p. 128 sq., infra.

'conic section' to hyperbola and parabola, as well as to allipse.' Many hold also, that the superordinate term, as it is of greater extension, so is of less intension; less being meant by calling anything an animal than by calling it a man; or by the term 'conic section', than by the term 'ellipse'. Hence it has been said that the extension and intension of terms vary inversely; 'when the intent of meaning of a term is increased, the extent is decreased; and vice versa, when the extent is increased, the intent is decreased.' In abort as one is increased, the other is decreased.'

This inverse relation of intension and extension in terms may be the control of t

Still, when we thus qualify a general or an abstract term, we are instituting a sort of classification; we make an Armenian species within the genus Christian, or a class, eay, of bright colours within the genus colour. Therefore we may say generally that it is only terms in a classification, and in one 'esteries of subordination' in it, that the doctrine of the inverse relation of intension and extension applies. It would be ridiculous to compare in this matter such different concepts as descreazy and stems-regise; it is even unmeaning to compare terms belonging to the same classification but to different lines, or 'esterie of subordination', in it; bird and reptice, for example, both belong to a classification of animals, but are not subordinate one to the other, and nobody can well tell which has the greater intension, nor if that were decided would he be able to infer from the decision, which had the greater extension, or comprised the larger number of subordinate species.

¹ Porph. Isag. c. viii ἐτι τὰ μέν γένη πλουσίζει τῷ τῶν ὑπ' αἰτὰ εἰδῶν πυροχῷ, τὰ δὲ εἶδη τῶν γενῶν πλουσίζει ταἰε οἰκείαιε διαφοραῖε. (Further, genera exceed species in the compan of the species under them, species genera in the differentian halpacing to them.)

species in the compass of the species under them, species genera in the differential belonging to them.

"Jerons, Principles of Science, 2nd ed., c. ii. p. 28. Cf. Sir W. Hamilton, Lectures on Logic, viii." 4 xx; Thomson, Loses of Thought, § 28; Bain, Logic, Defluctive, p. 51 ('the greater the one the less the other').

Amplying only to terms subordinated one to enother in a classic figation, the doctrine is an attempt to explain the nature of classifiention as a series of terms so related that each is of wider extension and narrower intension than the next below it.

Now it may be questioned whether this idea is just. The seneric term undoubtedly exceeds the specific in extension, but does it fall short in intension? This question may be put in another form . is the process of classification one of mere abstraction? do I form a generic concept from specific concepts merely by leaving out part of the latter, and attending only to the remainder? If our concents of species and genus were constituted by sets of attributes disconnected but coincident, then this would be the case. The generic concept would be formed by picking out from several sets those attributes or marks, which occur in them all: it would contain fewer marks, or he of less intension, in the same sort of way as one man may have fewer decorations than another. On these principles the nature of a classification might be satisfactorily expressed by the following symbols:-



But we have seen 1 that the genus is not something which can be got by any process of subtraction from the species : it is not the same in all its species, and does not enter unchanged into them all as water into every pipe that leads from a common cistern. You cannot form a concept of it apart from all the species, as a can be read and written apart from other letters with which it may be combined. Attributes that are really independent, such as blue, and sweet, and heavy, can be thus conceived apart; but they cannot stand to each other in the relation of genus and species 2.

If we look at terms which are really in a relation of genus and

¹ Cf. p. 69, supra.

And therefore the introduction of differentiae into a division which are not differentiae of those before them is not and ro opdor, cf. supra, p. 116, though they may still be such of which only the genus from which we started is susceptible.

species, it is not clear that the wider term has the less meaning. Take asimal and man; if I may of anything that it is an animal, I certainly convey less information about it than if I may it is a man; but it does not follow that the concept asimal is of less intension than man. For it must be noted, that I should not say of anything that it is asimal, but as animal; which implies that I am wave of other animals, and that the concept asimal includes alternatives, among which I am at present doubtful how to choose. But if so, the generic concept would seem to exceed the specific in intension; 'animal' means "man, or horse, or or, or ass, or some other form in which the general nature of an animal may manifest itself'. As we become familiar with the infinite variety of animal life, the term comes to mean not less to us, but more.

Or take another illustration. Say that a boy first makes acquaintance with the steam-engine in the form of railway locomotives. For a long time the term means that to him : but by and by he meets in his experience with traction-engines, ship's-engines, and the stationary engines of a factory. His earlier concept of a steam-engine the earlier intension of the term for him-will alter: much which he included at first in it, because he found it in all railway locomotives, he will learn to be unessential-first running on rails, then the familiar shape, then the moving from place to place. And according to the doctrine before us he will leave out from the concept one point after another, and at the end his notion of a steam-engine will be the unexcised residuum. But surely his notion of a steam-engine will have become richer and not poorer in the process; it is not that he finds that a steamengine need not run on rails, so much as that it may run on the roads, nor that its familiar shape is unessential, so much as that it may be built in quite a different manner: nor that it need not move from place to place, so much as that it may work as a stationary engine. It becomes a genus to him, because it becomes a thing of alternative possibilities; and the experience which leads him to extend the term to new kinds of objects leads him to use it with a wider range of meaning. It is true that in becoming generic, the term comes to have a less definite meaning, when applied to any object; but in itself it does not come to have less meaning.

The doctrine of the inverse relation of extension and intension in terms seems therefore wrong; it mirrepresents the nature of a classification. But a doctrine which has been accepted so widely of late!, and seems at first sight so plausible, must have some degree of instification. Its instification or around a seems founding.

- 1. The thought which general terms suggest to the mind is often vacue, and the more so in proportion as they less suggest a definite cancible object. We do not realize all the alternative possibilities involved in animal nature each time that we use the term animal. Hence in the term of wider, as compared with that of narrower, extension there is often little definite; and we are ant to suppose instead that there is a definite little. This error is encouraged by mistaking for thought the imagery that accompanies thinking. The nature of this imagery differs with different people. and any illustration can be only arbitrary. But it might well be that when the notion of man or horse rose in one's mind he pictured to himself the look of either with fair completeness: but that with the notion of animal there went the kind of image which a child would draw of a quadruped—four lines sticking out of an elongated trapezium, with a few more for the head and tail. There is less detail in such an image than in that of a horse or a man: and it is not impossible that one might hence be led to suppose there was less intension in the notion.
- 2. Our actual classifications, as we have seen, fall short of perfection in many respects; we often do not understand the interdependence of the various characteristics of an organic kind, or of the various properties of an elementary substance. In these circumstances, we are compelled at times to fix on certain characters as constituting a genus, and then distribute into species the objects in which they are found by means of attributes whose connexion with these characters we cannot conceive. For example, there is a far-reaching division of flowering plants (already referred to) into monocotyledons and diotyledons, based on the number of the seed-leaves; but in these two classes the sub-classes are distinguished by various characteristics of the calyx and corolla, of the mode in which the stamens are inserted, &c. Now we are ignorant why

¹ There are, however, eminent names on the other side, e.g. Mr. F. H. Bradley, Prof. Bosanquet, and R. L. Nettleship. Cf. capecially section u of the 'Lectures on Logic' in The Philosophical Remains of R. L. Nettleship.

a plant with two seed-leaves should be capable of one series of flower-developments, and a plant with one seed-leaf of another series; the number of seed-leaves is, for all we can see, an irrelevant character; though it cannot really be so; and the concept of dictytledon or monocotytedon is complete, without reference to the character of the flower. Here therefore the intension of the wider term is less than that of the narrower. To the botanist the term Dichlamydese, whose extension is less than that of Dioctytedon, means plants which in the first place have two seedleaves, and over and above that have both cally and corolla; the term Dioctyledon means merely a plant with two seed-leaves. Such access give colour to the doctrie, that where terms are subordinated one to the other, the intension varies inversely with the extension; but they do not embody the true surie for a classification.

3. We have seen that a term may be qualified by an adjective which is really an accident of it. by which is meant that the adjectival concept is an addition to the original concept. rather than a further determination of it as when we qualify the term Christian (which implies a certain religious belief) with the adjective Armenian (which implies a certain nationality)-there being no necessary connexion between creed and race, but any variety of one being capable of coinciding in individuals with any variety of the other. These cases (to which those considered in the last paragraph approximate) bear out the doctrine of inverse relation, so far as they go. But it may be observed that they only bear it out, because they have been as it were constructed to do so. We take a term, and qualify it by an adjective which in the first place is known not to be commensurate with it (and therefore narrows the extension), and in the second place is not implied in it in any way as a possible development of it: so that it is a sheer addition to whatever intension the original term possessed. Then we call attention to the fact that in the original term, and the term composed of it and of an adjective, extension and intension vary inversely. Of course they do, because we have carefully arranged it, by so qualifying the original term that they must. But it is ridiculous to infer from this, that in all terms, where one is of wider extension than the other, its intension is less. Because this holds where the terms are not related as genus and species should be, it must not be concluded to hold where they are so related.

4. It may still be felt that there is more truth in the doctrine than has been conceded. Take the most unimperchable examples of genns and species, such as triangle, with its species equilateral. isospeles and scalene. Can we not and do we not form a notion of triangle which includes those points in which conflateral, isosceles. and scalene agree, but none of those in which they differ? and may not this potion be perfectly precise and definite? and if such be the intension of the genus-term, is it not less than that of the species term? We must admit that this is possible. In the words of R. L. Nattleship 1, 'we may, for convenience' sake, mentally hold apart a certain fraction of the fact . for instance the minimum of meaning which instiffes us in using the word "triangularity" We may call this the generic triangle, and distinguish it from particular forms of triangle. But the true intension of the term is not the 'minimum of meaning' with which we can use it, but its 'full meaning'.

What has been so far said with regard to the relation of intension and extension in terms may perhaps be rendered clearer to some as follows. Wherever we have species of a penus, or distinguishable varieties of a common notion, we may contrast the unity which they present with the variety. To attend to the intension is to attend to the element of unity: to attend to the extension is to attend to the element of variety. Sometimes we are more interested in one, and sometimes in the other. When Socrates in the Meso asks what is virtue, and Meno begins describing the virtue of a man, the virtue of a woman, and so forth. Socrates explains that he wants to know what virtue is as one in all these, and not what the divers virtues are: in later language, he wished for the intension and not the extension of the term. Aristotle remarks 2 that an enumeration of these different virtues and a description of them severally are more valuable than a vague statement of their common nature : i.e. that here at any rate the element of variety was more worth consideration than the element of unity, if either is to be neglected. But if the two are realized together, the unity of the superordinate whole must be seen as the more comprehensive unity, not as the more jejune extract. So far however as we cannot realize them together, and see their

Philosophical Remains, i. p. 220. The italics are mine.
 Plat. Mes. 71 D-72 D; Ar. Pol. a. xiii. 1280= 20-28.

necessary connexion, it will have the character of the jejune extract and be a whole of less meaning, even although we know that the variety of species into which it enters is great; and in these conditions, it may be said to be of less intension.

It follows, that in reference to an influe species, or a notion within whose unity we recognize no conceptual variety, intension and extension are indistinguishable. The equilateral triangle may differ in the length of its sides; and we may if we like regard this difference as constituting a variety in the notion of equilateral triangle. But if we do not—if we conceive the particular length of the sides to constitute no difference in the equilateral triangle—then we recognize no such variety in the unity as makes the distinction of intension and extension possible. The nature of equilateral triangle is not shown in species that are distinguished within that unity, but in that unity itself. The two aspects of the meaning of the term coincide or rather, do not full naret.

But it may be said that even if there are no distinguishable species of equilateral triangle, there are very many distinguishable equilateral triangles. Two interlaced equilateral triangles are a favorrite symbol in the decoration of Christian buildings; and the number of equilateral triangles delineated on the walls and in the windows of churches alone must be past counting. Do not all these and others form the extension of the term, and are not they distinguishable from its intension?

We have treated the extension of the term as 'the variety of kinds over which its predication may extend'; the variety which we conceive within a unity. We have dealt throughout with a relation of general terms or notions; the development of variety within the unity of a conceptual or logical whole has been regarded as stopping with whatever we take as infimas species. The extension of a term is, however, sometimes understood to be not the various conceptually distinct forms which are included within the unity of a single whole (like the various virtues, or species of animal or plant, or kinds of conic section, or sources of income), but various individual instances in which a common nature is realized. According to this view, the extension of man is not Aryan and Semitic, Negro and Berber, &c., paul Socrakes and Plato, Caesar and Pompey, &c.; the extension of triangle is not equilateral, inosceles and scalene, but the triangles on particular church walls and windows or

elsewhere: the extension of colour is not red, blue, and green, but the particular display of colour in every portion of the sky or blade of grass, or fragment of an army jacket. And the contrast of extension and intension is no longer the contrast of variety and unity in a notion or concept, but that between individuals and the common character which makes them individuals of a bind

This view has never prevailed in respect of abstract terms. No doubt qualities have their instances; the whiteness of this page and that of the next are each an instance of whiteness. But it is the function of abstraction to consider the anality in its identity and to ignore the difference between the concrete instances in which it is manifested: let the quality differ qualitatively, as the whiteness of milk does from that of snow, and we may be interested in the difference; but if it differs only numerically, as the whiteness in one patch of snow from the whiteness in the next, we ignore it. We may be separately interested in the various concrete things which exhibit the same quality, but the very purpose and nature of the abstraction which we perform in considering the quality is to treat it as the same in these instances, and to impore their difference. With concrete terms it is otherwise: an attention to the identity of man in Socrates and Plato does not exclude our interest in them as senarate individuals: and it is of concrete terms that individual instances are cometimes taken to constitute the extension.

Now we need not quarrel with this use of the word : but it is important to see that we are introducing a new distinction. The relation of man to animal, or of negro to man, the relation which we recognize between species and genus, is not the same as the relation of Socrates to man or animal, the relation between an individual and its kind or universal. The inverse relation of extension and intension of which we have spoken does not hold, except between notions or universale; if the extension of a term is the individual instances, it is meaningless. The individual instances may be more or fewer, but what is meant by the common term predicated of them all remains the same. We saw how the intension of the term assimal might from one point of view be said to increase, as a man becomes acquainted with fresh forms of animal life; and how from another point of view, because what at first he might have regarded as essential to an animal turns out not to be indispensable, it might be said to diminish, shrinking to a jejune residuum. But whichever

v.1

way we look at it, it is only acquaintance with fresh forms of animals that produces this result; a mere increase in the sumbers of one's acquaintance would produce no such effect. The intension of the term below does not increase and decrease with the flucture. tions of the hirth-rate 1. when eminess were called in the term did not alter its intension. Intension has nothing to do with actual existence. There may never have been a nerfectly just man and vet we mean something by perfect justice. The dodo is extinct, but dods would not have less intension if the hird were as common as the sparrow. As it is, the chaffinch is commoner than the soldfinch. but there is not any consequent difference in intension between the two terms

We may therefore mean as we please, by the extension of a concrete term, either the distinguishable species or the individuals included under it : but we must not treat the relation of extension and intension as the same in both seess. It is two that concepts individuals of one kind are distinguished from one another by their characters : and if we attend sufficiently to these distinctions, then as our acquaintance extends our conception of the variety of which the kind is susceptible enlarges. Unobservant people may be familiar all their lives with earwise, without recognizing the richness of earwig nature as diversely displayed in divers individuals. The least observant of us have the richness of human nature forced to some extent upon our attention. But so far as our growing experience of life leads us to realize more fully the variety of human nature, it is not because the men we meet differ numerically, but because they differ in character from one another. With a kind like man, where the differences of character between different individuals are so closely noted, it might seem that as the individuals are conceptually distinguished, therefore in passing from man to Socrates and Plato we are only carrying on the same process of thought which we had employed in distinguishing within the genus animal the species of man and horse and ox. That is not so. Man is not

Bradley's Logio, p. 158.
 If intension and extension varied inversely, and by extension were meant the various individuals, then the intension of dodo should become infinite when the species became extinct. Perhaps it might be replied that past as well as present individuals are included in the extension; but if there never has been nor can be a body moving freely in space, that term at least should have an infinite intension.

less an universal notion because it is rifere specific than animal; and if we were merely further specifying our conception of man in the case of Scerates, Scorates would be an universal notion too. But Scorates is an individual; and I cannot arrive at individuality by any specification of a general notion. Scerates is distinguished conceptually from Plato; but that is not the whole of the distinction, for they exist in the concerts.

In place of the words Extension and Intension various writers have need others to mark the same distinction and in particular since the publication of J. S. Mill's Logic 1, the words Denotation and Connectation have come into favour for Extension and Intension respectively. Mill claimed for these that they possess an advantage in the existence of the corresponding verbs, to denote and to console, which other expressions do not possess : we may speak of a term denoting or connoting this or that, but we should have to use a periphrasis and say that so and so constituted the intension, or was included in the extension, of a term. Though this is a real advantage, yet in other respects the terms which he selects seem to be ill chosen. Extension succests what we want to convey, the range of species over which the application of a generic term extends: Denotation does not. Moreover, usage allows us equally to say that a species or an individual is denoted by a term : if either is the more natural expression, it is perhaps the latter: and so the very reference to individuals which we wish to avoid is foisted on us. Again, Intension naturally suggests what we intend or mean by a term : Connotation suggests not that, but some subsidiary meaning, a meaning additional to some other. It would, perhaps, be convenient if the term Connotation were dropped, or restored to its original signification (according to which nomes connotations meant an attributive term), and if Denotation were distinguished from Extension as reference to individuals from reference to subordinate species. We could then say that asimal denoted Socrates and Bucephalus, but that mes and Aorse were part of its extension.

Such an emancipation from what seems to be an unhappy phraseology may, however, be too much to hope for. But from a doctrine which Mill used his phraseology to express it is necessary that we should emancipate ourselves. Mill drew a distinction between connectation and confinementation names which he described as being one of the most important distinctions which we shall have occasion to point out, and one of those which go deepest into the nature of language'. There are however, no non-connotative names

The distinction had better be stated in his own words. 'A nonconnotative term is one which signifies a subject only or an attribute only. A connectative term is one which denotes a subject, and implies an attribute. By a subject is here meant anything that nomenes attributes. Thus John, or London, or England, are names which signify a subject only. Whiteness, length, virtue, signify an attribute only. None of these names therefore, are connotative, But white long, pirtuous, are connotative. The word white, denotes all white things, as snow, paper, the foam of the sea, &c., and implies, or in the language of the schoolmen 1, consoler the attribute whiteness. The word white is not predicated of the attribute, but of the subjects, snow, &c. : but when we predicate it of them. we convey the meaning that the attribute whiteness belongs to them. . . All concrete general names are connotative. The word was for example, denotes Peter, Jane, John, and an indefinite number of other individuals, of whom, taken as a class, it is the name. But it is applied to them, because they possess, and to signify that they possess, certain attributes. . . . The word man, therefore, signifies all these attributes, and all subjects which possess these attributes. . . . Even abstract names though the names only of attributes, may in some instances be justly considered as connotative: for attributes themselves may have attributes ascribed to them; and a word which denotes attributes may connote an attribute of those attributes. Of this description, for example, is such a word as fault; equivalent to bad or hurtful quality. This word is a name common to many attributes, and connotes hurtfulness. an attribute of those various attributes.2 . . . Proper names are not connotative: they denote the individuals who are called by

¹ Mill means that in the case of such terms as these, the schoolmen spoke

Mill means that in the case of such terms as these, the soncolmen spote of attributes being connoted; but not that his use of the word common conforms generally with that of the schoolmen: cf. in/ra, pp. 140-142.

Mill instances 'slowness in a horse' as an attribute denoted by the word 'fault'. It is clear that if 'fault' is connotative, 'virtue' should not have been given as an example of a non-connotative name. The italics in this quotation are his.

them; but they do not indicate or imply any attributes as belonging to those individuals.

Thre Mill considers to be connotative-

- (a) general concrete terms:
- (b) attributive terms:
- (c) abstract terms, if they are names of a genus of attributes;
 - (a) proper names :
 - (5) abstract terms, if they are names of a simple or a logically undivided attribute.

Designations, i. a. descriptions of an individual involving connotative terms, he considers connotative; abstract terms which and logically undivided, but not indefinable, like esceity or momentum, he does not specially discuss; they ought to be connotative, if (as he helds) definition unfolds the connotation of a name; they ought to be non-connotative, if (as appears to be the case) they signify an attribute only 's and not an attribute sortied to other attributes; but as he has forgotten his view of definition in this section, we seem justified in following the indications of the context and classing them as non-connotative.

We have to consider, therefore, two classes of names which according to this doctrine have no connotation (or intension): proper names, and abstract terms which are not generic, i. e. not predicated of other abstract terms which would form their extension. We may begin with the latter.

According to Mill, fault is a connotative term, became it denotes slowness in a horse, and other hurtful attributes, while connoting their common stribute of hurtfulness. Fice would be connotative, denoting indolence, intemperance, jealousy, and so forth, and connoting their common character as vices. (It is to be observed that all terms are assumed to decode something, and the question is whether they do or do not connote something as well.) Blowness, on the other hand, is non-connotative, and so is indolence or jealousy; for these merely denote each a single attribute.

It would be very strange, however, if this were true. What I mean by calling Othello's passion a vice forms the connotation of that term; vice is connotative by what it means in regard

¹ i. e. one of which we do not distinguish and name subordinate species.

thereto; but when I call his passion jealousy, though that includes calling it a vice (for vice is part of the notion of jealousy), we are told that the term has no connotation; 'vice' is a connotative term; but 'the vice of readily suspecting the unfaithfulness of those we love' is not.

The fact is that Mill starts from the distinction between conrete individuals, and their common character on the ground of which they are called by the same name; and he takes a name to be connotative, if it has a common meaning distinct from the individuals of which it is predicated. Thus sam is connotative because its meaning is not identical with John or Peter; and saids because its meaning is not identical with John or Peter; and saids by the common term vice, slowness and stupidity by the common term fault; and since we can distinguish the common meaning of the terms fault and vice from the particular attributes of which they are predicable, he treats them as connotative terms; while indolence and jealousy, slowness and stupidity are non-connotative like John and Peter.

Now we shall see that John and Peter are also connotative terms : and therefore that even if indolence and such-like terms were comparable with them, they would not have been shown to be devoid of connotation. But they are not comparable. Indolence and icalousy are not individual attributes; if we are to talk of individual attributes, we must mean the indolence exhibited by a given person at a given time and place; as the icalousy which fired Othello's heart when he strangled Desdemona; and so far as indolence and jealousy can be predicated of these and other indolences and jealousies, we can distinguish the common meaning of the terms from the particular manifestations of that meaning. They will therefore be as connotative as any general concrete term. We have seen, however, that in abstraction we are not considering the particular manifestations of an identical quality; we are looking upon indolence as one thing, not different things every time that it is exhibited. Therefore the distinction between the concrete individuals and their common character, from which Mill starts, is altogether out of place, and a view of connotation based on that cannot apply to abstract terms. We must fall back upon the relation of concepts, which was developed at the **71**]

beginning of this chapter by the help of the words intension and extension. Let us call these respectively connotation and denotation if any one prefers it; but what we shall have to say about connotation and denotation in abstract terms is as follows.

An abstract term has a meaning . it means a certain attribute 1 as an unity. This is its connectation. But we may recognize a diversity within this unity, or forms of this unity concentually distingt-the kinds, e. c., of vice or virtue. If so, these form its denotation. The term may be predicated of any part of its denotation separately, and so far as we distinguish the divers parts from the unity of which they are parts (e. g. indolence from vice as such). it does not denote precisely what it connotes. But when we come down to attributes within the unity of which we distinguish no diversity, the distinction between what a term denotes and what it connotes disappears. Indolence, so far as we recognize no separate energies of indolence, is just one attribute - not one like a concrete individual, but as an universal. The term connotes that attribute : and that is what it denotes or is the name of. It can be predicated. as a name or word of the attribute it means. As a thing (i.e. here. an attribute) it is itself, and not a genus of different things. Suppose we recognized (as indeed we may) degrees of indolence: so far as we thought of them as different when we spoke of indolence, material for the distinction between what the term denotes and what it connotes would be furnished afresh. We might still have no separate names for indolence of divers degrees, but in spite of this the term would have connotation. Are we to say that when we cease to think of these degrees of indolence, it has connotation no longer? What has become of the meaning (for connotation is meaning) which it had before? Clearly it must have meaning. What we have to explain is how it can be predicated of that which is not precisely what it means. This arises through the recognition of a conceptual diversity within a conceptual unity. Where that is not recognized, the problem does not arise; but the term still has meaning, or connotation.

The other class of terms which Mill regards as non-connotative are Proper Names. His view is equally untenable in this case, but

^{&#}x27;I use the word attribute because Mill uses it; but it includes such complex 'attributes' as a political constitution. And what is said in this paragraph is true as wall of concrete terms so long as they are general.

for different reasons; and there is more plansibility in it. For there is an important difference in instructiveness between proper and general concrete names, which ought not to be overlooked, though it ought not to be stated as lying in the non-connotative character of the former.

Mill denies that proper names are connotative, because they tell you nothing about the individual which they denote; whereas general names give you information about it. 'A proper name,' he says, 'is but an unmeaning mark which we connect in our minds with the ides of the object, in order that whenever this mark meets our eyes or occurs to our thoughts, we may think of that individual object'; and he contrasts' connotative' names as 'not mere marks, but more, that is to say, significant marks.' A general name is used of an individual on the ground of some character which the thing is believed to possess; and that forms its connotation, which it possesses independently of its use about this individual: a proper name is given upon no such ground, but merely in order to distinguish the individual its gives to from others.

The premisses here are correct, but they do not justify the conclusion drawn from them. A proper name need be given on the ground of no attribute 1; for we may set uside as irrelevant to the real issue the case which Mill instances of a name like Dartmouth, intended to imply that the town is at the mouth of the Dart, and compounded out of elements whereof one is general; in the case of the river Dart itself, at any rate, no much significance is to be found in the name. On the other hand, general names are used on the ground of some attribute. I should not call London a port, except to indicate that cosma-going ships resorted there. Yet it does not follow that proper names are non-connotative. For the proper name is only unmeaning before it as gives by being given, and becoming a mark, it acquires a meaning. And the general name was equally unmeaning before it was ever given; but being general, it can be given to more things than one, and having acquired a meaning by given to more things than one, and having acquired a meaning by

³ Except, indeed, that of individuality: to be an individual is an attribute of the individual denoted, and Mill should have allowed that this was

Most proper names are selected for a definite reason; a child christened Septimus is generally the seventh child; a mountain may be named after its discoverer, a college after its founder, or a society after some one of whom its members wish to be considered the disciples.

its original imposition, has a meaning in advance of its subsequent

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The account which Mill gives of a proper name is substantially indistinguishable from Hobbes's definition of any name which Mill himself had accented in the first section of the same chanter. According to that a name is 'a word taken at pleasure to serve for a mark which may raise in our mind a thought like to some thought we had before. Heing a word taken at pleasure it can have had originally no meaning 1. else that meaning would have restricted our choice. It acquired a meaning when we marked with it the object which we would have it to signify. And whether we wish to mark with it an individual object, or a kind of object makes so far no difference. All names, whether general or proper, are as Aristotle called them down muarrical sara appliants 2, originally, and before they are assigned to an object, they are depot only. sounds without meaning. In being assigned to an object, or becoming marks, they co ipeo acquire meaning; for an unmeaning mark is not properly a mark at all though I may of course be ignorant of the meaning of it. The broad arrow T which is occasionally seen on gateposts, milestones, &c., is a mark: the traveller would know that it was not a mere flaw in the wood or stone: he might not know what it meant: but he would know that it meant something. By enquiry he might learn that it meant that the spot where it was placed was the precise epot whose height was recorded in that portion of the ordnance survey. Here the mark is general. But the mark by which his nurse recognized Odysseus was equally significant. In its own nature it was a scar, the consequence of a wound, and not (like a brand) intended as a mark. Yet this scar (its precise form and position being taken into account) to those who had observed it in Odysseus became a mark by which to know him. He had been absent twenty years, and was changed otherwise beyond recognition; he was supposed to be dead; but his nurse, seeing the mark, knew the man before her to be him-knew that about the man before her which otherwise she would not have known. How can it be said that it was an unmeaning mark for her? And suppose that instead he had at once told her that he was Odysseus;

¹ The case of derivative names is, of course, different.

2. Articulate sounds having signification by convention.—de Interp. ii. 18s 19.

the name would have given her precisely the same information; how could the name be unmeaning? The doctrine that proper names have no connotation is refuted by every criminal who secures an alies!

Proper names it was admitted are not sesioned (as general names are employed) on account of their meaning. They only acquire their meaning by being assigned to an object. But in being assigned to an object they must acquire connotation. The error which it is important to avoid is that a name can denote without connoting; for that implies that a thing can be, and be distinguished, without any attributes distinguishing it. I may frame the sound Glamby: it is doubtless non-connotative: but neither does it as yet denote anything. So soon as I give it as a name to my house or my horse my dog or my daughter, it will denote that thing, and also connote it for me; for here, as in the case of non-peneric abstract terms, we may say that the term denotes what it connotes. The two kinds of term have important differences. Proper names are given to individuals; and what the individual is we can never know completely. The proper name therefore cannot be defined; and a great deal of its connotation may be said to be left as it were in the dark : the name connotes an individual characterized by all which distinguishes it from others: but we do not know all that. Practically we may say that the connotation is anything which enters into our notion of the individual, and therefore so far as no two men have the same knowledge of Glamby, that name will have partially different connotation for different men. The same remark might be made, however, in some degree about general names. And if Glamby were a mark denoting an individual, but connoting nothing, how should any one whom I told to go to Glamby know whether I sent him to a person or a place?

It is hardly necessary to labour the point further. If the connotation of a name were a fixed and constant meaning, borne by it in every case of its application, and therefore general, it would be fairly said that proper names were non-connotative. For they have no constant meaning, except in reference to the same individual; and so far as they belong to several individuals, they are equivocal. But an equivocal term is not a term without meaning;

' Cf. Prof. Bosanquet, Essentials of Logic, Lect. v. § 6

it is a term with more than one meaning. And whatever has meaning has connotation. The comnotation of a proper name can only be learnt by knowledge, personal or through report, of the individual denoted; such report must of course be made by help of general terms. But the connotation of a general term is in the last resort learnt through personal acquaintance with or report of some object of the kind denoted. Only being general it serves now to convey information about individuals without the need of personal acquaintance.

[A little further examination of the passage quoted on n 132 will show how thoroughly confused Mill's account of the matter is. A connotative name, he save, is one which denotes a subject and implies an attribute: a non-connotative name denotes a subject only or an attribute only. He clearly intends here to distinguish between subjects and attributes; and by a subject he means an individual. 'By a subject is here meant anything which possesses attributes. Thus John, or London, or England are names which signify a subject only.' But whether such a subject of attributes is a have uncharacterized that, and all its predicates are attributes; or whether it is a subject of a certain kind, of which its further predicates in other categories are to be called the attributes. Mill does not say in so many words. The former is, however, implied: for the word man connotes all that makes John a man; and the account of substance in the next chapter bears this out. Yet we are told that fault is a connotative term because it denotes, e.g., slowness in a horse and connotes the hurtfulness of this quality: the names of attributes 'may in some cases be justly considered as connotative . for attributes themselves may have attributes ascribed to them . According to the definition of a connotative term given at the outset, slowness ought to be a subject and not an attribute. if fault is connotative.

Mill has confused the logical relation of subject and predicate, which allows you equally to say that slowness is a fault and London is a city, with the metaphysical relation of substance and attribute, also sometimes called the relation of subject and attribute; as has not any very coherent view of what he means by a subject as

I Yary often the form even of a proper name gives a clue to the nature of nationality or set of the object denoted; and surmane, so fare a they denote the members of one family, are not altogether equivocal. Every one knows too how proper names come to acquire a general meaning; Cosser; is a familiar instance; and we have all heard of a Daniel come to judgement, and that Cognets Howevith of the proper in the come to proper the set of the Cognets of the come of the same of the come of the come of the come of the come of the same of the come of the same of the come [= mbstance. He has consequently also failed to distinguish the relation of genus and species from the relation of general to singular, or migreral to individual. Thus terms like white or tritious are connotative, because their form implies a substance or not) distinct from whiteness or virtue, of which they are to be predicated; colour is connotative, while whiteness into, because that is a genus, and this is an infima species; city is connotative, while London is not, because city is recently on universal, and London is infortular or individual.]

[For the sake of the curious, a few words may be added on the history of the term 'connotative'. In William of Ocean a distinction is found between absolute and connotative terms. Absolute terms have not different primary and secondary significations; 'nomen autem connotativum est illud, quod significat aliquid primario et aliquid secundario. He gives as instances relative names (for father signifies a man, and a certain relation between him and another): names expressing quantity (since there must be something which has the quantity); and certain other words; v. Prantl, Geschickte der Logik, Abs. xix. Anm. 831, vol. iii. p. 864. Johannes Buridanus said that some terms connote nothing beyond what they stand for ('nihil connotantes ultra ea, pro quibus supponunt'): but 'omnis terminus connotans aliud ab eo, pro quo supponit, dicitur appellativus et appellat illud quod connotat per modum adiacentis et, pro que supponit'.1 Thus meus and tuus stand for something which is mine or yours; but they connote or signify further and 'appellant me et te tanquam adiacentes' (id. ib. xx. 111, vol. iv. p. 80). In the same way elsewhere we are told that 'rationale' connotat formam substantialem hominis' (xx. 282, vol. iv. p. 63; cf. Anm. 459, p. 109). Albus and agens are given elsewhere by Occam (ib, xix, 917, vol. iii, p. 886) as examples respectively of connotative and relative terms; and it is explained (ib. Anm. 918) that a connotative or a relative term is one which cannot be defined without reference to one thing primarily and secondarily another; thus the meaning of album is expressed by 'aliquid habens albedinem': and when by any term anything 'connotatur vel consignificatur, pro quo tamen talis terminus supponere non potest, quia de tali non verificatur 2', such a term is connotative or relative. Thus a term was called connotative if it stood for ('supponit pro') one thing. but signified as well ('connotat') something else about it; as Archbishop Whately says (Logic, II. c. v. & 1, ed. 9, p. 122),

i.e. to use J. S. Mill's terms, it denotes 'id pro quo supponit', and connotes 'id quod appellat'. For appellatio cf. Prantl, vol. III. xvii. 59 ('propletas secundum quam signification termini potest dici de aliquo mediante hoc verbo "est"). Cf. also ib. xiz. 875.

^{*} Occam means that, e.g., snow can be referred to as album, but not as

['it' connotes", i.e. "notes along with" the object [or implies], something considered as inherent therein." The Archbindop suggests the term attributive as its equivalent; and though connotative terms were not all of them adjectives, since relative terms also some connote, and so do terms like 'mischin-maker' or 'pedant', which though adjectival in meaning are substantives in form, yet adjectives are the principal class of connotative terms, in the original sense of that word.

conginus sense or tank wou.

Connotation and denotation were thus originally not opposed to each other, and the terms were by no means equivalent (as they have come to be treated as being) to intension and extension. And James Mill, who probably by his remarks upon the word console and some influence is directing his son's attention to it, says that "skite, in the phrase skite horse, denotes two things, the colour, and the horse, but it denotes the colour prisarily, the horse secondarily, by many and the primary, consoler the secondarily the primary engineering the secondarily the prover what the schoolmen called absolute, and opposed to connotative, names, introduced a committed attention into its meaning.

John and man are both absolute names in Occam's sense. Man. no doubt, according to some (though not according to a nominalist like Occam) may stand for either an individual or an universal: for an individual when I say 'this man', for an universal or species when I say that man is mortal. (Occam would have said that in the latter case it stood for all the individuals.) But even when I say 'this man', meaning John, the name man does not denote two things, man and John; for John is a man; and if I abstract from that, John disappears too; I have no notion of John as something with which I can proceed to combine in thought another thing, viz. man. With white it is different : I have a notion of paper. and a notion of whiteness, and whiteness is no necessary part of my notion of paper; and so with any other subject of which whiteness is only an attribute and not the essence. Hence the name white may be said to denote two things, the colour, and that which is so coloured; for these can be conceived each without the other, as John and man cannot. James Mill, who thought that objects were 'clusters of ideas', and that we gave names sometimes to clusters (in which case the names were concrete) and sometimes to a particular idea out of a cluster (in which case they were abstract), could also say that white, when predicated of this paper, denoted two things—the whiteness, and the cluster not including whiteness

[which I call paper. But John only denotes one thing-the cluster of ideas which make John; and mes only one thing, the cluster of ideas common to John and Peter. J. S. Mill however distinenished what is common to John and Peter from John or Peter. and said not indeed that man denoted two things, but that it denoted one and connoted the other. But if he had been saked what John, the subject, was as distinct from man, his attribute, he would either have had to say that he was not something different from man, any more than slowness is something different from a fault, though fault was also held by him to denote one thing and to connote another; or that John was just the uncharacterized substance in which those attributes inkered, the unknown subject : or else that he was what remained of the concrete individual when his humanity had been left out of his nature. None of these answers would be very satisfactory. Again, coloured is connotative. in the original meaning of that word, because it is predicable, say of a horse and to be a horse is something else than to be coloured. in J. S. Mill's usage, because it is predicable of brown, though to be brown is to be coloured. Mill treats as two, when he opposes a term's denotation to its connotation, things like John and man, hown and colour, whereof the latter is simply the universal realized in the former, and the former nothing without the latter: as well as things like horse and colour, which are conceptually two. Originally, only a name that was predicated of something thus conceptually a distinct thing from the attribute implied by predicating it was called connotative: and it is only where there are thus conceptually two things, together indicated by the name, that the word connotative has any appropriateness.

(Cf. also on the history of the word Connotative a note in Minto's Lovic, p. 46.)]

CHAPTER VII

OF THE PROPOSITION OR JUDGEMENT

A GENERAL acquaintance with the nature of the indocement or proposition has been hitherto semmed. It would be impossible for Logic to be written or if written to be understood unless the acts of thought which it investigates were already in a way familiar : for Logic arises by reflection mon the modes in which we already think of things. Now independ is the form in which our thought of things is realized, and it is only in judgement that we form concepts. The varieties of the concept, as they are distinguished in the doctrine of terms, the different relations of one concept to another which form the basis of the distinction of predicables, would be unintelligible. unless it were realized that, in the first instance, concents come before us only as elements in a judgement. They live, as it were, in a medium of continuous judging and thinking; it is by an effort that we isolate them, and considering subject and predicate severally by themselves ask in what relation one stands to the other, whether they are positive or pegative, abstract or concrete, singular or general. and so forth. Without presuming some knowledge of this medium in which they live it would be of as little use to discuss terms, as it would be to discuss the styles of Gothic architecture without presuming some knowledge of the nature of space.

We must now consider more closely what judgement is, and what varieties of judgement there are that concern Logic—i.e. varieties arising in the manner of our judging about any subject, not in the matter which we indee of.

A general definition of judgement raises many metaphysical problems, which cannot be fully discussed in such a work as this. But a few things may be pointed out about it.

² This antithesis must not be pressed too far, as was pointed out above, c. i, pp. 5-7. To regard it as absolute, as if what we judged of made no difference to the manner of judging, is the error of those who attempt to treat Logic as a 'purely formal' science. But I do not think that, with this caution, the statement in the text need misled.

Every judgement makes an assertion, which must be either true or false. This carecity of truth or falsehood is the nemliar distinction of indocument, expressed grammatically by the indicative mood Imperatives, optatives, exclamations, and interrogations are not indeements as they stand though they imply the power of indeing. 'I say unto this man "Come" and he cometh.' Here the indicative sentence 'I my unto this man "Come" may be true or false, the indicative contence 'He cometh' may be true or false and both these are indocements : but we cannot ask of the imperative 'Come' is it false or true ?-it is not a indosment. Again the question 'Art. thou he that troubleth Israel?' is not a judgement; it is not itself true or false, but enquires whether the indocument implied is true or false. An optative as in the line 'Mine he a cot beside the rill' is not as it stands a judgement: it could hardly be met with the rejoinder 'That's true', or 'That's a lie'; if it were, and we were to ask 'What is true?' or 'What is a lie?' the answer would be 'That you really wish to live in a cot beside the rill': so that. although an assertion is implied about the wishes of the person speaking, it is not so expressed in the optative. Exclamations may in like manner imply an assertion which they do not express, as when we say 'Strange!' or 'Incredible!' They may also be mere modes of expressing feeling, like an action and gesture; and in such cases, though something doubtless 'passes in the mind', the exclamation can hardly be regarded as an attempt at asserting 1 anything. It is not however, necessary to go into any subtleties: the same grammatical form may indicate different acts of mind, and the same act of mind be indicated by different grammatical forms; 'Let the king live for ever' may be called imperative or optative: 'Angels and ministers of grace defend us,' imperative, optative, or exclamatory: 'I would that I were dead,' optative or indicative. It is enough for us to realize that a judgement being an assertion. capable of truth and falsehood, the full and proper expression of it is in the indicative mood.

A judgement makes one assertion; an assertion is one, when there is one thing said of one thing—by saif Judge. i.e. when the subject is

¹ The reasoning which would make all exclamations imply a judgement was extended to actions by Wollaston, when in his Beligion of Nature Delineared he regarded all wrongdoing as a particular mode of telling a lie.

one, and the predicate one; though the subject and predicate may be complex to any degree. Thus it is one judgement that 'The last rose of summer is over and field'; but two that 'Jaok and Jill are male and female'; for the latter is equivalent to 'Jack is male and Jill is female'; one thing is asserted of Jack and another of Jill: there is one grammatical sentence, but two judgements.

Subject and predicate are terms which have already been explained, as that about which something is seserted, and that which is seserted about it. A judgement is often said to be composed of three parts, subject, predicate, and copula; the copula being the verb substantive, is, iterfu, est, ist, sometimes, though mischierously, represented in Logic books by the mathematical sign of equation, =. We may consider at this point the nature and function of the copula, and the monriets of thus recloning it as a third member of a judgement.

Common speech does not always employ the copula. Take the line 'It comes, it comes : oh, rest is sweet'. Here in the judgement 'Rest is sweet', we have subject (rest), predicate (excet) and copula all severally present: whereas in the indocment 'It comes', we have the subject (if referring to the omnibus), and for copula and predicate together the one word, comes. But that word contains what is said about the omnibus (for it is said to be coming as rest is said to be sweet) : and it also contains in the inflexion, a sign that this is said about a subject : and the judgement may, if we like, be put in a form that exhibits predicate and copula separately, viz. 'it is coming'. It is true that such a change of verbal expression may sometimes change the sense : it is not the same to say 'he plays the violin', and to say 'be is playing the violin'; we must use a periphrasis, and say, 'he is one who plays the violin', or 'he is a violinist'. But it is clear that the copula is present as much in the proposition 'he plays the violin' as in the proposition 'he is a violinist'; just as it is present alike in thought, whether I say Beati immaculati in via or Beati sunt immaculati in via. The inflexion of the predicate verb or the inflexion of the predicate adjective together with the form and balance of the sentence, replaces or renders superfluous the more precise exhibition of the copula; it is however always understood. and if we set down the subject and predicate in symbols whose meaning is helped out by no inflexion, we naturally express it. We symbolize the judgement generally by the form 'A is B'; we may

1 C. S. Calverley, Lines on the St. John's Wood Omnibus.

write it 'A B', but that is an abbreviation; to write it 'A = B' is an error

If the copula is thus present, openly or surreptitiously, in every judgement, what is its function, and can it be regarded as one three parts composing a judgement? Its function is to express that the subject and predicate are brought into the unity of a judgement: that the predicate is asserted of the subject, and that the subject is qualified by the predicate. I may think of property and I may think of robbery, but they may remain apart in my thought—subjects successively contemplated, like breakfast and a morning's work; if I say that 'property is robbery', I show that they are not unconnected concepts, to my thinking, but that one onslifes the other.

Is the copula then a third member in the judgement, distinct from subject and predicate? Strictly speaking, no. For two terms are not subject and predicate, except in the judgement; and the act of judging, whereby they become subject and predicate, is already taken into scount in calling them subject and predicate; it ought not therefore to be reckoned over again in the copula. In the verbal expression of judgement, which we call a proposition, the copula may fairly be called a third and distinct member; but the whole proposition 'A is B' expresses a single act, in which though we may distinguish subject and predicate from the predicating, we cannot distinguish them from it as we can from one another. In our thought, the copula is the synthesis (or linking) of judgement: it is the form of the act, as distinguished from subject and predicate, which are the matter. In our language, the copula is a word used to express the performance of that act.

Is it of any consequence how that act is expressed—(1) whether by an inflexion or by an independent word; (2) if the latter, whether by the verb substantive or some different word or sign (such as the mathematical sign of equality)?

(1) Every judgement is analysable into subject and predicate, though in the act of judgement we recognize their unity, yet they are also distinguished; and the predicate may in its turn become a subject of thought. The separation of the sign of predication from the predicate (as in the proposition 'He is a violinit', compared with 'He plays the violin') frees the predicate, as it were, from its immersion in the present indement. If therefore we wish to set

out a indocement in a form that shows clearly what is the enhicet and what the predicate each separately considered an independent word is better as a gion of predication than an inflation. For the purposes of a logical example, we should prefer to express a indeement in a form that shows this; but it would be nedentry to do it where owing to the idiom of the language it perverts the sense. and we do not need to do it at all when we have no such need to extricate the predicate.

(2) Different languages agree to use the verb substantive or verb of existence as the sign of predication. Home sum I am a man : Cocito, ereo sees. I think, therefore I am. 1 The use of the verb of existence as copula supposts that every indepenent predicates existence, that if I may that 'government is a science'. I declare not only that it is a science but that it is or exists : on the other hand. the content of many indocuments seems to negative this idea: if I my that 'a griffin is a fabulous monster', or that 'Queen Anne is dead'. I do not assert that a griffin or that Queen Anne exists. Hence some have holdly said that the work 'to be' is a more equivoral term employed cometimes to signify existence, and cometimes to signify predication, with no more identity of meaning in these two uses, then there is between set = 'is' and set = 'esta'. From this it would follow that there is no special appropriateness in using the verb to be as sign of predication, rather than any other eion.

Yet if there were no special appropriateness in the verb to be, as the sign of predication, it is strange that so many languages should have agreed to use it. The case seems to be thus: that every judgement does imply existence, but not necessarily the existence of the subject of the sentence. The distinguishing characteristic of a judgement is, as we have seen, that it is true or false. With the false we need not here concern ourselves; for the man who makes a judgement, unless he mays what he does not really think, says what he thinks to be true, and therefore intends to declare the truth. All judgements therefore, besides affirming or denying a predicate of a subject, affirm themselves as true. But a judgement which

¹ Propositions in which the verb of existence was predicate used to be called propositions secundi adiscensis; and those which had some other predicate, where the verb to be was present or implied as oppuls only, were called propositions tertii adiacentia.

C.Y. J. B. Mill. Logic, I. iv. 1.

affirms itself as true claims to express, so far as it goes, the nature of things, the facts, or the reality of the universe. In doing this it may be said to imply existence, not of its grammatical subject, but of the whole matter of fact asserted in it.

When I say that a griffin is a fabulous monster, I do not affirm that oriffing exist like pips and cows. But my independent implies the existence of a mass of fable, in which criffins have their place as fables too. If there were no fables, I could not say that griffing were fabulous: but fables are an element in reality-i.a. in the totality of what is real-no less than pigs and cows. Again, when I say that Queen Anne is dead, I do not affirm the present existence of Queen Anne: I do affirm her existence in the past: and the copula therefore still has the meaning of existence. It may be asked why it should be in the present tense, when the existence meant is past. The answer is first, that the predicate corrects this so far as is necessary : but secondly, that the past (like fable) has a kind of existence. If I am the same to-day as I was vesterday. then I do somehow unite in me at once the present and the past; the past has ceased to be present, but it still somehow belongs to me. What is true of me is true of others, and of reality as a whole. Its history is in time: but it is one through that history; and the past belongs to it now, as well as the present. Queen Anne does not exist now : but that exists now in whose past the life and death of Queen Anne have their place. They belong to the whole system of things which we call the universe; therein they exist, and only in belonging to it can they or anything else exist. The moon. if it had no place there, would not be : neither would justice, nor the triangle: though these different things play different parts in the whole 1

Every judgement then that I make claims to declare some portion of the whole truth that is to be known about the universe: in what form (so far as its purview goes) the universe exists. Hence it is no

^{&#}x27;Some writers have used the notion of a 'universe of discourse' to express
the foregoing contention. In the whole universe fact and fishle, savages
and Roussean's conception of surges slike have their place; but it can make
statements which are true about Rousseau's conception which would relate about surgess themselves. It is said that these are different 'universes'
of discourse; and that propositions which do not sessert the existence of
arything in the material universe may search it in some other. 'The royal
dragon of Chins has feed slaws'—I do not affirm its existence in the universe
of soology, but in that of Chines here benditic design. Cf. p. 28, a. 1, a. spru.

socident that the verb of existence is employed to express the set of judgement. I may entertain a concept, say that of Public Schools; I may think of them as tending to stifle originality in boys, but without deciding in my mind whether they do so or not; so far, the complex concept of public schools as tending to stifle originality in boys floats as it were before my mind, but it is not declared to express the facts; if I judge, no eway or the other, that public schools do or do not tend to stifle originality in boys, then I believe that my notion of them expresses them as they are—that it is no mere notion of mine, but the character of the real school-world; and to express that a combination of which I think is real and true, I use the verb to be. Public schools are liable (or not liable) to stifle originality in boys, because the liability (or non-liability) of public schools to do so is, or exists.

IIt will be observed that in the last paragraph the copula was said to imply, not to predicate, existence. For existence by itself is not a significant predicate, as we have already seen, and therefore cannot strictly speaking be predicated. We may ask, for example. whether griffins exist, as we may ask whether ostriches fly; but whereas in the latter case the subject is assumed to exist, and the question is whether it possesses a certain predicate, in the former case we do not assume that there are griffins, and enquire whether they possess the predicate of existence. Their existence would consist in being griffins, and not merely in being; and to ask whether griffing exist is to ask whether anything existing has the character intended by the term griffin. The existent is thus assumed as the subject of our indepenent, and the judgement claims to declare its nature; we do not assume its nature as a subject of which to predicate existence. Hence it has been said that reality is the ultimate subject of every judgement. A judgement as a whole always has a content—the concept of the subject as qualified by the predicate and this content is believed not to be a mere idea entertained by the person judging, but to be true, i.e. to be the nature of the real; and all true judgements are true together, because reality is manifold, and each judgement seizes some portion of its nature. To ask, Can I make such and such a judgement? is to ask whether reality is correctly apprehended (in part) in the concept of such a subject so qualified. To make the judgement is to apprehend reality in that way, to affirm of it the content of the indepenent; and it is because of this reference to reality involved in every judgement, that we use in expressing a judgement the verb to be.

This view that reality is the ultimate subject of every judge-

[ment must not, however, he understood to mean that it is the torical subject, or be taken as destroying the force of the logical distinction between subject and predicate. We may distincuish in fact three subjects, the logical, the grammatical, and the ultimate or metaphysical. That the logical subject is not the same as the grammatical subject of the sentence is readily apprehended. The proposition ' Belladonna dilates the pupil' may be an answer either to the question 'What dilates the pupil?' or 'What do you know of belladonna?' In either case the grammatical subject is belladonna : but the logical subject is in the former case 'dilating the pupil': that is what we are thinking about, and shout that the judgement informs us that belladonna will effect it; in the latter case, the logical subject is belladonna, and about that the judgement informs us that it produces this effect. This distinction of logical subject and predicate is always present in thought when we judge, though sometimes the logical subject may be very vacue. as when we say 'it rains' or 'it is hot'. But subject and predicate together may qualify something further. This is easily seen when the subject is an abstract term. 'Jealousy is a violent emotion': ealousy may be the logical subject here, but it only exists in those who are icalous. It is not then the ultimate subject, for it can in turn be predicated of something else. Some have thought (and this seems to have been Aristotle's opinion) that there was no single metaphysical subject, but as many as there are concrete individuals. And in the Categories he defines the concrete individual as that which can neither be predicated of nor inhere in anything further.3

But the doctrine which makes Reality the ultimate subject of every judgement holds that in a sense the metaphysical subject is always one and the same : i.e. that there can be only one real system, to which all judgements refer, and which they all contribute to determine and qualify. That a particular thing should exist or be real means that it has its place in this system; and what is called the existential judgement—the judgement whose predicate

¹ ii. 15 8-9. v. 20 11-14.

iii 1 8-9, v. 2-11-4.
It is true that a singular term may appear as predicate of a judgement, as, for example, if we say 'The greatest epic poet is Homer' or 'The first man was Adam.' But in rote a case Aristoile regards the predicate as only accidentally predicate, or zerd confidence of Met. A. vij: by which he means that the concrete individual does not really qualify or being to what figures as its subject, but that because these two ones together, or because it befulls Homer to be the greatest epic poet, and Adam to have been the first man, therefore you can say that one is the other, as you can seen the first man, therefore you can may thus one is the variety of order in one individual, though 'musician' is not what 'being a grammarian' is, any more than Homer is what being the greatest epic poet is, or Adam what being the first man is. In fact, when we enunciate such judgements as these, we cannot help at the same time thinking of the predicate as qualified by what figures as subject.

Lie the week to be in the sense of to exist—as in 'Sunt on non habeant, est qui non curat habere', or 'Before Abraham was, I am '-declares a part of the one system of reality. The content of an existential judgement cannot indeed be predicated of reality as a quality or attribute. When I say that jealousy is a violent emotion. I think of it as an attribute of lealous men: when I say 'Est oui non curat habere'. I do not think of Horace as an attribute of reality. Nevertheless his existence is bound up with the existence of the whole universe; the universe of reality is found (when we think the matter out) to be presupposed by the existential judgement as much as by any other: and though in it existence appears to be first affirmed in the predicate, and therefore not assumed in the subject, yet this cannot represent the true course of our thought. We could make no independent at all, if we did not presume a reality about which it was made. Even the negative existential-' Joseph is not, and Simeon is not '-implies this: for not to be means to have no place in that which is

We are indeed accustomed to think of things and persons as if each were complete and independently real; and in that case the metaphysical subject of any judgement would be some concrete individual or other. The doctrine we are considering carries the question further, and holds that what is predicated of the concrete individual is not true of him in complete isolation from all else, and therefore that he is not, metaphysically speaking, or in the last resort, the subject of which it is true. There is no desire to deny to individuals a relative independence, or to pretend that the relation of attributes or universals to the concrete individual is the same relation as that of an individual to the system of reality which includes him. The judgement 'Jealousy is a violent emotion can be so restated as to make the concrete subject man the logical subject of the independent : I may express it, for example, by saving that jealous men are violent in their jealousy. I cannot so restate the existential judgement, or any other in which the logical subject is already a concrete term, as to make Reality the logical subject instead. But it is the metaphysical subject in the sense that it is presupposed and referred to even in those judgements. We cannot maintain the view that the metaphysical subject of every judgement is always in the last resort a particular individual. 'Civilization is progressive.' Doubtless civilization is only seen in the lives of men; but it is seen in the lives not of this and that man singly but of the community to which they belong. We have to think of men as forming a system and an unity, if we are to give meaning to a judgement like this. What is contended is. that all judgements involve us in the thought of one all-embracing system of reality, whose nature and constitution none can express [completely, though each true judgement declares a part of it. Logic, as has been said before, cannot be rigidly separated from metaphysics; indeed, it derives its chief importance from its connexion therewith. If it had merely to work out the scheme of syllogistic inference, and such-like matters, the problem which the present note has raised would be superfluous; but it investigates how we think; and whether we must think of the universe as a sum of independent reals or as a system is a fundamental mobilem.¹³

In the act of indocement the subject with which we start is modified or enlarged by the predicate, and in that form declared to he real. We end with the subject with which we becan, differently conceived. A synthesis, and the affirmation of the result for real. are common features of every judgement, and the copula expresses them always, and so far has always the same meaning. Whatever sion he seed, whether an inflexion, or the verb substantive, or the mathematical symbol for equality, or anything else, this synthesis. and the affirmation of the result for real, must be meant. The verb to be naturally lends itself to this meaning. The mathematical symbol of equality has a different meaning; it is not a sign of predication, but an incomplete predicate; it implies of one thing. quantitative identity with some other. If I say A = B, the predicate is not B but 'equal to B': the special force of the sign '=' is 'equal to': I must still perform in thought the act of predication, whether I say A is equal to B, or A is the first letter of the alphabet : and if = were adopted as the sign of predication, the equation A = B(which means A is equal to B) must be written A = B.

A judgement then contains subject and predicate; subject

¹ The view that Reality is the ultimate metaphysical subject of judgement is of course familiar to all readers of Mr. F. H. Bradley's or Professor Beanquet's logical work.
* i.e. the logical subject.

Signart has pointed out that the movement of thought in a judgement is different for a speaker comminisating information and for his hearer. The speaker knows the whole fact, when he starts putting forward one aspect of it in enucleating the subject, and supplements it with the other by adding the predicate if I say. This book took a long time to write; the whole fact is present to my mind in its entity before? begin passing. To plementation: to him the predicate comes as new information, which he has now to combine with the concept of the subject hitherto formed by him. The judgement is for him an act of synthesis first, and in retrospect, when he has completed; to, analysis; to the speaker it is an act of analysis first, and in retrospect, when he has completed it, a surplies it is an act of analysis first, and in retrospect, when he has completed it, a surplies the surplies in the speaker it is an act of analysis first, and in retrospect, when he has completed it, a surplies it is an act of analysis first, and in retrospect, when he has completed it, a surplies it is an act of analysis first, and in retrospect, when he has completed it, a surplies it is an act of analysis first, and in which fact from which he stated. v. Zeys, § 8.

and predicate in their combination are declared true of the real. To the words which signify the subject and the predicate separately is added a word which signifies that they are combined as subject and predicate one of the other in a judgement. This word is called the copula; it may be omitted in speech or writing, or be replaced by an inflexion: but the act of thought which it indicates cannot be omitted, if there is to be a judgement. This act. however is not a part of the independent in the same way that subject and predicate are. It is the act or form of judging, and they are the matter indeed. Hence it is at least generically, the same, while subject and predicate change; and for this reason the scheme of a judgement 'A is B' represents subject and predicate by symbols, but retains the 'copula' itself. We write A and B for subject and predicate 1, because they represent indifferently any subject and predicate, being themselves none; we write 'is', and not another symbol in its place, because whatever be the subject and predicate, the act of judgement is, generically, the same.

every indocement. it is the same in so far as it involves a synthesis of subject and predicate and affirms the result of that synthesis for real. It may differ in the nature of the synthesis of subject and predicate. If therefore we speak of judgement as a common form realized, for every difference in the subject and predicate, in different matter, we must admit that there are also differences in the common form. This was pointed out in the first chapter, as precluding what is called a nurely formal treatment of Logic. We cannot study the form of thought with no reference to its content, because on the nature of the content depends in part the form. Having got some notion of the form of judgement, so far as it is always one and the same, we must now proceed to consider some of the variations of which it is susceptible, so far as these belong to its form, and not merely to the content. Differences that belong merely to the content (as between the judgements 'men are animals' and 'roses are plants') we can of course ignore.

The act of indocement is however, only accordable the same in

Of course any other indifferent symbols will serve, such as X and Y or S and P.

CHAPTER VIII

OF THE VARIOUS FORMS OF THE JUDGEMENT

JUDGEMENTS have for long been commonly distinguished according to Quantity, Quality, Relation, and Modality.

In respect of quantity, judgements are said to be either singular, or universal, or particular. But the differences at the bottom of this distinction are not in reality purely quantitative, though they have sometimes been represented as being so.

The subject of a judgement may be either a singular term like 'Scorates' or 'Cassas' or 'the present Cabinet', or a common term like 'man' or 'triangle'. In the former case, the judgement is also called singular. In the latter, the judgement may affirm or dany the predicate of the subject either universally, i. in every case, e.g. 'All equilateral triangles are equiangular', 'Nemo omnibus boris sapit': in which case it is called universal; or partially i.e. in particular cases, or of a part of the subject, only, e.g. 'Some larkspurs are perennial', 'Some animals cannot swim': in which case it is called particular.

By a part of the subject is meant here a logical part, i.e. some part of all that it denotes; thus when I say that some larkspurs are personal. I mean some species of that genus: when I say that some aimake annot swim, I mean some species of animal, or some individuals of some species. Now the singular, particular, and universal judgements may be represented as referring respective an individual, to a part of a class, and to the whole of a class, i.e. to one, some and all of a certain number. Or since an individual in a part of a class, i.e. to one, some and all of a certain number. Or since an individual in ineapable of logical division, and a singular term, as denoting one individual, cannot refer to less than all that it denotes, singular judgements may be ranked with universal judgements, and constrated with particular; both the former referring to the whole of

¹ Cf. infra, p. 159, n. 1.

what their enlipicts denote, while the latter refers to a part only. We shall see latter, in dealing with syllogism, that singular judge-ments may for certain purposes be treated as if they were universal, because they equally render possible certain inferences. But at present it is important rather to realize that such attempts to treat the differences between singular particular and universal, or singular + universal and particular, as morely quantitative do not do justice to the differences in the thought contained in them.

A logical whole or class (if we are to give it that name) is as we have already seen-ill conceived as a collection of individuals. It is rather an unity, or identity running through things which are different. It may form the subject of our thought and of our indeement: but it differs from an individual not as all from one of a collection, which would be a quantitative difference, but rather notionally as what is universal from what is individual. The difference between singular and universal indocuments is therefore not essentially quantitative. Again, the individuals contained within a class are not, as individuals, an unity but a collection : between some and all of this collection the difference is quantitative : but that is not the proper difference between a particular and an universal independent for the universal independent regards primarily the class as kind, and not as a totality of individuals. -The difference therefore between particular and universal independents. is not essentially quantitative. On the other hand, the difference between individual and particular judgements is often quantitative.1 A criticism of the forms in which language expresses judgements of these different types will throw further light on what has just hear maid

It is common to indicate an universal judgement by the words

¹ The Aristotelian diration (or rather Platonic—for it occur in Platonic Platonica) constitution is another example in which differences not resulty quantitative have been presented under a quantitative form. A monarchy, an aristocnery, and a democracy though said to differ according as power is in the hands of one man, of the few, or of the many, really that Aristotla does not put forward any purely quantitative diration of judgements (of de fatery, vii. 17 88 few) of service and service of service and the service of service of service of services.

all or so (sous) prefixed to the subject, according as the judgement is affirmative or negative: a particular indocument by the word some similarly prefixed : these are called signs or marks of anantity. The idiom of language will indeed often express a universal indocument in other wave : we can say Man is mortal as wall as All men are mortal . A harometer will not more in a namum as well as No harometer will much in a narrow Rut in the absence of a mark of quantity, it is not always clear whether a judgement is meant to be universal or particular; if I say Women are jealous, A flower is a beautiful object. I need not mean all flowers, or all women. Precision requires the quantity of a judgement to be expressly indicated . particularly where (as in logical examples) the judgement is taken out of context and we lack the help which context often affords us in divining the writer's intention; and at least where the subject is in the plural 1, the words all, none, some are appropriated to that service. A judgement without any mark of quantity is technically known as an indefinite judgement: because it is not clear whether the whole, or only a part, of the extension of the subject is referred to and so the scope of the judgement is undetermined : the examples just given. Women are jealous. A flower is a beautiful object, are therefore indefinite indocuments.

At the same time, the words all and sous, as signs of the universality of a judgement, have disadvantages of their own. For a judgement is really universal, when the subject is universal or general, and the predicate attaches to the subject (or is excluded from it) necessarily; but if it is found to satisch to the subject (or to be excluded from it) in every existing instance without any necessity that we know of, we use the same expressions, all and some. Thus we may say that No American poet stands is the first rank, or that All the French ministeries or short-lived; but neither of these is really an universal judgement. Each is a judgement made about a number of individuals: it states an historical fact, and not a ceientific truth. It would be convenient to call such judgements collective or unumarative judgements; for they really collect in one the statements which may be made about every

¹ A form like 'Man is mortal' is clearly universal; but represented in symbols it will not unambiguously show its universality.
² Cf. Bradley's Logic, Bk. I. c. ii. §§ 6 and 45. In the Table of Contents he speaks of 'collective' judgements in this same.

instance of a certain class, and make their assertion on the strength not of any conceptual necessity, but of an enumeration.

We must of course distinguish the question whether a judgement is meant as universal, from the question whether we have a right to enunciate it universally. If instead of saying All the Preach ministries are short-lived (where the article the shows that I am referring to all of a certain number of thinge), I were to say All Preach ministries are short-lived, it might be contended that the judgement no longer referred to individuals or instances, but affirmed a necessary character of French ministries as such. In truth the statement is not clear, and a man would have to sak me, whether I meant it as an historical summary, or an universal truth; but the ambiguity of the statement is the very point to be noticed; for the two interpretations indicate the difference between a merely enumerative, and a true universal, judgement. If we contrast such judgements as All my bones are out of joint and All triangles in a sumicine are relateranted. In difference is very plain.

We have seen that there is a marked distinction between a sinoular indocement, whose subject is an individual, and an universal or particular independent, whose subject is a general or abstract term, a concept or kind of thing. The enumerative judgement (and this is true in some degree of the particular judgement also) approximates to the type of the singular rather than of the universal.1 For though the subject be a general term, and I predicate about all the members included under that term, vet I do so because I have examined them as individuals, and found the predicate in them all, not because of any necessary connexion between the predicate, and the common character of these individuals which the general term signifies. French ministry is a general term ; but (for all that I see) it is not because being a French ministry involves being short-lived, that I assert all the French ministries to be short-lived; it is because I have noted each case; just as it would be upon the strength of noting the individual case that I should assert the first ministry of M. Jules Ferry to have been short-lived. At the same time, the collective judgement, though thus approximating to the type of the singular, gives the hint of a true universal judgement. It suggests that the ground for the

¹ Cf. Bradley's Logic, Bk. L c. ii. § 45.

predicts may lie in the common character signified by the general term under which all these instances are collected. If I say Lather sees lated, there is nothing to indicate what about him was hateful: with which of all the coincident attributes in Luther his hatefulness is universally connected. If I say All reformers have been lated, though that is as much an historical statement as the first, and therefore enumerative only, it suggests that the reason why all those men have been hated (Luther and Calvin, Cromwell and Gladstone—the statement implies a possible enumeration) lies in the fact that they were reformers. Thus from an enumerative judgement we may pass to an universal connection of characters. When we enuaciate sumerative judgement more close summerative judgements, we are on that road: sometimes factors.

The difference between a true universal independent and one merely enumerative is exceedingly important. The one belongs to science, the other to chronicle or history. An universal judgement holds of any and every instance, alike past present and future, examined or unexamined. An enumerative independent holds only of those instances which we have examined, and summed up in the subject. All reformers are hated; if that is merely enumerative, it affords me no ground to anticipate hatred if I undertake reform : it affords me no explanation of the hatred with which reformers have been met. But if it is a true universal, it explains the past, and predicts the future. Nevertheless an universal judgement has nothing, as such, to do with sumbers of instances; if the connexion affirmed in it be necessary, the judgement is still universal, whether there be a million instances of its truth, or only one 1; so that the form 'All A is B' hardly does justice to it. An enumerative judgement contemplates a number of instances, and refers to all of them; and the form 'All A is R' or 'All the A's are B' expresses it adequately.

The particular judgement may be interpreted as referring either to individuals not enumerated or to an universal not fully determined; and it will approximate more to the enumerative, or more to the

¹ Or, as some logicians would add, none. Buch a view makes the universal judgement, however, purely hypothetical: cf. Leibnis, Nouseeux Essais, IV xi. 14; Bradley, Logic, Bk. I. c. ii, §§ 48-6; Bosanquet, Logic, vol. i. pp. 278-282; a also Bradley, Appearance and Radily, p. 361.

universal, accordingly. If I my Some somes have ruled hingdons, I mean women whom I could enumerate—Seminamis, Cleopatra, Zenobias, Rinebeth, Christina, &c.: not women of such and such a type, but this and that woman. If I my Some pipments fade, I do not mean pigments that I could enumerate, but any pigments of a certain kind; and supposing that I could specify or determine the character of pigment, I could say that all pigments of that character fade. There is nothing in the outward form of a particular judgment to show whether the speaker is thinking rather of individuals whom he does not name, or of conditions which he does not same, or off conditions which he does not some of the point of the pidgement will often entitle no this moint.

It will be readily seen that there is the same nort of difference between the particular judgement interpreted of individuals not enumerated, and the particular judgement interpreted of conditions not fully specified, as exists between the enumerative and the true universal judgement. If the women vaguely referred to as some were enumerated, I could my All the somes on my list have ruled hispdoms; if the pigments vaguely referred to as some were characterized, I could my All such pigments fade. The former is the enumerative, the latter the universal All. And this difference, whether between the two interpretations of the particular judgement, or between the enumerative and the universal, may be expressed by saying that in the one case the judgement is interpreted in extension, when we are thinking primarily of the various instances (individual or specific) included in the subject to which the predicate refers; it

It will be remambered that in discensing the criession and intension of terms, it was pointed out how the extension of a term meant, properly, subordinate terms conceptually distinguished, and not merely the instance of a kind reparted as only numerically distinct. Thus in the extension of the term shilling would be included shillings of different disc or standard finences: but the extension of the Queen Victoria Jubiles shilling would not be subdivided. At the same time it was recognized that we may fit our have, or on the multitude of different shillings having that character: for things of a kind are a one in many, or a many in one—one form in many instances, many individual in one type. When we think of the many more than of the one, we may be said to consider the term in its extension: when the one than of the case, or, in its intension. And indeed individuals or placed that the contract of the contract o

is interpreted in intension, when we are thinking primarily of the subject as concept, of the character implied in the subject term. with which the predicate is connected. 'Some A is B' is internested in extension if I think of this that and the other 4. in intension if I think of d'a of a certain character. 'All d is R' is interpreted in extension if I think of every one of the A's in intension if I think of the character of A as such

What has been said on the quantity of indocuments may be summed up as follows. Judgement predicates either of individuals. or universals. In the former case, when it predicates of one individual the indocement is called singular: when of every one of a collection or enumeration, it may be called collective or enumerative. In the latter case, when the predicate is affirmed (or denied) of the subject without respect of instances, and therefore in any and every instance, the judgement is called universal; when otherwise, it is called particular. But an universal judgement is indicated by the same words (All and None) as an enumerative, and is often confused with it. A particular judgement is really incomplete: it may be an incomplete enumerative, or an incomplete universal judgement. according as we think rather of the instances we imperfectly denote, or the conditions we imperfectly specify, in the subject, A judgement may be viewed primarily in intension, as asserting a connexion of content, or in extension, as asserting a certain character in individuals. The former aspect predominates in the universal, the latter in the enumerative, and even more in the singular judgement: in the particular, sometimes the former and sometimes the latter, according as we think more of the conditions imperfectly specified, or the instances imperfectly denoted. Some of these distinctions, though we are conscious of them in our thought, are not expressed in language; and for certain purposes of inference, it is enough to consider judgements simply as either universal or particular: universal, when the whole of a kind 1, or

might think of the shilling in my pocket, in yours, &c.); though when the grounds of distinction are no longer proper to the kind (as distinctions of first and second, here and there do not belong to shillings we shillings, they are ignored in classification.

1. a. a kind or any 'universal'; but I have swoided the word 'universal' here, and preferred kind (though otherwise a less appeats term) in order to avoid controls to bettern the universal concept referred to in the

judgement, and the universal judgement referring to the whole of this universal.

when an individual is referred to (for in both cases the subject is completely indicated), particular when a kind is referred to only in part (and the subject therefore incompletely indicated).

In respect of quality, judgements are distinguished as affirmative or agestire. An affirmative judgement assigns a predicate to a subject; a negative judgement puts it from it. But the distinction between affirming and denying is too familiar to need and too simple to admit of expressing in any other way, in order to indicate what is meant.

There are certain difficulties connected with negative judgements which have already met us in dealing with negative terms. Judgement, as we have seen, refers to the existent: the content of our thought is declared to express the character of the real, its manner of being (so the judgement declares) is as we conceive. But the real is positive: it only exists by being something, not by being nothing. A negative indeement declares what it is not, and how can this express it as it is? Dead-nett/es don't sting. How does that tell me anything real in dead-nettles? You may say that I formed an idea of a stinging dead-nettle, and in the negative judgement declare it false, an idea of nothing real. But the indepenent is not about my idea; I may reflect on that, and say that the idea I had formed of a dead-nettle was a wrong one : at present I am judging about the dead-nettle, not about any past idea of it. And when I say that it does not sting, what am I saying about it? in it, what is this property of not stinging? surely, it may be urged. just nothing: so that the negative judgement expresses nothing real.

These migrivings are sometimes, though unfairly, met by ridicule. Still, in face of them, we must assert, that everything finite is what it is, by not being something different; and at the same time, that it is not something different, in virtue of what it positively is. Hence we must accept the negative judgement as expressing the real limitation of thinge; but we must allow that it rests upon and presupposes the affirmative. If dead-nettles do not sting, there must be some characteristic which they do possess, incompatible with stinging. There is always a positive character as the ground of a negation. Snow is not hot, because it is cold;

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Moreover this would really mean that I now judged a previous judgement to be false: about which the original question would at once arise.

this is not indeed an explanation of the temperature of mosw; but it means that a material body (which must have some temperature) can only not have one degree of temperature through having another. If sow had no other degree of temperature, it would have 212° Pahr. if it also none but 32° Pahr. it must have that.

To say that negative judgements presuppose affirmative does not get rid of the difficulties to which we have referred. If mow is not hot because it is cold, then the cold is not hot. No one will deny that; some people will think it a mere tautological proposition. But it is not tautological, though it is superfluous. It is tautological to say that the cold is cold; to say that it is not hot because it is cold informs us that hot and cold are mutually exclusive attributes. Cold is no more identical with not-bot, than odd with not-even; though the numbers which are odd are the same numbers as are not even. The reciprocal exclusiveness of certain attributes and mode of being is the real truth underlying negation. But for that, everything would be everything else; that is as positive, as these several modes of being is the of being themselves.

Negation, as Plato saw 1, is as necessary as affirmation, if there are to be any differences or discriminations within reality; that A is not B means that it is different from B and not that it is non-existent.

[The further pursuit of this subject would take us too far into metaphysics. It may be pointed out in passing that the notion of an infinite (or, as philosophers sometimes say, an absolute) being in of a being who is everything that there is to be; of whom it cannot be said that he has one attribute by lacking another; whereas finiteness comes by limitation and exclusion: whence Spinoza's Determinatio ast segatio. Whether this is a tenable conception is another matter. In particular it raises the problem of the meaning, and reality, of evil. For if an infinite being is all things, and evil is something real, he ought inter alia to be will. It has been contended therefore that evil is in reality just nothing, a view against which there are obvious objections on the surface: or at least that it is a mere appearance incident to limitation, but in itself no more than limitation.

It has sometimes been proposed to treat the negative judgement,

A is not B, as an affirmative judgement, A is not- B^1 , by combining the negative with the predicate. But insamuch as the reciprocal exclusiveness of certain attributes and modes of being is a positive fact, it is no use trying to ignore it by a verbal manipulation. Nothing will make A is not-Ban affirmative judgement, unless not-B is a positive concept: and if not-B is a positive concept (sav C). it is only because B and C are reciprocally exclusive attributes : but if they are reciprocally exclusive attributes, then C is not B and B is not Co nor can these negative judgements he done away by repeating the same manipulation and writing C is not R. R is not C. For if C means the very same as not R then not C means the very same as not-not-R and the proposition R is not-C means no more than R is not not R. That however is abourd: for C is a positive concept, and the consciousness of the distinction between it and R and of their reciprocal exclusiveness cannot be reduced to a consciousness that B cannot be denied to be itself. The argument thus expressed symbolically can be easily applied to a concrete case by any one who chooses to substitute for B and C odd and even or doe and horse : though there is less temptation to think not-a-doe a positive concept, than not-odd, as it leaves us to select in the dark among a large number of still remaining alternatives.

Judgements are distinguished according to relation into categorical, Appothetical, and distractive. We have been considering hitherto categorical judgements. A categorical judgement merely affirms or denies a predicate of a subject : does bark, dead mon tell no tales. An hypothetical judgement connects a consequent with a condition which it does not however, imply to be necessarily fulfilled: if money is scarce, the rate of discount rises. The condition is called sometimes the antecedent (in grammar, the protesis), as what is connected with it is called the consequent (in grammar, the apodosis). A distunctive judgement affirms alternatives : rocks are either igneous, agreeus. or metamorphic.2 The hypothetical judgement is sometimes called compunctive, as conjoining the truth of the consequent with that of the antecedent: while the disjunctive disjoins the truth of one alternative

¹ Such judgements, with an infinite term (cf. p. 30, supre) for predicate, have been called infinite judgements.
² For any given rock, these are alternatives: for rocks collectively, they are three forms which are all realized: cf. p. 168.

from that of the others. Both are sometimes called complex judgements, in contrast with the categorical, which is called simple.

ments, in contrast with the estagorical, which is called amplie.

In an hypothetical judgement, the antecedent and consequent
may have the same, or different, subjects: the scheme of the
judgement may be either 'If A is B, it is C' (If cons is scarce,
it is dear), or 'If A is B, C is D' (If money is scarce, the rate
of discount rises). Again, either antecedent or consequent may
be either negative or affirmative: but these differences make
no difference to the character of the judgement as hypothetical; it still affirms the dependence of a consequent on a condition:
hence the distinction of affirmative and negative, though applying
to the antecedent and consequent everally, does not apply to the
hypothetical judgement as a whole.

Where the subject of the antecedent and the consequent is the same, the hypothetical judgement may commonly be reduced to categorical form: 'If A is B, it is C' may be written 'A that is B is C': If corn is scarce, it is dear, becomes Scarce corn is dear. Even when antecedent and consequent have different subjects, a little manipulation will sometimes produce an equivalent judgement categorical in form: If wishes were horses, become would ride might be written Become whose wishes were horses would ride. For the hypothetical judgement asserts a predicate of the subject of the consequent, under a condition expressed in the antecedent; and if that condition can be expressed as an adjective of the subject of the consequent, then of that subject, so qualified, we may assert the predicate in the consequent categorically. But we do not thus reduce hypothetical to categorical judgements: the hypothetical meaning remains under the categorical dress. Scarce corn is dear is not really a judgement about scarce corn, but about corn; we realize that corn is something which may be scarce, and is dear when seame: and so the dependence in corn of a consequent on a condition is the burden of our judgement about it.

The difference between the categorical and the hypothetical judgmenta—between affirming or donying a predicate of a subject, and asserting the dependence of a consequent on a condition—becomes clear in the case of unfulfield conditions, in past or future time. If I had served my God as I have served my hing, He would not have given me over in my grey hairs: no doubt this implies the categorical judgment God does not forestate those who serve Him

faithfully; but it cannot be reduced to this, for it implies also Therefore He would not have formakes me, of I had served Him stathfully; and we cannot eliminate the hypothetical judgement. Kopicor Ahav bashis profibus quarterial propers; here it is not stated whether Crossus will cross the river or not; so that as the fulfilment of the condition upon which the assertion in the consequent depends is left in doubt, there is nothing but the dependence categorically assertion. It may be urged that at least the dependence is assertion.

It may be urged that at least the dependence is categorically asserted; and therefore the hypothetical judgement is categorical after all. This is a very good answer to any one who attempts to abolish the distinction between the two judgements by deelaring that all judgements are in reality hypothetical; for it shows that the hypothetical does presume the categorical. But it does not invalidate the distinction rest upon the difference between asserting a dependence of consequent upon condition, and asserting an attribute of a subject; if it is granted that the hypothetical asserts the former, though it do so categorically, yet it differs from the categorical judgement.

It has been said "that the very reason just given for maintaining the essential difference of these two types of judgement excludes the consideration of that difference from Logic. For both assert; they differ in what they assert; the difference is therefore in the matter and not the form of judgement. We have the same form, A is B, whether for A we write Crossus, and for B as ting of Ipdia, or for A the destruction of a great power, and for B as thing of Ipdia, or for A the destruction of a great power, and for B as the Ipdia on Crossus crossing the Halps. But it will be readily admitted that the distinction between categorical and hypothetical assertion in formal in the sense that it meets us, whatever be the subject we may think about; and to exclude it from Logic on the ground that, as compared with the common form of assertion in both, it is material, only shows the impossibility of making Logic a purely formal science. It is claiming to consider the genus, and refusing to consider the species: a procedure which would be tolerated in no other science, and cannot be tolerated in Logic.

² Cf. Manael, Prolegomena Logica, pp. 282, 251.

¹ This oncice shows that the cotward or grammatical form of a judgment is no sure guide to the meaning; for it may be translated 'Crossna will cross the flatys and ruin a great power', in which case it becomes categorical: the two translations are clearly different, though the same Greak line covers both sense.

There is a metaphysical problem suggested by the hypothetical independent, which must be briefly noticed. If Hannibal had marched on Rome after Cannae, he would have taken it. This judgement makes an assertion : in doing so it declares something to hold good of the real for it declares its own content to be true. But what does it declars true of the real and what historical fact (as we may put it in such a case) does it affirm? Not that Hannihal marched on Rome after Cannae for he did not nor that he took Rome for he did not: nor that the one event was due to the other for neither hannened. If he had marched on Rome then he would have taken it : but that is not a fact in his history, or in the history of Rome: it is an unfulfilled contingency: and how can that he real? Every hypothetical judgement presents this problem: for it asserts that under certain conditions something would exist or have existed but not that the conditions are realized nor therefore that it does or will exist or has existed. Nor does its truth require this; in order that an hypothetical judgement should he true neither condition nor consequent need be realized: and yet if an hypothetical judgement is true, it is true of reality, and reality, we may urge, is actual; what then does the hypothetical judgement affirm to be actual in the real? A character. save Mr. F. H. Bradlev 1, which is the ground of the connexion hypothetically asserted in the judgement. Rome was in such a state that it could not have resisted Hannibal after Cannae. This is true : but it still leaves us with the question, how can there be the ground. in the real universe, of something which nevertheless does not happen? We speak freely of unrealized possibilities, as if they existed as well as realized actualities. We are not always conscious of the metaphysical difficulties involved : how are we to think of what we so freely speak of? When we reflect, in Logic, upon the hypothetical form of judgement, we become conscious of the problem.

The disjunctive judgement may be expressed schematically in the forms 'A is either B or C' (Every man at forty is either a fool or

¹ Logic, Bk. I. c. ii. § 50 : cf. § 52.

^{2.56.,} pkr. 1. C. ii. 900' cit. 900.
The reader must not uppose that these paragraphs deal at all completely with the promptes maked by the hypothetically off more of judgement, bothing, for each and about the questicty of hypothetical judgement, and the period of the period of

a physician), 'Either A is B or C is D' (He either fours his fate too much, Or his desert is enall', Who dares not put it to the touch, To gain or lose it all), 'Either A or B is C' (Either the Pope or the King of Italy should retire from Rome). As the hypothetical judgement always affirms a disjunction, whether the alternatives themselves be given affirmatively or negatively. So far as the nature of the disjunction goes, there is no difference between 'A is either B or C', and 'A is either not B or not C': between 'Either A is B, or C is D', and 'Either A is not B, or C is not D': between 'Either A or B is C', and 'Either A is not B is not C'. But it should be noted that 'Neither . . . nor 'is no B is not C'. But it should be noted that 'Neither . . . nor 's no disjunction at all, but a conjunction of negation. On St. Paul's voyage to Rome 'neither sun nor stars in many days appeared'; there is no choice between alternatives here, but two statements—the run did not appear, and the stars also did not.

There may be any number of alternatives in the disjunction; but that clearly does not alter the character of the judgment.

It is not always clear in a disjunctive judgement whether the alternatives offered are meant to be mutually exclusive. If A ceither B or C, then it cannot be neither; but may it be both? The question concerns the right interpretation of a form of speech, rather than the nature of disjunctive judgement. Sometimes from the nature of the case we may know that the alternatives exclude each other: as if we are told that Plato was born either in 429 or 427 s.c. Where this is not so, it is perhaps after to assume that they are intended as mutually exclusive, unless the contrary is stated; a legal document is careful so to write it, where 'A or B or both' is meant, or to write '4 and/or B' with that signification.

It has been suggested that the disjunctive judgement is in reality a combination of hypotheticals; that 'A is either B or C' means 'If A is not B, it is C; if A is not C, it is B; if A is B, it is not C; if A is C, it is not B'. Doubtless these four propositions are involved (supposing B and C to exclude each other); but we do not therefore get rid of the peculiar nature of the disjunctive

[&]quot;This might be equally expressed. 'He either fears his fats too much or dearms little i indeed in sense the alternative pedicates are predicated of the same subject, not (as in the proposition Ether Tactius was a aleaderer or Thereise a cities) of different subject. This affords another example of the fact that the logical character of a judgement cannot aiways be inferred from the grammatical form of the proposition.

judgement. For they are not four independent hypothetical judgements; and their force is not appreciated, unless it is seen that together they make up a disjunction, that they offer us a choice between alternative hypotheses. Thus disjunctive judgement at once includes and goes beyond hypothetical, in the same sort of way as hypothetical judgement includes and goes beyond categorical. An hypothetical judgement makes an assertion, like a categorical; but what it asserts is a relation of a consequent to a condition. A disjunctive judgement involves hypotheticals, but it presents them as alternatives and asserts that truth of one or other of them.

The disjunctive indocement also raises a metaphysical problem. when we ask what real fact corresponds to it. 'Plato was born either in 420 or 427 B.C.' cannot state the actual fact about Plato: he was born definitely in one year, not merely in one or other: it is because see do not know in which, that we state an alternative, and there was no alternative in the event. Here, therefore, the disjunctive judgement seems rather to express the state of our knowledge, than the state of the facts. On the other hand 'Number is either odd or even ' seems to express a disjunction in the facts 1: and the species of the same genus are a kind of real disjunction. If a colour is to exist, it must be blue, or red, or some other colour, and if it is one, it can be none of the others. We come back here upon the same truth which met us in considering positive indocements that a thing is definitely this or that by not being something else - we have to recognize also that there is often a limited number of possibilities, in the way, for example, of colour, or of animal species, but why or how there should be a limit to what is possible in the universe is a hard question a

We come next to the distinctions of modality in the judgement. In respect of modality, judgements are distinguished as assertoric, problematic, and spodeictic; the first is sometimes opposed as pure to the other two as modal; but we shall find that if judgements are divided into pure and modal, the assertoric can be

¹ Of course there is a disjunction in the facts, in the former case as well, so far as that a year must be either the 429th or the 427th or some other number, from any point of time whence we choose to begin our reckoning.

² For the fuller treatment of this form of judgement also the reader is referred to more advanced works.

conveniently retained as a form of modal judgement. Judgements of the form 'X is Y', 'X is not Y' are assertorio—'the train is late', the train is not late'; of the form 'X may be Y', 'X may not be Y', 'problematio—'the train may be late', 'the train may not be late', of the form 'X must be Y', 'X cannot be Y', apodesicate—'the train must be late', 'the sun cannot be late'. The distinctions are also expressed by adverbs: X actually, possibly, necessarily is $(\sigma'$ is not) T.

In the sense of the word to which we have so often called attention, these distinctions are clearly logical: i.e. they belong to no special science, but recur in our thought about all kinds of subject. Whatever X and Y may be ', we may find ourselves asserting that X is that it may be or that it must be T's.

It is clear that the modality of the indepenent whose subject and predicate are X and Y does not in any way affect or modify the predicate Y When I say that the train is actually or possibly or necessarily late it is not the predicate late which is actual nonsible, or necessary, -but the train being late; for there are not those three kinds of lateness. 'The bloseoms of that chrysanthemum are possibly white'. 'the blossoms of that chrysanthemum are actually white' it is clear that 'actually' and 'nossibly' do not qualify the predicate white, as the adverbe 'purely 'or ' brilliantly' might do: there is no such colour as possible white, as there is a brilliant white or a nure white. 'Water runs down hill': 'water must run down hill'; these are not different ways of running, like running fast and running slowly. Grammarians tell us that adverbe qualify verbs and adjectives; but these adverbs, actually, possibly, and necessarily, seem to form an exception to the rule. They qualify neither a verb nor an adjective, though these be predicates of the judgement, but the judgement itself.

For the real meaning of these expressions—'X is actually Y',
'X is possibly, or may be Y', 'X is necessarily, or must be Y'—

¹ Except so far as in some subjects, like arithmetic, a judgement is nearly always made with consciousness of its necessity: cf. infra, p. 175. Even here however light say, before I had made the calculation, that 87596 may be a source number.

may on a square number.

For the aske of brevity, I shall not throughout consider negative as well as affirmative judgements. It should be noted that the problematic affirmative 'X' may be Y' is not contradicted by the problematic negative Y.X may not be Y', but by the apodetic 'X' cannot be Y'; and similarly the problematic negative by the apodetic faffirmative.

is rather this: 'that X is Y is actual', 'that X is Y is possible',
'that X is Y is necessary'. They involve reflection upon the judgement that X is Y, and express difference not in the nature of X or
of the predicate belonging to it, but in the nature of our grounds
for affirming X to be Y. We may speak of differences of modality
in judgements, if we like, as differences in the mode in which, for
us, the judgement is grounded. Yet such an expression is open to
misinterpretation. For when I say that X may be Y, I do not
judge at all that X is Y, but that there are insufficient grounds for
so judging. We must, however, sortinize these forms of expression more closely; for the illustrations so far chosen do not bring
out their different meanings, having been chosen merely with the
purpose of showing that modality qualifies neither the subject
nor predicate of what appears to be the judgement in which it

occurs. Nothing is more fundamental in our thought than the constant search for necessity in our assertions the desire to see that the matter of fact asserted could not be otherwise than we assert. In this search we are not content with what is commonly called experience. I may find in my experience that a man whom I had trusted does me a wrong but I want to know further why he did it. So it is with any other event of which I have no explanation. My explanation in such a case would lie in connecting the event with another: we are perpetually tracing connexions between one fact and another, and cannot conceive anything to be completely isolated from everything else. 'Nothing in this world is single; All things by a law divine In one another's being mingle': this is the faith that underlies all effort after knowledge. All judgement expresses the connexion of things, or of one attribute with another in things; about a thing isolated altogether from everything else. united with no other by any common characteristic, judgement would be impossible. But we realize only gradually the interconnexions of fact. In many judgements intended by us to express the facts as we apprehend them, we find upon reflection that the connexion of the subject and the predicate is not intelligible to us ; we then seek some ground for the fact asserted; and if we cannot

¹ τελευτάτη πάντων λόγων έστιν άφάνιστε τὸ διαλύειν Γεοστον ἀπὸ πάντων : Plato, Soph. 259 m. ('All speech vanishes altogether if each thing be severed from everything else.')

find it by seeing more clearly into the fact, we look for it in another, i.e. in a wider system to which the first belongs. Often, however, when we make a judgement we do so without full reflection upon what is asserted and upon the grounds for it; and such judgements, barely asserted, are called assertoric; and the expression of them, 'X is X' ('crows are black', 'the train is not arrived'), is bare of any words that indicate reflection on a grounds for our assertion. It is true that such judgements, reporting what we perceive, are not made arbitrarily; but the appeal to perception does not satisfy us; for though we may be unable to doubt that a rose is red when we see it, and seeing it justifies our assertion, yet it does not show why the rose is red, and the fact remains one for which we see no ground.

But the assertoric form of judgement, X is Y, may express two different mental attitudes. We may affirm or deny unhesitatingly but without any thought in our minds of possible grounds for what is asserted. We may repeat our affirmation or denial as unhesitatingly as before when the question whether there are sufficient grounds has occurred to us, even though we have not found any to satisfy us. Some men detect water with the diviningrod. That is nerw entraordinary: how do you account for it? I can't. but they detect it. Here the assertoric judgement is challenged. and reneated: in the interval, we have reflected on the grounds for our judgement, and found none; none, that is, that make the fact asserted intelligible, though we may still think we have grounds for making the assertion in our experience of events that we cannot account for except by connecting the detection of water with the use of the divining-rod. We therefore still use the assertoric form; yet the force of it is not quite the same, though the words in which we express ourselves are: and we must be careful to notice the difference, since in Logic it is not the form of words that matters, but the form of thought,

The difference lies in the absence or presence of the thought of the grounds of our judgement. If there is no thought of them, we make the judgement without looking beyond it; if there is thought of them, we look beyond the judgement in making it, even when we look in vain. It might perhaps be best to call a judgement pure, rather than modal, when it is made without any thought of its prounds; and to call it assertoric, and so assign to it a species of modality, only when it is asserted with the thought of grounds that are not forthcoming. In this case, the introduction of the word actually would mark a judgement as assertoric, but the ordinary categorical form, X is (or is not) Y, might represent either a pure or an assertoric judgement. Very often the emphasis of the voice, or the use of italics, serves to distinguish the pure from the assertoric sense of such a form of judgement. If I say 'The stimulation of the retins by waves of ether is correlated with sensations of colour', I may barely intend to state a fact, without thought of looking beyond it for grounds; but if I emphasize the 'is' or write it in italies, I should be understood to affirm it as an actual fact in spite of my inability to give grounds for it; the general thought of grounds accompanies the judgement, but in a different form from what occurs in the problematic or apodeictic independent.

By the expression 'grounds for our judgement' in the last paragraph has been meant grounds for the matter of fact judged : and at the risk of repetition, it may be well again to distinguish between this, and grounds for judging. For the difficulties in the subject of modality centre in this distinction, and if our discussion cannot hope to solve the difficulties, it may at least be well to indicate where they lie. Even if I do not see how a man is made aware of the presence of water by the divining-rod. I may have reason for indeing that he is, if I have known water found by men who had no other means of detecting it. In scholastic phrase. I have here a ratio cognoscendi, but not a ratio essendi: a reason for acknowledging the fact, but not a reason for the being of the fact.1 Of course the ratio essendi is the best of all rationes coonsscendi : of course also my ratio coonoscendi may turn out inadequate on closer scrutiny. And if a judgement made without any thought of its grounds-what we have now called a pure and not a modal judgement—be reasserted in assertoric form, it is seldom that it is purely assertorio. Either we find our reasons for asserting it insufficient, and it has acquired the character of a problematic judgement; or we have begun to explain the fact, and then the judgement is on its way to become apodeictic. 'There were species

¹ I have translated cognoscendi by 'acknowledging', because in the full sense of knowledge I do not know a fact which I do not see in its own nature to be necessary.

once intermediate between the ane and man. How do you know that, since no specimen has been found? Much may have existed. of which no trace has survived.' This reply gives a tinge of the problematic to the original independent. Suppose a different reply . The structure of man bears the same relation to that of the ane as prevails between species in other cases where specimens of intermediate forms, now extinct, have been preserved.' This is something of a ground in the nature of the facts for accepting the original judgement; there must therefore, we might say, have once been forms intermediate between man and ane. Our 'must' in such a case expresses a different kind of necessity from what it expresses in a really apodeictic judgement; but still, it does express a kind of necessity. It is rare that a judgement is reaffirmed after challenge with unshaken confidence, and yet with no thought of any ratio essendi. 'I feel ill' is such a judgement. If a man challenges my assertion, I cannot justify it, but only reaffirm it. But the barely assertoric attitude, when once the mind has been awakened to the thought of the grounds of its judgement, is rare. Our pure judgements, when we have got so far as to ask their grounds, generally present themselves as either problematic or apodeictic. This might be considered to justify us in calling a nure indepenent, i. e. one made without reference to its grounds in our thought, assertoric; instead of reserving that name for the case in which a judgement is made in the consciousness that independents need grounds, and yet is neither problematic nor anodeictic. Nevertheless the distinction between the two cases ought to be observed: and is in fact expressed by the addition to the pure indocement 'X is Y' of the adverb that marks the assertoric form of modality, in the expression 'X actually is Y'. If we turn to the apodeictic and problematic judgements, the char-

If we turn to the apodeictic and problematic judgements, the character of the assertorio will become clears P be contrast. The apodeictic may be considered first. When we say 'X must, or cannot, be '('X necessarily is, or is not, Y'), we imply that there are grounds known to us for X being, or not being, Y. As a rule, these grounds are conceived to lie outside the content of the judgement XY: i. e, we do not upon reflection see immediately that X must or

^{&#}x27;We may symbolize thus the judgements whose subject and predicate are X and Y, and which are thus 'materially' the same, but whose 'formal' character—modality, quality, quantity—may differ.

cannot be Y upon a mere consideration of the nature of Y as such . we see it to be a consequence of other truths, which in their turn may be asserted either anodeictically or assertorically. The water must vice in the common numb when the nictor is reject why weet? herenes of the presence of the atmosphere. It is the conecioneness of that around for its rising which leads us to affer the water's rising apodeictically, whereas the mere observation of fact would only lead us to affirm it assertorically. But are we sure it may be asked, that the atmosphere must have weight? for if not, we can only say that the water must rise if and when the atmosphere has weight. We cannot here discuss the sufficiency of the grounds on which we regard the general propositions of science as demonstrated ; but it is clear that if the grounds of an apodeictic judgement are themselves affirmed only assertorically, there is a doubt thrown on the apodeictic judgement. It is necessary, if the judgements on which it is grounded are necessary. Animals must sleen, because they cannot be continuously active.' But how do we know that they cannot be continuously active? And supposing a reason were given, we might ask how it is known to be necessarily true, and so ad infinitum. An apodeictic judgement would thus be merely a judgement, made with reference to grounds from which it followed and which we accepted as true: but since these grounds might not be true, there would be no judgement absolutely necessary, because none safely grounded.

The remedy for this state of affairs would lie in the existence of judgements which we saw to be necessary (i.e. saw must be true) without going beyond them: the ground for the judgement. We have the Y' lying in the content of that judgement. We have

on necessary: and necessary, some immension, or on invices and sangable grounds.

No truth is isolated: and there is none (not even such a truth as 2-2-2-4) which would still be equally true if all other things per impossibile were different (e.g. if 2-2-5 and 2-8-7). So far, no judgement show unmediated, or immediately necessary. But there are judgements show

¹ We may call the necessity of a judgement, which we see to follow from certain grounds, but whose grounds we cannot affirm necessity, a hypothetical necessity. The consequent of every hypothetical judgement is seared as hypothetically necessary—'\(d \) is \(B \), \(X \) is \(T \) injth the written if \(I \) is \(B \), \(X \) is \(T \) injth the written if \(I \) is \(B \), \(X \) is \(T \) injth processary. It is should, however, be noted that in the hypothetical judgement if \(I \) is \(B \), it is a finite processary in the processary is should, however, be noted that in the hypothetical judgement if \(I \) is \(B \), it is a finite processary in the processary is a large from the processary in the processary is a large from the processary in the necessary, either immediately, or on further and assignable grounds.

curved, but they must be so.

already been made familiar, in discussing the heads of predicables, with the notion of judgements in which the subject and predicate are conceptually connected: some such judgements are immediately necessary. That a line must be either straight or curved is a judgement of this kind. A man may assert as fact that lines are either straight or curved, being led to that assertion by the memory of past experience: but if he pause to reflect on the ground for the assertion, he may realize that not only have the lines he has seen or imaging been all of them either straight or

An apodeictic judgement then is one whose truth is not merely affirmed (for every judgement affirms its own truth) but seen to be grounded, either in itself, or in other judgements accepted as true. It is to be noted that many judgements which are really or in thought apodeictic are commonly expressed in assertoric form. In mathematics for example every sten is by the mathematician seen to be necessary : almost all mathematical indocuments are anodeictio 1 . incomuch that it is often summarily said that mathematics deal with 'necessary matter'. There is consequently no need to distinguish anodeictic from other indogenents in mathematics and they are all, as a rule, expressed assertorically : we say '2 v 2 is 4'. not '2 x 2 must be 4': 'the interior angles of a triangle are'not 'must be '- 'equal to two right angles'. On the other hand. many independents expressed in appdeictic form are differently thought. Not only does the form 'X must be Y' leave it uncertain whether the judgement is asserted as immediately necessary. or as grounded in knowledge outside itself-a matter of which we cannot be unaware in our thought when we judge; but also the outside grounds of the judgement may be grounds that merely require the fact asserted or explain it : may be rationes connescends or rationes essendi. At times we even use the apodeictic form of propo-

necessity is seen in a particular case, as we see that 2×2 must be 4 in a particular conting, though it is not seen to be unconnected with all other judgements, but rather to be bound up with others. And the matter of fact in which we find necessity might be something much more complex—a far bigger system—than the numerical relations of 2×2 .

bigger system—than the numerical relations of 2×2.

Almost all; for a few judgements, such as formulae for the finding of prime numbers, have been believed to be universal, and turned out to break down for certain values. These were not apodeicite. If it had been seen that the formula must yield a prime for any value, it could not have broken down.

sition to hide our doubts: we are conscious of grounds for a judgement, and grounds against it, and we look to those only which enforce the side we wish to take, and in reference to them make our assertion apodeiotic. 'It must be so: Plato, thou reasonest well', does not express the same confidence as if the speaker had said it is so.' All these diversities of thought lie conceaded under the apodeictic formula, X must be Y; but it is always implied by that formula that our attention is directed to the grounds for the assertion XY.

The problematic judgement, on the other hand, implies that the truth of the judgement depends on grounds whose existence cannot be asserted. 'X may be Y means that we have not sufficient grounds for asserting positively that XY is true. Thus it involves the same attitude of reflection as the apodeictic judgement, or as the assertoric (if we distinguish the assertoric from the pure); but as a result of reflection, the relation of the content of our judgement to what we know its seen to be different and precarious

In order to understand the meaning of the problematic judgement, we must distinguish between those which are general (i. e. which have a general term for subject) and those which are singular. For where the subject is a general term, the problematic form may or may not express a judgement that is problematic in its logical character. A problematic judgement, as is obvious, expresses uncertainty; but uncertainty has been regarded as a state either of facts, or of our mind in regard to facts. As a state of our mind, uncertainty arises through ignorance; and it is this uncertainty which renders a judgement problematic, in the logical sense in which that is one of the modalities of judgement. As a state of facts uncertainty might mean either of froe things; but only one of these can be meant when the judgement is singular; and the judgement is not in both cases logically problematic. Yet the formula 'I may be I' is used in all these cases.

The judgement 'Rain may fall to-morrow' is a singular judgement: being concerned not with a particular thing or person, but still with a particular day. This judgement is problematic in the logical sense; for it does not imply that the fact, whether rain is to fall to-morrow or not, is uncertain, but only that we are ignorant of the present condition of some at least of those factors (wind and clouds, best and moisture, lie of land, and currents of sir) on which to-morrow's event depends. The fact is really certain, but we are uncertain; the rain falling or not falling to-morrows in no necessary, but to us problematic. With sufficient knowledge we could say 'Rain must (or cannot) fall to-morrow'. But sufficient knowledge is brown our resonance.

Again, 'The Sultan may behead his vizier to-morrow.' This is still problematic, for it implies that we have not sufficient grounds either for affirming or for denving that he will do so. But in the opinion of many, there is here a further uncertainty in the fact itself. For the issue depends in part upon the Sultan's will . and many hold that the future actions of the human will do not lie contained as it were necessarily in the present and therefore that no amount of knowledge would enable us to calculate and predict with certainty the acts of men, or events depending in part mon the acts of men, as it would enable us to calculate and predict events dependent purely upon physical causes. According to this view there is a 'real contingency' in human action.1 Such real contingency would of course carry with it, that our judgements about future contingents must be problematic in the logical sense: we cannot know for certain what in itself is undetermined. But the problematic nature of our judgement in such a case does not spring from our ignorance, since no increase of knowledge could remove it: it springs from the nature of the facts: and the difference in the nature of the facts between their real contingency in the one case, and their necessary interconnexion in the other, is not a difference of logical modality. Indeed, if we regard the human will as a principle of new beginnings, or source of events whose determining conditions cannot be found in events preceding them, we might even say that a particular future human action is necessarily contingent. It is to be observed, however, that this uncertainty in the event itself can only belong, if at all, to future events. If I say 'The Sultan may have beheaded his vizier vesterday'. I imply no more uncertainty in the facts than if I say 'Rain may have fallen vesterday': the same is true of the judgement 'The Sultan may now be beheading his vizier', just as much as of 'Rain may now be falling.' All these alike are problematic only in virtue of my

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¹ There are other views of human freedom which make the future acts of men as certain in themselves as any other.

uncertainty about the facts, and not of any uncertainty in the facts

The upshot of this is, that in singular judgements the problematic form X' may be Y' expresses always our want of grounds for making an assertion, but not necessarily any want of certainty in the facts themselves. All events—the acts of manial one perhaps excepted—happen necessarily when they happen, the conditions being largely unknown to us, we have not sufficient ground for asserting the events; hence our assertions assume a problematic form, X may be Y': meaning, that while we know nothing inconsistent with the assertion that X is Y, we do not know enough to justify us in saying that it must be so; though if it is so, it is so necessarily. Only in human action and what depends on human actions more would admit a real contingency; and would understand the formula X may be Y' to include in such case an assertion of uncertainty in the events themselves.

Let us now take a problematic judgement which is not singular.

'Cancer may be incurable.' Here we mean that though cancer either is incurable or not, we have not undicient grounds for a decision. The judgement is based on ignorance, and is logically problematic. But the same formula sometimes has a somewhat different meaning. 'Currants may be either black, white, or red': 'a man may die of joy'. We do not mean here that we are uncertain whether currants are black, white, or red though knowing they must be one or other; for on the contrary we know that they are all three in different cases. Nor do we mean that we are uncertain whether or not joy can kill a man, but that sometimes it does so. If you tell me that you have a currant bush in your garden, I can say the may be black, white, or red; as to that particular bush I am uncertain. But I make this disjunctive judgement about it because of my knowledge that there are those three colours in currants.

Such a judgement therefore is not problematic in the logical sense; for as referred to the species, or general term, which is the subject of it, it implies not my uncertainty, but my knowledge of the alternatives. Here the facts may be called uncertain, in the sense of being multiform or variable, but not in the sense (in which a particular fact, if really contingent, is uncertain) of not

¹ Or of any other being that has freedom in the same sense.

being the necessary outcome of pre-existent conditions. This variability arises either through the diversity of species necessarily included in a genus (as when we say that a conic section may be either an ellipse a narabola or an hyperbola) or through the multitude and complexity of the elements in the world that co in constantly shifting combinations to the production of what we record as single things or events. Any two elements (the word here must not be confined to its technical chemical sense) taken arbitravily in isolation from everything else would as we believe interact with each other always in the same way. Science endeavours to determine the interactions that would occur between such isolated or 'abstract' elements, and so to enunciate its propositions universally. But in fact we cannot readily secure such isolation. History, or the course of events, depends on all sorts of elements as it were justling in concrete, and so presents perpetually varying combinations or conjunctures. This gives rise. as we previously saw, to the accidental or 'coincidental': which is also sometimes called the contingent 1: and in the sense that the same conditions, in the kaleidoscopic movement of events, are combined now with these and now with those others, there is uncertainty in facts. We might know enough to say what precise conjunction of physiological and other factors is necessary in order that a man should die of joy; but the occurrence of this conjunction depends on historical conditions that are sometimes fulfilled and sometimes not. Hence we make a judgement which is problematic in form, 'a man may die of joy': meaning that if certain factors combine with his joy, a man will die. We have no right to connect a predicate Y universally with a given subject X. if its presence in X depends on the coincidence of other factors; and so long as in our judgement we do not specify all the conditions necessary in order that X should exhibit the predicate Y. our indeement will assume the form 'X may be Y'. These conditions may or may not be known to us. 'Water may boil below 212° Fahrenheit': this depends on its being sufficiently heated, and at an atmospheric pressure sufficiently low: both of them conditions not necessarily connected with the occurrence of water below

¹ In this sense, the region of concrete facts, where such ever-shifting combinations are found, is sometimes called 'contingent' matter, as opposed to the 'necessary matter' e.g. of mathematics: cf. p. 175, sepre.

212° Fahr. But the conditions here are known; and we give our judgement the problematic form, not on account of our uncertainty of the grounds on which the content of the assertion depends for its truth but because we know that those arounds are not always present. Here then the problematic form is due to an omission of the conditioning details. The particular indocument is cometimes particular for the same reason because we omit some of the conditions given which the predicate might be affirmed of the subject universally. In other cases of course the particular independent is all we are able to enunciate and we do not know under what conditions the predicate could be affirmed universally of the subject. Some triangles have the square on one side equal to the squares on the other two -viz. when that side subtends a right angle : 'some children are taller than either parent', but here we cannot give the condition on which it depends. The same difference is observable in the case of these quasi-problematic judgements: as may be seen if the foregoing particulars be put into the form 'X may be Y'. 'A man may smile and smile and be a villain' means much the same as if it were said that some men smile and smile, and yet are villains: but we do not know more than the fact which shows this conjunction to be possible; we cannot state the condition on which the conjunction of a smile with villainy depends In dealing with the quantity of judgements we saw that in the par-

ticular judgement 'Some X is T' we may either be thinking of individuals of the kind X_i not separately enumerated, or of some general determination of the kind X_i not specified, which would involve its being Γ_i that in the former case, it is rather of the nature of the singular judgement: in the latter, it is on its way to become universal. Particular judgements of the latter kind have been called 'modal particulars', because of their close similarity to the called 'modal particulars', because of their close similarity to the called 'modal particulars', because of their close similarity to the passing the particular judgements which we are now considering. They can indeed be expressed in the form 'X may be I' as easily as in the form 'Some X is I'. There is only this difference between the two expressions; each implies that these conditions are sometimes actually fulfilled, the former does not necessarily do so'.

¹ e.g. 'A man may call at every public-house from John o' Groats to Land's End.'

Where a indocument problematic in form states the alternatives within a genus, as if I say that a line may be straight or curved. the architecture of a church classical or Norman or Gothic, it is really as referred to the conne a necessary indocument if we see that the alternatives are necessary but assertoric if we morely eccent them as actual. As referred to any particular subject like the boundary between the United States and Canada or the parish church of Clayfield Porcorum it is problematic because it implies that I have grounds for offering these alternatives but not for oning further and deciding as between them. Where though the judgement is not disjunctive, yet I is general, and the unspecified conditions under which X is Y are known, the meaning of the form "X may be Y' has really nothing problematic about it i. a. it corresponds to no uncertainty in our thought with regard to the content. of the judgement. Where the conditions are unknown as well as unspecified, it has the logical character of the problematic indocement so far as it implies that we are uncertain under what conditions I is Y but is assertoric so far as it implies that we know that there are such conditions, because X is sometimes Y. The singular judgement 'This X may be Y' ('This water may be unwholesome') is problematic in the logical sense, because it means that we are processin whether the conditions under which X is Y are fulfilled in the case before us.

A problematic judgement therefore does not imply by its form that any particular event is in itself uncertain 1; though some hold that there is a real uncertainty about events involving human will. The matter of fact asserted in a problematic judgment whose subject is a general term may be uncertain, in the sense that the given subject does not carry with it the predicate, but will only exhibit it under conditions that are not constantly and necessarily combined with it. But a independent is not logically problematic unless it expresses our uncertainty with regard to the connexion of a predicate with a given subject. All singular judgements of the form 'X may be I' are therefore logically problematic; but general judgements of that form are not really problematic, when the form only serves to cover the omission of the known conditions

¹ To say that an event is uncertain of course often means only that we are uncertain about it.

under which X is Y universally, or to specify one of the alternative forms under which X is known to occur.

[The distinction between singular and general problematic judgements finds a parallel also in the case of apodicitic judgements, but as confusion is not so likely to arise there from want of noting it, the discussion of apodecitic judgement was not bardened by it. Any one remembering what was said in c. iv on the difference between conceptual and historical necessity will see that a singular apodeictic judgement is one in which an historical event is recognized to be necessary on the ground of previous historical events accepted as actual; these last may in turn be shown to have been necessary, on the ground of other events before them: but such a process of demonstration recedes into the past ad signitum, and so we never get more than hypothetical necessity. A general apodeictic judgement, on the other hand, is a really universal judgement—a judgement—asserting a connexion of content or of universals, irrespective of occasion or time.]

We may sum up what has been said of the modality of judgement as follows. In every judgement I intend to assert truth. but not necessarily about the particular reality that my judgement refers to: the truth I assert may be that I am unable to discover the truth about this reality. I may judge without looking for the grounds of what I assert; and in such case my judgement is called assertoric, and expressed in the form 'X is (or is not) Y': it can, however, also be called pure, as being pure or free of any reference to the grounds for what is asserted. On the other hand, I may reflect on the relation which the content of a suggested indeement bears to what I already know, or take, to be true: and if I find it involved in such truths, my judgement is called anodeictic, and expressed in the form 'X must (or cannot) be Y'. Judgements whose truth is seen to be grounded in the nature of their own content are also affirmed apodeictically. Those apodeictic judgements which are grounded in facts not forming part of what they affirm themselves have a different logical character according as these facts can be affirmed apodeictically or only assertorically; if the latter, the judgement resting on them is not strictly apodeictic, for only the sequence can be affirmed apodeictically. If I find the content of a suggested judgement involved in conditions about which I am ignorant or uncertain, I assert it to be possible: such a judgement is called problematic, and expressed in the form 'X may (or may not) be I'. The problematic judgement does not imply that particular events are unnecessary in their happening, though, when general, it does imply that an event of a certain kind depends on a conjuncture or continuency which is not universally passessey. It is possible that when reflecting on the grounds for what we sesert, we cannot find any except that we perceive or remember it, though this may be reason enough to convince us of the truth of our assertion; then the content of the independnt is affirmed to be actual, and the independnt called severtoric and expressed in the form 'X is (or is not) Y', with an emphasis perhaps on 'is', or the addition of the word 'actually'. This assertoric judgement, being not a bare unreflective assertion. but expressing besides our mental attitude towards the content of a judgement, is different from the assertoric judgement, above called also pure that contains no reflection upon the grounds for what is asserted or for its assertion; and as involving such reflection this is model

These distinctions of modality do not then express differences in the necessity with which elements connected in reality are connected; yet they do express this, that whereas some connections in reality are seen to be necessary, others, and the existence of such elements, and their distribution in time and place, are not. Many philosophers have felt it impossible not to believe that the existence of all things, and their distribution, and every feature of their interaction are as necessary as those matters which form the content of our really apodeictic judgements; and if their belief could pass into clear vision, judgements at present problematic or assertoric would be replaced by apodeictic.

[There are a few other adverbs (besides possibly, actually, and accessivily) which may be introduced into a judgement in order to express reference to the grounds for asserting it and an estimate of the truth of its contents e.g. probelly, stuly, placely, stully is all though all but the first of these may also be used merely to qualify some term in the judgement; a truly virtuous woman, for example, meaning a woman virtuous in a particular way, or a falsely delivered measage, one not delivered as it was received,

¹ Hence we cannot accept such a definition as Aldrich offers of modality: 'Modalis, quae cum Modo, h. e. vocabulo exprimente quo modo praedicatum insit subiecto.' Artis Logicas Rudimenta, c. ii. § 2. 1 (Mansel's 4th ed., p. 47).

I whereas a probably dangerous undertaking does not mean an undertaking involving a particular kind of danger. Such adverbe (if used to express our attitude as to the truth of the content of the judgement in which they occur) may be called modal, and judgements modal, in which they are used. But no adverte of any other kind make a indocement modal, and no qualification of the content, but only of the unreflecting directness with which in a 'pure' judgement, the content is affirmed. Differences of tense, for example, must not be reckoned to affect the modality of a judgement 1: they merely affect the predicate, and not our attitude towards affirming the predicate of the subject; and past, present, and future verbs may all occur (as we have seen) in indexments of any modality. No doubt differences of tense are a somewhat peculiar affection of the predicate. If I say Jeks drives furiously, I predicate a different action from what I predicate if I say that he drives slowly; but the action predicated is the same, whether I say that Jehu has driven, is driving, or will drive, and only the time of the action differs. This, however, merely

"As by J. 8. Mill. Logic, I. iv. 2, who rightly rejects the view of those who would make every advant the ground of a modal difference in the proposition where it occurs. The distinctions of modality descend from Articlité, de farter, mil. I and And. Pri. at il. 1, but the word spéces («modes) is said to occur first in the Commentary of Ammonius i. Ammonius i. Ad foster, 17. If you does it past Panni, yoi. i. p. 60-in-intimate of the principal of the principal

[amounts to saving that judgements differing in tense differ thereby in the category of time, and not in another category. Time a very peculiar feature in the existence of things, but still it is a feature in their existence, and gives rise to a great variety of modifications in their predicates. There is no more reason for reckoning as modal these differences in time, than there is for so reckoning the differences in degree, or in place, to which the existence of a predicate is susceptible in a subject. The plaque raged last year; it is raging now; it is raging here; it is raging in Calcutta. If the placue can exist in different times, so also can it exist in different places; and if judgements do not differ in modality by connecting its existence with different places, neither do they differ in modelity by connecting its existence with different times.

There are a few other distinctions drawn among judgements. which ought to be noticed. We may deal first with a series of antitheses whose force is sometimes too readily considered to be the same: these are analytic and synthetic, essential and accidental. verbal and real.

'In all judgements,' says Kant 1, 'wherein the relation of a subject to the predicate is cogitated (I mention affirmative judgements only here: the application to negative will be very easy), this relation is possible in two different ways. Either the predicate B belongs to the subject A, as somewhat which is contained (though covertly) in the conception A; or the predicate B lies completely out of the conception A, although it stands in connexion with it. In the first instance, I term the judgement analytical, in the second, synthetical. Analytical judgements (affirmative) are therefore those in which the connexion of the predicate with the subject is cogitated through identity 2: those in which this connexion is cogitated without identity, are called synthetical indeements. The former may be called explicative s, the latter augmentative judgements; because the former add in the predicate nothing to the conception of the subject, but only analyse it into its constituent concentions, which were thought already in the subject.

¹ Kritik of Pure Reason, E.T. (Meiklajohn), p. 7.

⁸ In speaking of the connexion between the predicate and subject as cogitated through identity. Kant means that the predicate concept is identical with some part of the subject concept: where it is cogitated without identity, the two concepts are quite distinct. Or ampliative.

although in a confused manner; the latter add to our conception of the subject a predicate which was not contained in it, and which no analysis could ever have discovered therein. Kant's example of an analytic judgement is 'all bodies are extended': for our conception of body is extended substance, and therefore, in order to make the judgement, we need only analyse the conception. 'All bodies are heavy', on the other hand, is a synthetic judgement; for it is not contained in the conception of bodies, that they gravitate towards one another.

Kant's statement of the distinction between analytic and synthetic judgements has been much discussed and criticized. In particular, it has been pointed out, and it is important to recognize, that no judgement is purely analytic: every judgement is a synthesis of distinguishable elements. Let the predicate B of an analytic judgement be contained in the conception of the subject A-extended for example in the conception of body. Suppose the constituent elements of the conception A to be BCD, as those of body are substance and extension. Yet the indeement 'A is B' (all bodies are extended) is not equivalent to the independent 'BCD is B' (all extended substances are extended). The latter does merely repeat in the predicate what is contained in the subject-conception : and inasmuch as the subject-conception has already been exhibited as a synthesis of elements, among which the predicate is one, the judgement only goes over old ground. But the former judgement performs a process of analysis, and does not pick out one element from an analysis already made. Now this difference is important : because in performing an analysis of the subject-conception, we realize at the same time that the predicate must be conjoined with the other constituent elements in the subject, in order to make the subject-conception. 'A is B' means 'to the constitution of A. B must so with CD': all bodies are extended means 'to the constitution of body, extension must go with substantiality'. Kant indeed tells us that until the analytic judgement is made, the predicate B is only covertly contained in the conception A: so that it is really the work of the judgement to recognize B (as an element along with other elements) in the conception A. On the other hand, the synthetic judgement is from one point of view analytic. 'Cats purr'; it is true that I learn this only by experience, and that purring is not otherwise necessary to constitute the

conception of a cat: but to me, who have learnt long ago that cats do purr, purring has become part of my conception of a cat, and when I make this judgement, I am picking out one element in my conception, in order to assert its connexion with the others. Except therefore to some one who knows what cats are, but not what noise they make, and knows what purring is extraneously, the judgement that cats purr is not purely synthetic. And even to him, in the act of making it, it becomes also analytic; for no sooner has he united the predicate 'purr' with his conception of a cat, than it becomes an element selected from among the other elements of his more enlarged conception.

Every judgement then is at once analytic and synthetic; for the act of judgement at once holds different elements spart and recognizes them as elements in a single whole. As held spart, it requires an act of synthesis to see that they make one whole: as recognized to make one whole, it requires an act of analysis to find and hold them apart.

In distinguishing analytic and synthetic judgements, then Kant has not distinguished judgements in which there is only an act of analysis from those in which there is only an act of synthesis. What he has really done is to distinguish those in which the predicate is part of the definition of the subject from those in which it is not. For he really had in his mind only judgements whose subject is general, or at any rate if his distinction can be applied to singular judgements, it is only so far as a particular thing is designated in the subject by a general term, or concept under which it is brought. 'This body is extended' would be analytic. and 'This body is heavy' synthetic, because the predicates are respectively explicative and augmentative of the concept body. Yet if we look to the particular experience which is the ground of the judgement 'This body is heavy', we shall have to acknowledge that it analyses what is given as a concrete whole; so that although the judgement is synthetic so far as concerns the relation of the predicate to the subject-concept, it is analytic as concerns its relation to the object of perception the body in question. Such judgements have in fact been called in consequence 'analytic judgements of sense', though they are emphatically synthetic in the Kantian sense, as being grounded on the conjunction of manifold elements empirically in an object, and not on a relation between subject and predicate which is necessary for thought, because 'cogitated through identity' and so incapable of being denied without self-contradiction

Now Kant, in drawing the distinction, was interested precisely in the question of the necessity belonging to certain judgements, in virtue of which our thought recognizes them as true without appeal to confirmation from repeated experience. His 'analytic' judgements have this necessity because they are analytic; the problem, be says, is to see how any 'synthetic' judgements can have it. So far as these merely state the conjunction in things of attributes which are distinguished and found together in them, they lack the character of necessity, whether we call them synthetic or analytic'; but he held, and rightly, that there are some judgements in which we do apprehend the necessity of the predication, without the connexion being 'cogritated through identity'. Such are the judgements '5+7=12', or 'Two straight lines cannot enclose a reace'.

A question next arises recording those indocuments in which the predicate is already covertly contained in the subject-concept, and which are therefore incapable of being denied without contradiction. and so concentually necessary: has this come to pass merely by the fact that we have chosen to include certain elements in the subject-concept, which we thereupon cannot consistently deny of it? We saw, in discussing Definition, that we have sometimes to determine arbitrarily what elements are to be included in our definition of a concept : and if this were always the case with definitions, it would appear that Kant's analytic judgements are necessarily true merely because of the meaning which we have given to the subject of them. On the other hand, if the elements in the definition are not arbitrarily selected, but are seen to hang together necessarily in the constitution of the thing defined, then the analytic judgement which predicates of a concept a part of its definition is justified by the same insight into the necessary connexion of distinguishable characters as justifies a synthetic judgement which is not empirical. Let us take an example of a subject in whose definition the elements are arbitrarily 2 put together. In

² Synthetic of elements, or analytic of a whole.
² Arbitrarily, not because there is no motive, but because there is no mocessity.

the Elementary Education Act of 1870, \$ 8, an elementary school is by definition 'a school, or department of a school, at which elementary education is the principal part of the education there given, and does not include any school or department of a school at which the ordinary payments in respect of the instruction, from each scholar, exceed ninenence a week. To say therefore that an elementary school charged less than 10d, per head per week in fees was to make an analytic judgement, from the standpoint of the Education Department in 1870 - but only because it had been arbitrarily settled that none charging 10d, or over should rank as an elementary action, and not because we have such a knowledge of what an elementary school must be as to see that it could not be elementary, and charge a fee so high. Whereas if I say that a figure has sides, that is true not because it is agreed to call nothing a figure which has not, but because I see that lines can be nut together into the unity of, and are required in, a figure.

It follows that some independents ranked by Kant as analytic may involve just the same insight into the necessary connexion of elements in an unity as is found in the class of synthetic judgements which most interested him-viz, those that are grounded not upon repeated experience but upon the apprehension of necessity: while others are true only in virtue of the meaning we have chosen to give to words; neither is any judgement purely analytic or purely synthetic. His distinction therefore is not well expressed by these terms. If, however, we take the terms explicative and augmentative (or ampliative), we may say that all his 'analytic' judgements are explicative of what is already involved in thinking the subject, but we may question whether all his 'synthetic' judgements are ampliative, unless singular judgements, which analyse a present experience, are excluded; nor does the term 'explicative' apply any otherwise to those judgements where the elements in the subject are arbitrarily put together than to those where they constitute a real unity for our thought. Now the former are, as we have seen, true by convention as to the meaning of words, and so they may be called verbal; and to verbal judgements we may oppose as real all whose truth does not rest upon the meaning given to words, but which state something about the nature of things; whether what they state is seen to be necessary -in which case they may be either analytic or synthetic in the

Kantian sense-or rests prop mere experience of fact-in which case Kant would call them synthetic. This does not commit us to the view that all definition is verbal, but only that if a so-called definition does no more than exhitmenly to include cortain elements in a concept, like the definition of 'elementary school' quoted shove, then it is verbal. On the other hand, if we wish to mark the distinction between judgements in which the predicate is part of the definition of the subject, and those in which it is not, we may call the former essential and the latter accidental. The term (essential) may be extended to cover those cases where the definition is arbitrary 1, and some essential independents will then rest merely on the law that forbids self-contradiction . while others will involve the same apprehension of the necessary connexion of elements in an unity as Kant's necessary 'synthetic' judgements : some, that is, will be verbal and others real. The term 'accidental' if 'accident' he taken as hy Aristotle in the phress saft' aird muses note to include what is demonstrable of a kind, will cover all Kant's 'synthetic' judgements, whether they are grounded on an experience which, so far as we can see, might have been otherwise, or on insight into a necessary relation of concepts 2. It will be seen that the three antitheses, of analytic and synthetic, essential and accidental verbal and real cannot really be regarded as equivalent : for neither are they made on the same fundamentum divisionis, nor do they respectively bring together and keep apart the same individual judgements.

Two comparatively unimportant classes of judgements may be mentioned before clearing this chapter—exceptive and excitative judgements. An exceptive judgement is one which excepts from its application a certain part of the extension of the subject. *s. in Clought's satirical vention of the second commandment—"No grave images may be Wornhipped, except the currency." An exclusive

¹ Arbitrary because what we are defining is something of our own institution, or because our so-called definition is a compromise of the nature explained pp. 85-88, super. In the strict sense of definition, none is arbitrary: things are what they are.

¹ 1.e. in Rantian language, whether they are synthetic a posterior or

a priori.

In strictness, of what would otherwise be the subject: as the part excepted cannot be called part of the subject of a judgement which expressly does not apply to it.

indocement is one which confines the application of the predicate to the subject of which it predicates it; as in Elijah's exclamation. 'I, even I only, am left.' It is clear that within a given whole, it makes no difference whether a predicate is affirmed of one part only, or denied of all but that: Only the brane deserve the fair would mean the same as the poet's actual line None but the brave deserve the fair. The scholastic logicians treated these and some other forms of indocement under the head of Exponibilia, i.e. propositions whose full meaning could only be expounded in more independents then one. Thus None but the brave deserve the fair' implies two statements, that the brave deserve the fair, and that those who are not brave do not. The infinite judgement was also an exponible; for if I say that Parliament is not-in-session I imply that it is not in session, and is in some other state instead.

CHAPTER IY

OF THE DISTRIBUTION OF TERMS IN THE JUDGEMENT: AND OF THE OPPOSITION OF JUDGEMENTS

WE saw in the last chapter that all judgements, in respect of their quality were either affirmative or negative; and in respect of quantity, might be treated as either universal or particular. The letter division indeed strictly applies to those indeements only whose subject is a general term, and therefore not to singular indocuments: but for the purposes for which these can be reckoned with universal indocements the division is exhaustive. The nurnoses in question are the determining the distribution of terms, together with what depends on that. A term is said to be distributed, when it is used in reference to its whole extension, or to all that it can denote.1 Now the subject of a singular judgement denotes one individual only, and the judgement refers to that : the subject of an universal indorment is general, and may denote any number of individuals. but since the indocement is universal, it applies to them all. Therefore in both singular and universal judgements, all that the subject can denote is referred to, or, in other words, the subject is distributed : and, in considering the distribution of terms in a judgement, we may accordingly rank the singular with the universal.

As every judgement must have both quantity and quality, and in each respect there are two alternatives open, there are four varieties of judgement in respect of these two characters combined. An affirmative judgement may be universal or particular: a negative judgement may be universal or particular. It is customary in

We have already sear, in discussing the extension, or denotation, of terms, that confinion may arise between the relation of a generic concept to the more specific concepts included under it and the relation of the universal to the individual. But in considering the distribution of terms, it is not always necessary to bear in mind this distinction. I may therefore any indifferently that a term is used with reference to its whole attaction, or to all that it can denote, even if we reserve the latter expression (denotation) to signify the individuals of which a term can be preficiated.

Logic to indicate these four forms of judgement by the first four vowels thus -

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an universal affirmative independent is indicated by the letter A:
an universal persative
                                                              R.
                                                              7:
a particular affirmative
a particular negative
                                                               'n
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Thus the affirmative judgements are A (universal) and I (particular): the negative judgements are E (universal) and O (particular); and this may be remembered by noting that A and I, which indicate the universal and particular affirmative advements, are the first two vowels in the verb 'affirmo': E and O, which indicate the universal and particular negative judgements, the vowels in the verb 'nem'

All universal judgements (A and E) distribute their subject; all negative judgements (E and O) distribute their predicate. No particular indoments (I and O) distribute their subject: no affirmative judgements (A and I) distribute their predicate. Thus :-

```
in A, the subject is distributed, the predicate undistributed;
in # . .
                 ., distributed. ..
                                                   distributed :
             ..
in I, ,,
                                                undistributed :
                 .. undistributed. ..
                                                   distributed
                 ., undistributed, ...
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It is important to understand and become familiar with these characteristics of a judgement.

A term, as was explained just now, is said to be distributed when it is used with reference to all that it can denote ! The term 'book' is distributed, when used in a proposition that refers to all books: undistributed, when used in a proposition that does not refer to all books. It is obvious that an universal proposition about books (whether affirmative or negative) refers to all : and that a particular proposition does not: all books are written before being printed: no book was printed before 14502; some books are published unseron: some books are never published. That the subject of universal propositions is distributed, and of particular propositions undistributed.

JOSEPH

¹ i.e. denote univocally : an equivocal term is to be regarded as a different

term in each sense.

The reconsition must be taken to refer to European books and movable type: the first dated examples being of 1454.

needs no further illustration. Two cautions, however, may be offered.

- 1. The subject of a proposition is the whole subject-term; if I say all modern books are printed from manable tune the subject in not backs but maders backs: it is true that my judgement does not refer to all books but it refers to all modern books and so the subject is still distributed while it is undistributed in the proposition some modern backs are printed from stereotone platen. But. I may restrict a general term like book not by words which leave it still general (e. g. modern book book printed by Elsenir in Lenden). and therefore canable of being either distributed or undistributed. but by a demonstrative pronoun, or other words which destroy its pemerality (e. p. that book these books the first book which I ever possessed. In the latter case, the term becomes a designation, and is therefore singular, or (like 'these books ') a collection of singulars : and the proposition should rank with universals. But the coneral term which is restricted, by a demonstrative or otherwise, to the designation of a particular individual, is not distributed, since it does not refer to all that it can denote. 'Book' therefore is undistributed, but 'this book' is distributed, in the proposition 'This book wants rebinding': for 'book' might be used of other books, but 'this book' is already used of the only book of which, so long as I mean the same by 'this', it can be used.
- 2. În speaking of the distribution of terms, we are insvitably led to view judgements in extension rather than intension: and indeed as referring (ultimately) to so many sadividual objects, rather than asserting a connexion between universals. Now we have seen that a judgement may refer to individuals, but need not; and that in a judgement properly universal, there is no particular thought of individuals. In saying that a triangle has its angles equal to two right angles, I am not referring to all the particular triangles that have ever existed or may exist; I am thinking of their common character as triangles, which being one and the same in them all may be spoken of in the singular number. It may therefore appear erroneous to say that such a judgement distributes its subject, if to distribute a term is to use it with reference to all that it can denote; for to the individuals which the term triangle.
- ¹ I do not deny that a particular 'representative' triangle must be conceived in making the judgement.

can denote I am not referring. But it is true in this sense, that whatever particular triangle you choose to take, my judgement holds good of that. We must avoid supposing that in every universal judgement we are thinking of all the different individuals of which the subject-term is predicable; but we must recognize that our judgement holds of them all.

The distribution of the predicate in a judgement is not generally so readily understood as that of the subject; for the extension of the predicate is not naturally before us. The rule is that negative propositions distribute their predicate; affirmative do not: and this equally whether they are universal or particular.

All preachers praise pirtue: some practise it. It is easy to see here that I refer in one case to all and in the other only to part of what the term preacher can denote. The subject therefore is distributed in one case, and not in the other. But what of the predicate? That is not distributed or undistributed because it refers to all or only some preachers: for a term is only distributed or undistributed when it is used in reference to the whole or to a part only of its own extension, not of the extension of the subject of which it is predicated. Now the extension of the terms 'praiser of virtue' and 'practiser of virtue' includes everything which can be said to praise or practise virtue. Preschers may do so but so may others who are not preachers; these also are therefore included in the extension of the predicate; but what is thus included is not predicated of preachers. In the judgement X is Y, I predicate Y of X: but I might predicate it also of Z; X and Z are both included in the extension of Y, or in what Y can denote; but when I affirm Y. I do not affirm it in its whole extension; for then in saying 'X is I', I should mean that it is X and Z, and in saying 'Z is I', I should mean that it is Z and X. The predicate therefore is not used in reference to its whole extension, i. e. is undistributed.

The predicate of an affirmative judgement in fact cannot be thought in extension at all. The subject of which it is predicated forms part of its extension; but in the predicate, as opposed to the subject, I am thinking of a character or attribute belonging to that subject. A great deal of the difficulty which hange about the doctrine of the distribution of terms arises from the fact that a term is said to be undistributed both when it is used with applict reference to a part only of its extension, and whom it is used

without explicit reference to its extension at all. The subject of a particular judgement is undistributed in the former sense: when I say that Some preachers practice pirtue. I am explicitly confining my statement to a part of the extension of the term associar. The predicate of an affirmative indepenent is undistributed in the latter sense. When I say that All preachers praise pirtue, though it is true that preachers, even all of them, are only part of the extension of the predicate, yet I am not thinking in the predicate of its extension but of its intension. The extension of a term consists of all the alternative enecies, or different individuals in which it is manifested. It is impossible to predicate alternative species of the same subject. or to say of anything that it is so many different individuals. 'An ellipse is a conic section.' The extension of the predicate cosic section is hyperbola, parabola, and ellipse: I cannot say that an ellipse is all of these. I do not want to say that it is an ellipse: I am thinking of the common character in them all, i.e. using the predicate in intension. Still, it is only part of the extension of the predicate which is referred to in this indocument, and therefore the term is said to be undistributed in the judgement, though in the predicate extension is not considered at all.

In a negative judgement, on the other hand, the predicate is mecessarily denied in its whole extension. Caesar is not ambitions; there are a thousand forms of ambition among mankind; but if I deny ambition of Caesar, I deny all these. It is the same whether the judgement is universal or particular. No Messelmans four death. Whether we look to the forms which fearing death may take, or to the individuals in whom it is exhibited, if I deny the predicate of Mussulmans, I deny all forms of it, or deny that they are any of those individuals in whom it is exhibited. But again, Some maries aximals are not certebrate; of those animals I do not merely dany that they are any place or almon, all of which form part of the extension of vertebrates vertebration in every form is denied of them; a negative judgement denies its predicate in tota.

In an affirmative judgement, the subject is necessarily part of the extension of the predicate; in a negative judgement it is as necessarily no part thereof. And to say that the subject is no part of the extension of the predicate is to say that the predicate is denied in its whole extension. But here again it is primarily the intension of the predicate which is in my mind. When I say that 'Brutus is an honourable man', the only individual referred to is Brutus, though 'they are all honourable men that have slain Caesar'; when I say 'Caesar was not ambitions', I need not be thinking of any one who was. It is an attribute which I affirm in one case and deny in the other. Nevertheless, whereas if I do attend in affirmatic judgements to the extension of the predicate I cannot affirm the whole, and do not want to affirm the only part—viz. the subject of the same judgement—which I can affirm, in a negative judgement, if I attend to the extension of the subject, I can depy the whole 'A cycloid is not a conic section'; if I remember that conic section includes hyperbola, parabola, and ellipse, I can say that a cycloid is neither an hyperbola nor a parabola nor an ellipse.

We are not thinking primarily of the extension of the predicate in a negative judgement; but if we do think of it, we must deny it is toto, or else our judgement will not mean what we intend it to mean; therefore the predicate is distributed. 'The Tenth don' dance'; we are not thinking of those who do; but bears dance, and so are part of the extension of the predicate, and if the predicate were not denied in its whole extension, it would be compatible with the truth of that proposition to say that the Tenth were bears; or if the predicate were used only in reference to the ursine portion of its extension, the proposition would mean no more than that the Tenth were not bear.

[Sometimes the device of circles, representing the extension of the subject and the predicate, is used in order to explain the distribution of terms. Collect the mammals in one

circle, and the enakes in another: then if no enakes are mammals, enakes will lie outside the whole mammal-ares: and if some vertebrates are not mammals, some part of the vertebratearea will lie outside the whole mammal-ares; whereas if some vertebrates are mammals, some



part of the vertebrate-area will coincide either with the whole or with a part only of the mammal-area; and if all mammals are vertebrates, the mammal-area will fall completely within the vertebrate-area. But all the objections which lie against representing in this figurate way the logical relation of a larger to a smaller class within it lie equally against so representing the distribution of terms. We may say that the negative proposition Fanakes are not mammals excludes snakes from the whole class of mammals, and not merely from a portion of it (say men); but we must not think of the class as an area cut up into districts called species or as a collection of which the species are component erouns.l

Any one who realizes that the predicate of a proposition is not thought in extension will see that there can be no truth in the doctrine of the Quantification of the Predicate. But the doctrine has the support of distinguished writers, among others of Sir William Hamilton who invented it, and of Stanley Jevons; and it ought perhaps to be examined here. It may be easily shown to be false; and the conscientious student haply stumbling upon the mass of intricate technicalities based upon it may be glad to feel excused from the labour of mastering them by the knowledge that they are built upon a worthless foundation.

By quantification of the predicate is meant affixing a mark of quantity to the predicate as well as the subject of a judgement. Thus instead of the four forms of judgement, A. E. I. O. we get eight, as follows :-

- U. All X is all Y. All organisms are all mortals.
 A. All X is some Y. All men are some mortals.
 Y. Some X is all Y. Some mortals are all men.

- / Some X is some Y. Some men are some (things) fleet of foot.
- E. No X is any Y. No snakes are any mammals.
- n. No X is some Y. No men are some mammals [e.g. not monkeys).
- O. Some X is no Y. Some vertebrates are not any mammals. ... Some X is not some Y. Some mammals are not some vertebrates [e.g. not cows].

In defence of this mode of stating propositions it is urged that as the proposition whose predicate has all before it, and the corresponding proposition whose predicate has some before it, do not mean the same thing, and we must know which we mean when we judge, we ought to express it. It is strange, if that is the case, that no language ever has expressed it; and it may be confidently asserted that none of these eight forms of proposition expresses anything that we ever really mean when we make a judgement (though some express, in 'portmanteau' fashion, what we mean when we make two judgements); and that the reason why we ought not to express in our proposition whether we mean all or some before the predicate, is that we mean neither.

Let us take an A proposition. It used to be stated 'All X is Y';

[we are told to state it 'All X is some Y'. All were are some sortals: which mortals are they? the horse? 'the greas of the field? clearly not, but only the men. Yet it can hardly be meant by the proposition, that all men are men; it is something about men that the proposition tells us. What about them? that they die, and not which kind they are among the kinds of things which die; we know that they are men already, and that need not be receased in the predicate.

But there is a difference between saying that all men are all mortals, and saying that all men are some mortals; the first implies that the terms are commensurate, that there are no mortals but must be seen as a second that men are mortal, but an undetermined range of objects (cate and dogs and horses and assess and what not) are so basides. Quelth not this difference to be excessed?

Doubless, but it requires another proposition: All was are wortals—some mortals are not was. In recognizing that men die, we do not judge that any other kind dies; and though we may be swares of it when we say that men die, it is no part of the judgement was die. There is much that we are aware of when we judge that men die, besides the content of that judgement—that the sun is shining, for example, or our feet aching; yet nhoody would suppose this to be included in that judgement, merely because we are aware of it in making the judgement. Here is no more reason to suppose the fact that other creatures besides men die to be included in the judgement. Hil sees are word, because we are aware of it in making the judgement. All sees are some mortals is not no judgement, but a 'portunateau' proposition—two judgementae to proposition—two judgements expressed in what (in respect of its grammatical form) is one sentence.

It is true that in some judgements we expressly think the predicate and the subject to be commensurate. In a definition, we must do this. Momentum is the product of mass into velocity: weaths it that which has evalue in acchange; in these cases, it is included in our thought that the product of mass into velocity is momentum, or that which has value in acchange, wallsh. But such judgements are ill expressed in the form "All X is all Y". We do not think of all moments, all samples of wealth, but of wealth and momentum each as one thing. Again, the formula "All X is all Y" makes us think of X and Y as different things: whereas the whole force of a definition is to assert that the subject and predicate, the thing defined and the definition of it, are the same thing.

There are propositions whose terms are known to be commensurate, but which are not definitions, such as all equilateral triangles are equiumquiar. These also we are told to represent in the form 'All X is all Y', and to say that all equilateral are all equiumquiar triangles. But this does not correctly express the true meaning of

[the other proposition. For granted that in enunciating it we are warse that the terms are commensurate: what we wish to assert is the mutual implication of two attributes in the triangle. It follows from this that every triangle exhibiting one exhibits the other; but those which exhibit one are not a different set of triangles from those that exhibit the other. By putting a mark of quantity before the predicate as well as before the subject, we make it appear as if the extension of one term was affirmed of the extension of the other, and (if we consider individuals) as if the individuals can be cheese the control of the other of the consider individuals as if the category of the consider individuals as if the category of the consider individuals as if the individuals can different, or tastelogous, if they are the same.

"All' can be no part of any predicate, except where (as in these red lt the spoults) the subject is collective. If the universal judgement 'All kiving things reproduce their kind' is true, then it is true of any living things and therefore of peas. I may introduce 'perfectly' into the predicate, and then it will be true that peas reproduce their kind perfectly. But I cannot introduce 'all' into the predicate their kind, peas would be all things that reproduce their kind, peas would be all things that reproduce their kind; and that is nonsense. The predicate of a judgement is affirmed distributively of each that falls under the subject; the predicate quantified by all could be only true of the subject; collectively. No equilateral triangle is all equiangular triangles; how then can they all be? The proposition only meass that all equilateral triangles are equiangular and sice error. As before, it is a 'portmantear' proposition, and not a single judgement.

The U form of proposition has been considered at some length, because it is in a way the most plausible member of the series. Universal judgements whose terms are commensurate do differ from those whose terms are not, and do form a very important class of judgements, and there is no special recognition of them in the ordinary fourfold classification of judgements (A, E, I, and O). It has been wrongly alleged that Aristotle ignored such judgements; on the contrary, he recognized their great importance in science. To remedy this supposed omission the doctrine of the quantification of the predicate offers us an entirely false analysis of them, and one which Aristotle himself exposed. The analysis overlooks altogether the

De Interp. vii. 17º 12 del là val aurypopulation addion terrepopulation desidone dei terre addion desimble addione des terre addion des terre addion des terre addion des terre addion des terres addion des addion aurypopulation, des fers ses depunces ses épopulations addion aurypopulation, des fers ses depunces ses épopulations de la company de la com

[intension of terms. Professing to complete what is defective in the current recognition of different kinds of proposition, it leaves important differences itself unrecognized. We have seen that a proposition of the form 'All X is ' represents two kinds of judgment: essentially different in thought, according as it is really universal, meaning 'X as we his is 'N or only summerative, meaning 'All the X's are Y'. Of this difference, whether in universal judgments whose terms are commensurate (I) or not (A), this doctrine takes no note; but sets up instead two kinds which misrepresent our thought by the sign of caustive prefixed to the neclicate.

The particular affirmative propositions may be dismissed briefly. We are told that 'Some X is I' should be written either 'Some X is some Y' or 'Some X is all Y'. Take the former. 'Some X is some Y': we ask immediately, which X are which Y?; and the only answer is that the X that are Y are the Y that are X. Some somers sean : if that means some somers are some seaners this can only mean that the sowers who rean are the reaners who sow. Take the latter. 'Some X are all Y'; some animals are all the pigs (for it does not mean, are all of them pigs; as we might say that some families all squint, meaning that all the members of some families squint). Which animals are all the pigs? surely only the pigs themselves. If it be said that the proposition means that there are more animals than pigs, then the real subject of the judgement is the other animals (which are not pigs), and not (as this form pretends) the animals which are pigs. If, again, it be said to mean that all pigs are animals and some animals are not pige, then as before we have two judgements packed into one sentence. What is one judgement. and what is the character of a judgement, are questions to be deter-mined by considering our thought, and not the verbal devices we adopt to express it. To think that all pige are animals, and some animals are not pigs, is to judge not once but twice, even though we were to write such a pair of judgements in the form some animals are

To the negative judgement also the quantification of the predicate does violence. The universal negative is to appear in the two forms 'No X is any Y'(E) and 'No X is some $Y'(\eta)$. The former may stand; for as we have seen, if X is not X, it is not any

affirmation is true whom universality (in extension) is usigned to the predicated universal, ag. All men aw all animals. Of Ammonius in loc. 182 who points cut that then each man would be all animals.) Assal. Fri. a. 1111. 439 T. aris 30 it is despined to Averice 30 in Streets, key at 50 is despined with Control of the Article 182 in Streets, and the Article 182 in Streets, and the Article 182 in Streets, and the Article 182 in Streets and Streets, of the variety and streets of the Article 182 in Streets, and the Article 182 in Streets and Streets, of the variety and the Article 182 in Streets and the Article 182 in Arti

Cose or kind of Y The latter may well muzzle us. It denies of X some part of the extension of Y; pig, for example, is part of the extension of animal, and sheep are not pigs; hence sheep are not some animals . but this is quite consistent with their being animals. 'No X is some Y' is therefore consistent with 'All X are Y' and what it means is that 'Some Y are not Y'. whether any Y are Y or not it leaves doubtful. There remain the particular negatives. 'Some X is not any Y', and 'Some X is not some Y'. Again the former will stand: but what does the latter mean? It does not mean that some X is not Y at all e o that some animals are not pies at all, but are something quite different (say sheep or cows) : for that is expressed by the form 'Some X are not any Y'. It can only mean that there are some Y's distinct from some X's. i.e. that though some X may be Y, they are not every Y. 'Some murderers are not caught' is sense : but 'Some murderers are not some caught'. if sense at all, is only true because fish and cricket-balls are also caught, and some murderers are not these; so that if the proposition were to be false, they would have to be fish and cricket-balls and everything else that is ever caught; it is the contradictory of the impossible judgement 'Some X is all Y'. But as we never make that judgement, we never want to contradict it : yet these are forms of judgement which those who would quantify the predicate condemn Logic for hitherto ignoring

Thus all the eight forms of proposition with quantified predicate have been found vicious, except \$\$ and \$0\$; and these are so interpreted as to lay undue stress on the sapect of extension in the predicate. The truth is that if we prefix to the predicate of a proposition a mark of quantity, \$all or some, we are bound to think of the various individuals (or species) characterized by the predicate, not merely of the character, or 'universal': we are bound to take the predicate in extension, and that we cannot really do. We cannot predicate in extension, and that we cannot really do. We cannot predicate in extension of one term the extension of another. If a set of individuals, or of species, forms the subject of a judgement, another set cannot form the predicate. 'All X is some Y is meaningless. 'Some Y,' we are told, means 'part of the class Y;' but which part is X' Let the class Y be divided into two parts, X and Z; we do not need to say that X is the former part; it is false to say that it is the latter.

We might make them a present of certain forms which they appear to have orerlooked. If the extension of Y be p, q, r, then 'No X is any Y' wears 'No X is either p or q or ". But the parts of the extension are taken disjunctively: why should they not be taken together? Them we should have the form 'No X is all Y remeaning that no X is both p and q and r. So we might have 'Some X are not all Y'. It is true these forms are notices: and in that they remembe the affirmative forms' all X are all Y and 'Soms X are all Y'. But they have the advantage over those of being true. Of p. 204, a.1.

[Still it is proved the judgement compares the extension of two classes. 'All X is all Y' means that the class X and the class Y are co-extensive . 'All Y is some F' means that the class Y is included in the class Y which extends beyond it. But if the class X and the class Y are co-extensive how are they two classes? Taken strictly in extension (as the doctrine of the quantification of the predicate takes its terms) the class X and the class Y are not the common character X and Y realized in many things, but the set of things in which this character is realized. If the class X is the things in which the common character X is realized, and Y is realized in the same things, then there is only one class or set of things, and no comparison between two classes : so that, after all, we have the class I and predicate the character Y of them, i.e. we do not take Y in extension. And if the class X is included in the class Y, what does that mean? Suppose that all I's were collected in one place. all I's would be found in the crowd : then when we said that all I is some I, we should mean that all X were included in the crowd of I's. But now our predicate is no longer Y, and has become included in the crowd of I's'. We must quantify that if all predicates are to be quantified and state whether all or part of what is included in the crowd of I's be meant. Clearly part: so that our judgement will run 'All X are some things included in the class Y (or crowd of I's)'. But which things so included are they? as before themselves, the X's. If this answer be not accepted, and it be said that some means 'included in the class of ', then our new judgement must run 'All X are included in the class of things included in the class I'. But now the last eleven words become the predicate, and it must again be quantified; we must say 'All X are some things included in the class of things included in the class Y'. So the process goes on ad infinitum. You cannot predicate of one class the whole or part of another. You may compare the extension of two classes: e.g. when we say that male infants are more numerous than female: but then one class is not predicated of another: female infants do not include male infants and extend beyond them. You may predicate a genus of a species, and the genus as compared with the species has a wider extension; but it is not the extension of the genus which you predicate of the species, nor any part of it.

It may be thought that in discussing the quantification of the predicate we have been belabouring errors too trivial for notice. No one, of course, really supposes that the act of judgement means any of these absurdities. But many people have supposed that a judgement compares the extension of two terms, or includes a subject in or excludes it from a clase; and they think of a clase as an examp things or kinds of thing. Such views imply the absurdities that have been danged to light; and the custom of elucidating the relation of terms in a judgement by the relative position of circles on paper,

[outside each other, one inside the other, or with a common segment, tends, as has been said before, to make us think wrongly about a judgement precisely in the direction of these absurdities. It is of great importance, is speaking of the distribution of trams (as we shall have to do frequently when examining the syllogism), not to suppose that the terms of a judgement are all taken in extension, and that we are always identifying and distinguishing all or part of what our terms denote. The doctrine of the quantification of the predicate flourishes upon this mistake, and a thorough examination of that doctrine is a road ourselvation.

Archbishop Thomson (Lause of Thought, pp. 187-188), though not contesting the doctrine of the quantification of the predicate, axcludes the forms of proposition n and w (No X is some X; Some X is not some Y') on the ground that though conceivable they are not actual cause of negative predication. 'It is not inconceivable that a man should say "No birds are predication. It is not inconcentrate that a man another as some animals" (the 7 of the Table), and yet such a judgement is never actually made, because it has the semblance only, and not the power, of a denial. True though it is, it does not prevent our making another of a denial. True though it is, it does not prevent our making another judgment of the affirmative kind, from the same tarms; and "All birds are animals" is also true. Though such a negative judgment is conceivable, it is necless; and feeling this, men in their daily conversation, as well as logicians in their treatises, have prescribed it.—But the fruitlessness of a negative judgement where both terms are particular is even more manifest; for "Some X is not some Y" is true, whatever terms X and Y stand for, and for "Some X is not some Y" is true, whistever terms X and Y stand for, and therefore the judgmennt, as presupposed in every case, in not worth the form of the present the present the present the present the present of common salt by saying "Common salt is othered so dodium", I cannot prevent another saying that. "Some common salt is not some colloride of sodium", because he may mean that the common salt in this salt-collar is not the chloride of sodium in that. A judgmenn of this sort is sperious upon two grounds; it denies nothing, because it does not prevent any of the modes of affirmation; it decides nothing, inasmuch as its truth is presuposed with reference to any pair of conceptions whatever. In a list of possed with recerence to any pair of conceptions wanterer. In a list of conceivable modes of predication, these two are entitled to a place. In this passage, the ridiculous nature of η and ω is excellently shown; and the observation that they have the semblance only and not the power of a denial is very just. But how then can they be negative judgements? A negative judgement is an act of thought that denies, not a sentence that looks negative on paper. It may be noticed that not only can we say 'Some salt is not some chloride of sodium', but with equal truth 'Some salt is not some salt'. Now that means 'One piece of salt is not another': a perfectly 'conceivable mode of predication'—only, there is no quantification of the predicate in it. It is true that there is a difference for thought between precises in it. In true teat there is a chiefence for knowled entire distinguishing individuals from one another, and desping an attribute of a subject: a difference which escapes in the common symbolic form "X is not Y.". The difference arises through the content; for we cannot think and judge about the relations between individuals as we think and judge. bout the relations between universals, or of attributes to a subject. Hence it is by something of a fiction that we include all possible judgments under four forms A. E. I. and O. the fiction being that singular may be treated as universal. It is well to bear in mind that the form of judgement is really different (although the difference comes through the matter, as was just now stated; for form and matter, we may repeat, are not rigidly We may pass now to the opposition of propositions or judge-

Propositions having the same subject and predicate, but differing in quantity, or quality, or both, are said to be opposed to one another. The four forms of proposition A, E, I, O admit four kinds of conception among them.

- 1. A.—E. Where the propositions differ in quality, and are both universal, they are called contrary to each other: corrything in Aristolle is true are contrary propositions!
- 2. I-O. Where they differ in quality, and both are particular, they are called sub-contrary: e.c. come things
- they are called sub-contrary: e.g. some things in Aristotle are true, some things in Aristotle are not true.
- A—O, E—I. Where they differ both in quantity and quality, they are called contradictory: e.g. everything in Aristotle is true, some things in Aristotle are not true: no



Mussulman fears death, some Mussulmans fear death.

4. A—I, E—O. Where they differ in quantity but not in quality, they are called substarm: a.g. corything in Aristotle is true, some things in Aristotle are true: no Mussulman fears death, some Mussulman do not fear death.

Contrary and contradictory are terms in common use, though sometimes treated as equivalent; the origin of the terms subattern

separated, like a mould and the july in it, so as that the form is the same whether the term are singular or naivesal; yet for certain purpose in the theory of syllogians we need not attend to the difference. But the real variety in the form of our judgements is not recognised by quantifying the precises: a process which, instead of bringing out the true features of thought, distorts and failifies even the commonest judgements in

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and sub-contrary may be seen in the above-given, and ancient, 'diagram of opposition'. I is placed under A, and O under E, for the same reason that in setting out a classification we place the species under the genns: the wider includes the narrower under it: A and T, E and O are called subaltern, because in each pair one is subordinated to the other: I and O are called sub-contrary, because they are subordinated to the contraries A and E, their respective universals.

It will be observed that in order to overthrow an universal proposition, affirmative or negative, it is only necessary to establish the particular negative or affirmative: that everything in Aristotle is true is refuted by showing something in his writings false: that nothing in Aristotle is true, by showing something true. We contradict the affirmation 'All men are liars' by saving 'not all', not by saving 'all not'. But of course the greater includes the less. and we refute a proposition by establishing its contrary, as well as by establishing its contradictory. In common speech therefore we are said to contradict a proposition when we advance another whose truth is inconsistent with that of the first, whether it he the contrary or the contradictory: and since the contrary imputes more error than the contradictory (for if a man tells me that all animals reason. I impute more error to him by replying that none do, than that some don't) it may in a sense be said to contradict more fully. It is, however, convenient to have different words to mark the relation of A and E to each other, and their relations to O and I respectively: and Logic confines the title of contradictory opposition to the latter.

Given the truth or falsity of any proposition, we can see at once which of the opposed propositions must be true, which false, and which (upon the information given us) remain doubtful. For contrary propositions cannot both be true, and therefore if A is given as true, E must be false, and vice verse: but they may both be false (for it is not necessary that either all babies should be disagreeable, or else none of them), and therefore if one is given as false, the other remains doubtful. Contradictory propositions cannot both be true, but neither can they both be false; and therefore if A, E, I, or O is given as true, O, I, E, or A must respectively be false, and vice versa. Subaltern propositions may both be true, or both false, or the particular may be true while

the universal is false; but the particular cannot be false while the universal is true, for the greater includes the less; hence given the truth of A or E, I or O is true, and given the falsity of I or O, A or E is false; but given the falsity of A or E, I or O remains doubtful, and given the truth of I or O, A or E remains doubtful. Sub-contrary propositions cannot both be false (for in that case their respective contradictories, which are contrary to one another, would both be true); but they may both be true, just as contraries may both be false; hence given the falsity of I, O is true, and vice versa; but given the truth of I, O remains doubtful, and vice versa;

Of two contrary or of two contradictory propositions one may be advanced against the other, i.e. we may deny one, and advance the other in its place and of two subaltern propositions, the particular may be advanced against the universal. If any one said 'Some animals reason', we could not answer 'No, but all do'; but if he said, 'All snimals reason', we could answer, 'No, but some do '. Sub-contrary propositions on the other hand, cannot be advanced one against the other. 'Some animals reason': we cannot retort. 'No. but some don't': 'Some animals don't reason': we cannot retort. 'No (i.e. that is false), but some do'. We may indeed, to the statement that some animals reason, reply, 'Yes, but some don't': and to the statement that some animals do not reason. 'Yes, but some do'. In these cases, however, the particular proposition 'Some don't reason', or 'Some do reason', is advanced not against its sub-contrary. 'Some do reason' or 'Some don't reason', but against the universal proposition 'All reason' or 'None reason': which it is feared we might otherwise be supposed to allow, when we admit that some reason, or that some do not. Hence it has been urged that we ought not to speak of sub-contrary propositions as opposed 1, nor include them in a list of the forms of opposition; but if they are not opposed, they are anyhow contrasted, and that may justify their continued inclusion. Given the truth or falsity of any proposition, the step by which we pass to the perception of the truth, falsity or doubtfulness of its several opposites is in the strictest sense formal. It depends in no way

¹ Aristotle notices this in Anal, Pri. β. xv. 68^b 27 το γόρ τενὶ ττὰ οὐ τενὶ κατὰ τὴν λέξω ἀντίκειται μάσαν (* For some are is only verbally opposed to some are not *).

upon the special content of the proposition, but solely upon the necessary relations, according to their quantity and quality, in respect of truth and fallity, between propositions having the same subject and predicate. And since no other information need be given, except whether the one proposition is true or false, in order that we may determine the truth, falsity, or doubtfulness of the remaining three, the process of inference (if inference it is to be called) in immediate.

CHAPTER Y

OF IMMEDIATE INFERENCES

INTERPRETED in a process of thought which starting with one or more judgementa! ends in another judgement made necessary by the former. The latter, which, in relation to the independent or judgements from which the process starts is called a conclusion. must, as compared with them, be a new judgement : to repeat in fresh words our original statement is not inference, any more than translation is inference. For the most part a new judgement is only got by putting together two judgements, and as it were extracting what they yield. But there are a few conclusions which we annear to draw not from any 'nutting together' of two indocements but simply from the relation to one another of the terms in one indepenent. This is called immediate inference, stymologically because (in contrast with syllogism *) it proceeds without the use of a middle term: but, to put it more generally, because we seem to proceed from a given judgement to another, without anything further being required as a means of passing to the conolugion 3

It was mentioned at the end of the last chapter, that when we infer, from the truth or falsity of a given proposition, its various opposites to be true, or false, or doubtful, we perform an act of immediate inference. We have now to consider other forms of immediate inference of which the principal are Conversion. Permutation (or Observiou) and Contraposition.

¹ Or, more generally, elements, if we allow (with Bradley, *Logic*, pp. 870-378) that, e.g., 2+2=4 is inference. But the above is not intended as a final definition of inference.

For the function of the middle term in syllogism, of, safra, c. xi.

All inference is immediate in the sense that from the pre "All interesce is immediate in the sense that from the previous we pass without the help of anything does to the conclusion; but this is called immediate in the sense that from the given relation of two terms in a single proposition. It is doubtful, however, whether, so far as there is any interence in it at all, it is really always immediate, either in this or in the extmological is at all, it is really always immediate, either in this or in the extmological. sense. Cf. the discussion pp. 217 ag.

A proposition is converted, when its subject is made the predicate, and vice versa, its quality (affirmative or negative) remaining unchanged : as, for example, when from 'No true Mussulman cate nork' we need to 'No one who eats nork is a true Museulman' The original proposition is called the connectout and the new proposition its converse.

Whether and in what way, a proposition can be converted. depends on its form. A. R. I. or Q1: because the process of conversion is invalid, unless it conforms to the following rule, that no term may be distributed in the converse, which was not distributed in the connected. An A proposition is converted by limitation: an E or an I proposition simply: and an O proposition not at all except. through first permuting it.

A proposition is said to be converted simuly, when the quantity of the converse is the same with that of the convertend. In an universal negative proposition (E) both terms are distributed . in a particular affirmative proposition (I) both are undistributed. Therefore their mutual substitution in the process of simple conversion does not distribute any term that was not distributed before. Thus E. no X is Y, becomes E, no Y is X; e.g. 'no lawyers are parsons'-'no parsons are lawyers': 'no true poet admires Macanlay's Lava' - 'no one who admires Macanlay's Lava is a true poet " ; ' no snakes suckle their young '- no mammals are snakes ': 'Chatham is not the younger Pitt'-'the younger Pitt is not Chatham '.

Again, I, some Y is X, becomes I, some X is Y: e.g. some dismonds are black '-- 'some black stones are diamonds': 'some ever-

The matter of some judgements renders their conversion unnatural, even where the form allows of it: e.g. Civilization spreads by the extermination of lower races. Cf. pp. 218, in fro.

Another rule for conversion is sometimes given, to the effect that the terms (or the subject and predicate) of the converse must be the same as the corms or tan suspect and predicate of the converse must be the same as the terms for the predicate and subject of the convertend. But this is not a to the same that the converting of the predicate and subject of the converted of the same than the converting of the same than the converting of the converting the convertin

tival term, we must either substitute for it in the converse a substantive, if tival term, we muse either substitute for it in the converse a substantive, in there be one of equivalent meaning (as in this case), or import some sub-stantival expression like 'one who '(as in the previous example; for the original predicate, now introduced into the subject, to qualify. We often choose the granu of the subject about which we are speaking, as in the first example of the conversion of I.

green shrubs flower brilliantly'—'some brilliant flowering shrubs are evergreen'; 'some victories are more fatal than defeat'—
'some events more fatal than defeat are victories'.

A proposition is said to be converted by limitation or per accident, when it being universal its converse is particular. In an universal affirmative proposition Y is predicated of all X: but it may attach to other subjects cously, P. O. and R: therefore what is Y need not be X, and we can only say that some Y is X, not that all I is X. To use the language of distribution, the subject is distributed, the predicate not: if we merely substituted each for the other, the original predicate, become the subject of an universal proposition, would be distributed . for 'all roses are deciduous' we should have 'everything deciduous is a rose'. We must therefore limit the extent to which we affirm our original subject rose of our original predicate decidnous: and hence such conversion is called 'conversion by limitation'. So A. all X is Y. becomes L. some Y is X: 'all men are mortal'-'some mortals are men': 'all Roman priests are celibate '- 'some celibates are Roman priests': 'all isosceles triangles have equal angles at the base '-- 'some triangles with equal angles at the base are isosceles '.1

In the last example, any one who knows geometry will be tempted to convert simpliciter, and say that all triangles with equal angles at the base are isosceles. He would not be wrong as a geometrician; but he would need a knowledge of geometry, and not merely of logic, to justify him. In conversion, we look solely / to what is justified by the form of the proposition to be converted, be it A. E. I. or O; in this respect 'all isosceles triangles have equal angles at the base' is indistinguishable from 'all isosceles triangles have angles equal to two right angles': the geometrician knows that it does not follow from the latter, that all triangles having angles equal to two right angles are isosceles; neither therefore does it follow looically from the former, that all triangles having equal angles at the base are isosceles. The form of proposition 'all X is Y' only instifies a conversion to 'some Y is X': in order to convert to 'all Y is X' we must know that X and Y necessitate each other, or that there is nothing accidental in the relation between them; this is not implied merely in the one being predicable of the other, because the relation of a predicate to its subject

With this paragraph, cf. supra, pp. 199, 200.

may be either accidental or essential. It must at the least be accidental, and therefore from its bare form, we are entitled to constant A proposition as if Y were an accident of X_i but we are not entitled to do more. For this reason, conversion by limitation is enalled conversion per accident (axrd $evuple\betanch()$); if Y is an accident of X_i i. a coincides in the same individual subject with X_i then X is predicable of a subject which Y characterizes, and we may say that some Y in X_i !

In a particular populive proposition (O) the subject is undistributed the predicate distributed if here we substituted each for the other the original enhiert, become the predicate of a negative proposition would be distributed in the converse. And since the predicate of a negative judgement cannot, like the subject of a indowment, he limited by a gion of 'particular' quantity, an O proposition is not convertible, except by negation: a process which will be explained later (p. 215). This is not always realized, when we use symbols, and forbid the passage from 'some X is not Y' to 'some Y is not X': for it is quite possible that both of these propositions may be true at once : e. g. some freemasons are not freethinkers ". and some freethinkers are not freemasons. But although 'some X is not Y' and 'some Y is not X' may be true at once, yet we are not instified by the form of the one in passing to the other: and this becomes obvious by comparing such an example as the last (where both propositions are true) with another, where the converse is manifestly false: e.g. 'some men are not monks'-'some monks are not men'. In form the two propositions ('some freemasons are not freethinkers ' and ' some men are not monks ') are

I Even when the predicate is known to be of the essence of the subject we made convert per accident, if the predicate is the genus : a, "all men are animals"—"some animals are men". We cannot call animal as as men, but we may my that it is an accident for an animal should be a man, in this sense, that the conditions necessary to the generation of an animal sense. that the conditions necessary to the generation of an animal state of the subject of the s

the same; and therefore formally the conversion must be invalid in the former case since it is invalid in the latter.

It is indeed impossible in converting a proposition to treat the terms quite like symbols, and to proceed solely by the consideration of the distribution of the terms in the convertend, without considering what the terms are. In an E proposition, for example if both terms are proper names, the act of conversion is felt to be different from what it is where the subject is a general concrete term and the predicate attributive : in passing from 'no judge has any right to meddle in politics ' to ' no one who has any right to meddle in politics is a judge, the character of the judgement alters in a way that it does not, when we pass from 'Chatham is not the younger Pitt 'to 'the younger Pitt is not Chatham'. It is not natural to say 'no one who has any right to meddle in politics is a judge': and though it is natural enough to say 'no one who meddles in politics has any right to be a judge, this is not the converse of the proposition with which we started. It is equally natural to say 'Chatham is not the vounger Pitt' and 'the vounger Pitt is not Chatham ': according as we are discoursing about the one or the other: for two individuals stand as it were on the same level in thought, and each may indifferently be distinguished from either. But our rights depend upon our position, and not vice versa: so that it is natural to denv certain rights to a man filling a certain position, but not to deny the position to a man possessed of those rights. Other examples of the same thing might be given. A proposition both whose terms are singular is called an A proposition, but it cannot be converted per accident: 'Chatham is the elder Pitt' can only become 'the elder Pitt is Chatham'. If the subject is and the predicate is not a singular term, conversion is a form without meaning: 'Chatham was eloquent' becomes 'an eloonent man was Chatham ', and however we may write it, the latter means just the same as the former : we cannot predicate Chatham of 'an eloquent man', for this is a general term, and that a singular. Again, ' Demosthenes and Cicero were the greatest orators of antiquity becomes 'the greatest orators of antiquity were Demosthenes and Cicero': we cannot say 'some greatest orators of antiquity were Demosthenes and Cicero' without altering the force of the term 'greatest orators' from comparative to positive. 'Some men are Christians' is a proper, 'some Christians are men' an improper mode of speech; religion can belong only to men, and we do not predicate of an attribute partially the subject presupposed by it. A difficulty arises again in a proposition not universal where some measure is given of the extent to which the predicate characterizes the subject, e.g. by using such words as 'many' or 'few'; 'must great men have been of obscure origin' converts to 'some men of obscure origin have been most great men'; but no one would ever say this, for the measure 'most' applies to 'great men' as taken in extencion and therefore cannot be medicated of 'unen of obscure origin'.

It would be aband to say that as conversion is a strictly formal process we must therefore convert propositions by its rules, according to their form as A. R. or I. Logic investigates the actual nature and procedure of our thought; and when we find that our thought is not governed by the bare form of a judgement irrespective of its content, it is no use to pretend otherwise. The conversion of propositions may be studied formally, with symbols for terms: but when real terms replace the symbols they must affect the judgement, and our treatment of it in conversion : for example, symbols, like X and Y in the proposition 'no X is Y', are always regarded as general terms, but the actual terms need not be general. This is said, not in order to discredit the abstract and formal treatment of conversion, which is sound within its limits; but in order to emphasize the fact that the form and matter (or the form and content) of thought are not capable of separate consideration, like the mould and the pudding: what from one point of view is form is from another matter, and the same form in different kinds of content is not altogether the same, any more than is the same genus in different species. The importance of this fact must excuse the reiteration of it; meanwhile in a textbook of Logic, as of any other science, we must consider typical cases, with a general caveat that the subject is thereby artificially simplified.

In conversion, the subject and predicate were transposed, but otherwise unaltered, and the quality of the proposition remained the same. In Permutation, or (as it has been also called) Obversion. there is no transposition of terms, but the quality of the pro-

¹ Jevons, in his Elementory Lessons, calls it Immediate Inference by Privative Conception. Earther writers dealt with it under the head of Equipolleary of Propositions: cf. Sanderson, II. 6 'Asquipolleatis communiter sumpta est duarum propositionum, verbo tenus, quoquomodo discrepantium omnimoda in semu compinatio:

position is changed, and the predicate at the same time replaced by its contradictory. It consists in fact of substituting for an affirmative or negative proposition an equivalent negative or affirmative of opposits on suitable by means of neartine the predicate.

prosite quality, by means or negating the predical

- A, All X is Y, becomes E, No X is not-Y: All right angles are equal, No right angles are unequal; Barkis is willin',

 Rarkis is not unwillin'
- E, No X is Y, becomes A, All X is not-Y: No dogs allowed, All does forbidden: Lear is not mad. Lear is not mad.
- Some X is Y, becomes O, Some X is not not Y: Some stretches
 of the road are level, Some stretches of the road have no
 ornalism.
- O, Some X is not Y, becomes I, Some X is not-Y: Some learned theories are not sense, Some learned theories are nonsense;

 Some swans are not white, Some swans are not white.

Further transformation of a given proposition may be effected by a combination of Conversion and Fernutation. The process of permuting and then converting is called Conversion by Megation. The conclusion so obtained may be converted again, and this process of permuting, converting, and permuting is called Contraposition.

All forms of proposition except I can be converted by negation; the process is inapplicable to I, because it becomes O by permutation, and a particular negative, as we have seen, cannot be converted. For the same reason I cannot be contraposed.

In conversion by negation-

- A becomes E: All X is Y .. No X is not-Y .. No not-Y is X. All soids turn blue litmus-paper red .. No saids do not turn blue litmus-paper red .. Nothing that does not turn blue litmus-paper red is an acid.
- B becomes I: No X is Y ... All X is not-Y ... Some not-Y is X.
 No stimulant nourishes ... All stimulants are innutritious,
 ... Some things innutritious are stimulants.
- O becomes I: Some X is not Y .. Some X is not Y .. Some not Y is X. Some sea-animals are not vertebrate .. Some sea-animals are invertebrate .. Some invertebrates are sea-animals. Some things necessary to life have no market.

value ... Some things that have no market-value are neces-

This is the only way in which a particular negative can be

In contraposition 1___

- A becomes A: All X is Y. No not-Y is X. All not-Y is not-X. All Arabs are hospitable .. All who are not-hospitable are not-Arabs.
- E becomes O: No X is Y ... Some not-Y is X ... Some not-Y is not not-X. No unfriendly man is happy ∴ Some who are not happy are not friendly.
- O becomes O: Some X is not Y ∴ Some not-Y is X ∴ Some not-Y is not not-X. Some reformers are not radicals ∴ Some who are not radicals are not not-reformers (are not opposed to reform).

The above processes, when worked in symbols, might be supposed to be equally applicable to all judgements. But when we apply them to concrete examples, we see at once (as with Convention) that it is not so. It is indeed often convenient in discourse to make what was predicated of a subject itself the subject and starting-point in our predication, or to lay stress on the affirmative value of a negative, or the negative value of an affirmative statement. But the use of these processes is limited in part by the idiom and vocabulary of the language, in part by the logical character of the terms in the judgement. The permutation of 1 to 0 looks almost ridiculous in symbolic form; but where there exist two terms, the affirmation of one of which is equivalent to the denial of the other, there the process is in practice perfectly natural. No one would pass from 'Steam is invisible' to 'Steam is not not-invisible'; but he might naturally pass to 'Steam is not visible'.

Contraposition, as involving the largest number of steps, and employing permutation twice may seem to lead to the least natural modes of expression. For permutation introduces 'infinite' terms, not Y and not X; and infinite terms do not ordinarily figure in speech; so that unless we can substitute a term that is not infinite in form, our result seems fantastic. But we may see that

¹ Contraposition has not always been distinguished from conversion by negation: e. g. Wallis, II. 7.

the process of thought involved in contraposition is a common one (although the mode of expression may be awkward) if we look at it from the point of view of hypothetical judgement. Given that all lovers are icalone it is possible to infer that all the not-icalons are not-lovers. No one would however express himself thus. But the original proposition if it is a true universal states a necessary connexion between the predicate and the subject : it involves the proposition that if any one is a lover he is jealous. Therefore if any one is not jealous, he is not a lover; and this is an inference onite naturally expressed. 'If anything is X, it is Y .. if it is not Y, it is not X': we have here precisely the same inference as in the contraposition of A. 'All X is Y .. All not Y is not X.' We may interpret in a corresponding way the contraposition of E and O. if we bear in mind the modal or problematic force which may belong to the particular judgement. 'No X is Y' will mean, 'If a thing is X, it is not Y': from this we cannot, however, infer that if it is not Y it is X: if a man is insufficiently fed, he cannot do a proper day's work : but it does not follow that if he cannot do a proper day's work, he is insufficiently fed; this may or may not be so. Hence we can only infer that 'If a thing is not Y, it may or may not be X': and that is the force of 'Some not-Y is not-X'. regarded as a modal particular. Similarly with 0: 'Some X is not Y' will mean, 'If a thing is X, it may or may not be Y': from which it follows that 'If a thing is not Y, it may or may not he X'.

[The operations whose formal character has been considered in this chapter are called Immediate Inferences; but we have seen that one of them, Permutation, used to be regarded as belonging to the subject of Equipollency of Propositions, and J. S. Müll's in totalone in so regarding them all. In his view we have been dealing merely with equivalent propositional forms; the processes are 'inferences improperly so called'; and indeed they have once or twice been called transformations in the course of the text. Thus conceived, they would belong rather to a study of language than to Logic. We must therefore consider whether there is really any inference involved in them or not.*

We must at the outset bear two things in mind: firstly, that in all inference there must be some moreowers of thought; we must conclude with something not quite the same as what we started with; though the obviousness of the inference is no ground for \$Look. III. 2. * O.R. Bradley* Look, B. III. Pt. I. c. ii, \$50-51. Idenving that it is inference. Secondly, that the same form of proposition, A, E, I, or O, may be diversely intended, and express different judgements, as we have already seen. I, for example, the particular affirmative may be intended to assert the compatibility of attributes, or to make a statement about unnamed individuals. If I say that some cities are episcopal sees. I may either have in mind particular cities not named, say Durham, Winchester, and York, and make my assertion about them : or I may wish to affirm generally that the status of a city and an episcopal see are compatible. In the former case, Durham, Winchester, and York are thought of for their own sake; in the latter, as instances establishing the judgement. We may say that a proposition. taken as making an assertion about individuals, whether these are specified by name, or indicated as some or all of a specified kind, is intended historically; when it is taken as asserting a relation, whether of compatibility or of necessary connexion (or separability or necessary disconnexion) between universals, that it is intended ecientifically. We shall find that the presence of inference. in some of the processes which we have to examine depends on there being a transition from one to the other of these modes of understanding the proposition.

In the conversion of A to I if convertend and converse are both understood historically, or both scientifically, there is no inference. All ruminants part the hoof .. some animals that part the hoof russingle. If by the former statement I mean that various species. which I could enumerate if I had leisure, but prefer to designate as all ruminants (i. e. all she ruminants), part the hoof, then I must know in making it that those cloven-footed species ruminate. The subjects of my thought are cows, stags, and camels, and so forth; I affirm that they part the hoof; but I have recognized that they are all the ruminants, and can be so designated. In the converse, I am still thinking of the same animals; I designate them as cloven-footed, which I previously affirmed them to be: and I affirm that they ruminate, which I had previously recognized. It is true that my former proposition spoke of 'all', and the latter of 'some'; and it might be urged that there is inference in seeing that I am not entitled to say that all cloven-footed animals ruminate. But surely I recognize this from the outset; when I say that all ruminants part the hoof, I know that is not equivalent to saying that all cloven-footed animals ruminate; it can hardly be called inference to refrain from asserting what I know I have no right to assert 1; and it is to be observed that when I assert that some cloven-footed animals ruminate, I do not positively assert that some do not: I merely restrict myself within the limits of what I have a right to assert.

¹ Cf. Bradley, loc, cit.

[Again, scientifically, the convertend asserts that whatever runinates parts the hoof; and the converse, that what parts the hoof may runinate. And I cannot know one property to be necessarily connected with another, without knowing them to be compatible, or capable of coexisting in the same individual. There is therefore on movement of thought, no transition to saything new; in passing from the former proposition to the latter. If, again, the inference be said to be in the limitation, in seeing that the right to infer a cloven foot from runination from a cloven foot, the sarver is as before; this should be known from the outset, and there is no inference in not inferring what you have no right to infer

But now, suppose the proposition 'All X is Y' to be understood historically, and the converse 'Some Y is X' scientifically; them there is inference. If in fact all the runninants do part the hoof, then generally runnination is compatible with a cloven foot. So to tin full, the argument would be that cows, and stage, and camels, and so forth, which runninate, part the hoof, and therefore an animal that parts the hoof may runninate. But the inference is no longer immediate. It is really in the third figure of syllogism.\(^1\)

Similarly if the convertend is understood scientifically and the converse historically: because whatever ruminates parts the hoof, therefore any given animals which ruminate will do so, and they will be animals which exhibit both characters, so that some cloven-footd animals ruminate. This side is inference, but not immediate; for we are applying a general principle to particulars which fall under it. as in the first floure of syllogists.

The simple conversion of I is to be similarly regarded. If 'Some Is I' be intended historically to assert that some things, which are I, are I, then it means also that some things, which are I, are I'. to realist one statement is to realize both, and there is no inference in passing from one to the other. If it be intended cientifically, to mean that I' is compatible with I', then it already means also that I' is compatible with I'. Then it already means also that I' is compatible with I'. But if it be intended near I', are also I', and the converse be intended scientifically, to sasert in general that I' is compatible with I', then there is influence, but it in not immediate. We infer generally that I' may be I, because certain individuals are in fact both I and I'; it is not from one relation between I' and I' that we infer another, but from the relation of both as predicates to the same third term (hose individuals) as subjects, we infer the compatibility between I' and I' themselves. If, however, the converted be intended scientifically, to assert the compatibility of I' with I, I', then the

1 Cf. infra, pp. 284, 257.

00.000

Iconverse as an historical statement does not follow. There is converse as an insured state for War being President of the Board of Trade; the latter office is compatible with the former: but it cannot be inferred that some Presidents of the · lastente Board of Trade have been Secretaries for War. -burgent

With the simple conversion of E the case seems to be different. Sections. Here, if both convertend and converse be taken scientifically, there seems to be inference 'No Y is Y 'No Y is Y' understood scientifically, means, 'If anything is X, it is not Y.' If anything is Y, it is not X? This inference is of the same kind as what we found in the contraposition of A. and shall meet with again in hypothetical reasoning. Again, if both be taken historically, there seems to be the same form of inference. 'No mountain in England is 5,000' high .. No mountain 5,000' high is in England'; I am

not here, as in the conversion of A considering the same individuals as my subject (though starting from a different character in them) in convertend and converse. I realize that if a given mountain 5.000' high (say the Rigi whose height I might know but not its situation) were in England, that would contradict the proposition that no mountain in England is 5.000' high: therefore the Rigi cannot be in England; and this seems to involve hypothetical reasoning. But if the convertend be intended historically, we cannot infer the converse in its scientific intention. Because as a matter of fact 'No X is Y', it does not follow, so far as we can see, that what is Y is necessarily not X. If no Sikh smokes, but this is a mere fact about every Sikh, it does not follow that no smoker could ever be a Sikh. On the other hand, let the convertend be understood scientifically, and the converse historically and there will be inference, for the converse in its historical intention is only reached by first inferring the converse in its scientific intention, and applying the universal principle so obtained to all the actual cases of I': again, however, the convertend, as understood scientifically, fails to assert the existence of any actual

The process of Permutation involves the use of the infinite or negative term not-Y in the predicate in lieu of Y. Now we have seen that an infinite term has not any meaning at all unless it has some positive meaning; not-Y must mean something else than Y.1 We have seen also that the disjunctive judgement ' A is either B or C' does not always imply than it cannot be both. But Permutation rests upon disjunction: Y and not-Y are alternatives, and it is assumed that if Y is affirmed or denied of any subject, not-Y can be denied or affirmed accordingly. Bearing in mind these

¹ Otherwise, the term is Y, and the form not Y only shows that Y is being denied of something in a judgement.

[considerations, we shall find that there is a certain difference in different cases, in respect of the presence of any real inference in permutation, according to the meaning attached to the negative term.

It is unnecessary here to separate universal and particular propositions. If we are told that X is not Y, and Y and not-Y are alternatives, one of which must attach to it, then since it does not exhibit Y, it must exhibit the other, not-Y. We thus reach the affirmative, X is not-Y; and the question is whether that is any way different from the necessitive with which we started.

Now we cannot dony that there is any inference in disjunctive B, therefore it is C, there is clearly inference; and I could not argue that, because A is not B, this C, unless I were given the disjunctive premise, A is either B or C, as well. But in permutation, my alternatives are not two different positive terms, like B and C, but Y and not Y. Is there any inference in saving that

because X is not Y. it is not-Y?

It will be allowed that the conclusion would not hold unless X were either I or not-I. But it may be said that this, the 'principle of Excluded Middle', though true, is not a premise of inference. No one knows what he means in saying that X is not I, unless he sees that in that case it is not-I'. any more than he can know what he means in saying that X is I, unless he sees that in that case it is not not-I'. If a proposition is true, it contradictory is false; but there is no step from the truth of the one to the falsity of the other, no movement of thought; since the truth of the one is not apprehended without apprehending the falsity of the other.

If the infinite term not-I were purely negative, this view of the matter would demand assent. But I are not-I are in practice always alternatives within some definite limits. I may be bise, and then not-I will be of some colour not bise: or I may be English speaking, and not-I speaking some language not English. And in passing from one of these predicates to the other, there is inference, and we do not rely merely on the law of Excluded Middle. 'Noble blood in not blue .' it is not-blue': if this means of a colour not-blue' were require the further permiss that it is either blue or of some other colour. We thus pass from a determinate positive predicate to another predicate less determinate, but all positive.

If however there is no positive alternative meaning in the predicate not-T, then indeed there is no inference, but only equipollency. Steam is not visible. it is invisible' seems a mere substitution of one equivalent expression for another. It follows, that we cannot tall by the mere symbolic form whether the permutation of a negative proposition contains any real inference or not, but must look to Ithe content 1. and if it contains real inference the inference is disjunctive

The permutation of an affirmative proposition may, like this last. be no real process of inference. We ness here from 'X is Y' to 'X is not not-Y'. It is not always possible to find in this any other meaning than that from which we started. We cannot always interpret not. Y to mean ' possessed of some other of the range of alternatives to which I belongs': if a subject must display some one out of a given range of alternatives and does not display Y. it will display one of the others; but if it does display Y, we cannot he sure that it may not display one of the others as well. If a man holds office in the Government and does not hold an office that entitles him to Cabinet rank, he must hold an office that does not entitle him to Cabinet rank: but if he does hold an office that so entitles him, he may also hold one that does not. Equally if not-Y is quite unlimited in range, and includes everything whatever except Y it will not follow that because X is Y it is not also not-Y: because we can predicate of a goose that it hisses, we are not precluded from applying any predicate but hissing. The only sense, therefore in which it is true to say that X is not not-Y, is one in which we deny no alternative, but only deny the denial of Y: and that is just equivalent to the affirmation of Y, or at least can hardly be said to involve any inference from it. If however we have in mind a range of mutually exclusive alternatives among which I is one, then permutation takes us from the affirmation of Y to the denial of the rest: and this is again disjunctive reasoning, wherein the conclusion will be more or less definite according to the definitiveness of our knowledge of the alternatives to Y. But so far as there is inference here, there is no use of an infinite term; where not-Y is really infinite or unlimited. the only sense in which the permutation of an affirmative proposition is logically justifiable is one in which it involves no step of inference §

We have already dealt with Contraposition so far as it can

¹ The reader may be reminded, that among the range of alternatives The reader may be reminded, that among the range of alternatives which the denial of a positive term leaves open, the corresponding pegative term has often come to signify one only. Meddue may cover all designify one only. Meddue may cover all designify one only the contract of the interpretation of the contract of the interpretation of the contract of the interpretation of languages relate than one of Logic.

"This is no doubt why Wullis (cf. p. 216, n. 1, supra) did not distinguish contraposition from conversion to pragation. Hene formulam locate makes document of the contract of t

Aliqued animal non est homo: ergo, Aliqued non-homo non est nea-animal; seu (qued tantundem est) Aliqued non-homo est animal; seu, Aliqued qued non est homo, est tamen animal; loc. cit.

The treated as a mode of inference from hypothetical propositions be treated as a mode of interence from appointment a propositions. It is hardly necessary to deal at length with conversion by negation. The conversion of O by negation is permutation, and then the simple conversion of I. The general result of our investigation is, that from the symbolic form of these processes it cannot be determined whether they contain any real inference or no: that where there is real inference, it is either, as in the conversion of E and the contraposition of A, of the kind that we shall study in dealing with hypothetical arguments; or, as in the permutation of E and O, of the kind that we shall study in dealing with disjunctive arguments: or, as in the conversion of A and I. and that of O by negation, it involves suppressed syllogism. Immediate inferences, therefore, so far as they are inferences, are not a distinct kind of inference; so far as they seem distinct, and specially unquestionable, it is because they merely bring out another aspect of what we have already intended in a proposition, without any fresh step in thought. This result may throw some doubt upon the appropriateness of the name by which they have become known.

The immediate inferences which we have considered so far have all been of a more or less formal character : as is shown by the fact that they have been capable of explanation, up to a point, by using symbols and not real terms. There are certain kinds of inferences which have been called immediate that cannot be exhibited by symbols at all, but only in concreto. One of these is known as Immediate Inference by Added Determinants: in which we add the same qualification to both subject and predicate in a judgement, and hold the result of our operation to be true, on the strength of the truth of the original judgement; e.g. 'A negro is a fellow creature ... a negro in suffering is a fellow creature in suffering '.1 Another is called Immediate Inference by Complex Conception; in which the subject and predicate of a given judgement are used to qualify in some way the same term, and thus complex concepts are formed, that are made subject and predicate of a new judgement, e. g. 'Physics is a science ... physical treatises are scientific treatises'. The following examples, some of them sound and some unsound, but the sound identical in form with the unsound, will serve to show that the ground of the soundness of these arguments does not lie in the form of them :-

¹ Thomson, Love of Thought, 6 55.

The horse is an animal ... the head of a horse is the head of an animal

Horses are animals ... the greater number of horses is the greater

A shark is not a mammal .. the anatomy of a shark is not the

A shark is not a mammal ... the food of a shark is not the food of a mammal.

A shark is not a dog ... the owner of a shark is not the owner of a dog.

It is not worth while multiplying arguments to show how entirely the validity of such inferences as these involves their content. It would not be possible to reduce them to a definite number of fixed types, though in considering generally which are valid, some of Aristotle's observations in the Sonkistici Eleuchi, especially those on what he calls the Fallacy of Accident, would be pertinent. But their mention here will serve to illustrate, what it is well to realize early, that inference is not a purely formal process: that arguments are not all built on the principle of American watches, with interchangeable parts 1, so that terms from one may be transferred to another, without interfering with the working of the inference : and that the study of inference, like the study of life, is largely a matter of examining topes: though there are a certain number of common forms, which recur identically in divers contents. One of the most famous of these common forms is the Syllogism, to which we must now proceed: it has often been regarded as the form of all inference whatever that is not 'immediate': it is indeed highly general, and applicable to all kinds of subject-matter; though the nature even of it cannot be profitably studied altogether in the abstract, but is to some extent affected by the concrete character of its terms.

¹ s. Marshall's Principles of Economics, Bk. IV. c. ix. § 4.

CHAPTER XI

OF STLLOGISM IN GENERAL.

ARISTOTER, who was the first person to work out the theory of syllogism, though not, of course, (as Locke maliciously suggests his followers claimed) the first to reason syllogistically, defines a sullogism as follows: More do a reflorme ruche freede re rain seculous if andreas ovubalves to rate eleast: that is to say. discourse in which certain things being posited, something else than what is posited necessarily follows on their being true '.

This definition is too wide. It covers as the word syllogism in its etymological menification itself covers, every argument in which from a consideration of two truths we infer a third-every argument in which (to use a homely phrase) we 'put two and two together'. and find a certain conclusion necessarily following. But neither by Aristotle, when he investigated in his Prior Analytics the various forms of syllogism, nor by the world, which has followed Aristotle, has the term been actually used so comprehensively. A syllogism is actually an argument in which, from the given relation of two terms, in the way of subject and predicate, to the same third term, there follows necessarily a relation, in the way of subject and predicate, between those two terms themselves."

Example will best explain what is here meant by the words italicized. If A is equal to B, and B is equal to C, then A is equal to C. If a bullet travels faster than a horse, and a horse travels faster than a man, then a bullet travels faster than a man. Now here the terms are A. B. and C: or a bullet, a horse, and a man: but the relations between the terms are in the one case relations of

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^{&#}x27; Anal. Pri. a. i. 24°18: cf. Top. a. i. 100°25, where the same definition recurs, with the substitution of hat via supprise for vi vivio riva.

' Putting two and two together is often a process which leads people to conclusions of a highly conjectural character. In such cases, their reasoning close not come under the Aristotelian definition: for it is expressly stated by him that the conclusion must be inertiable—if designs.

Bradley 2. dept., Br. II. Pr. I. c. i. v. j. 0; of express.

quantity, in the other of velocity. A and B are not related as subject and predicate for I do not say of A that it is B, but only that it is equal (in quantity) to B: a bullet and a horse are not related as enhiest and predicate for a bullet is not a horse, its asserted relation to a horse is in the way of travelling faster not in the way of being a subject whereof horse is a predicate. No doubt it is a predicate of a bullet, that it travels faster than a horse, as it is a predicate of A to be sound to R: but then what I proceed in my argument to compare with C is B itself, and not that which is equal to it: what I say travels faster than a man is a horse, and not what travels faster than a horse. A. B. and C. a bullet, a horse. and a man, are the terms which I compare, the former in respect of quantity the latter of velocity; and from the given relations of A and C to the common term B, in the way of quantity, I deduce a relation between A and C themselves in that respect; or from the given relations of a bullet and a man to a horse in the way of velocity, I deduce a relation in the way of velocity between a bullet and a man.

Now the relations between the terms of an argument may be in the way of subject and predicate; and then the argument is a syllogiam. Let us for the present use the symbols X, Y, and Z to represent terms related in this way. Suppose that X is predicated of Y. and Y of Z: then X must be predicable of Z. For example. silver prints fade in the sun; and the photographs which I have bought are silver prints : therefore they fade in the sun. Here the term common to the two premises (for such the given propositions are called, from which the conclusion is deduced) is silver prints (Y): that is predicable of the photographs which I have bought (Z), and of that is predicable be fade in the sun (X); hence be fade in the sun (X) is predicable of the photographs which I have bought (Z). Or again, Y may be a predicate affirmed or denied both of X and Z: in the Drevfus affair, the French War Office frequently argued that the man who wrote the famous 'bordereau' was on the General Staff: Esterhazy was not on the General Staff, and therefore did not write it : here Y (being on the General Staff) is affirmed of X (the man who wrote the 'bordereau') and denied of Z (Esterhazy): and hence X is denied of Z -Esterhazy did not write the 'bordereau'. Yet again, I may be a subject of which both X and Z are predicates affirmed or denied : then X may be predicable of Z, or vice versa. The horse is strong. and is an animal that lives exclusively upon a vegetable diet; therefore an animal that lives exclusively upon a vegetable diet may be strong. Here we have two terms, strong (X) and being an animal that lives exclusively upon a vegetable diet (2), affirmed as predicates of the same term (Y) the hore; and we hence deduce that I, strong, is predicable of Z, an animal that lives exclusively upon a vegetable diet, not indeed no Z, an animal that lives exclusively upon a vegetable diet, not indeed no Z, and animal that lives exclusively upon a vegetable diet, not indeed no Z, and animal that lives exclusively upon a vegetable diet, not indeed

These examples may perhaps explain what is meant by terms being related in the way of subject and predicate, and how the relation of two terms in that way to a common third term may necessitate their relation in the way of subject and predicate to one another.

What is here called a relation in the way of subject and predicate may be also called a relation in the way of subject and attribute: as it is called, for example, by Mr. Bradley in his Logic, Bk. II. Pt. r. c. iv. 6 10 and elsewhere. If the word attribute is used it must be understood generally of anything predicated 1: it is an attribute of Baal to be a god, to be talking, to pursue his enemies. to be on a journey, to be asleep, to need awakening, to have 450 prophets in Israel, to be worshipped by the Philistines: whatever can be affirmed or denied of him is an attribute affirmed or denied: the attribute may be in any category, of substance (as when we say that he is a god), of quality, time, place, state, relation, &c.; the only thing necessary is that it should be related to him as a predicate to a subject, not (for example) as an uncle to a nephew, as yesterday to to-day, as cause to effect, as here to there, as means to end, as more to less, &c.; all of these are relations in which terms may stand to one another, if we mean by terms distinct subjects of thought, and not merely the subject and predicate into which the judgement which affirms their relation is resoluble. Thus when I say that the Old Pretender was nephew to Charles II, he and Charles II may be called the terms placed (in this judgement) in a relation of consanguinity; he and 'nephew to Charles II' are the terms placed in a relation of subject and attribute. When I say that Edinburgh is west of Liverpool, Edinburgh and Liverpool are the terms placed in a space-relation; but Edinburgh and 'west of Liverpool' the terms placed in a relation of subject and attribute.

¹ i.e. in a wider seme than it is used in when the attributes of anything are distinguished from its substance or kind.

Understanding the word in this comprehensive sense, we may say that the theory of syllogism is the theory of inference in the domain 1 of subject and attribute, just as well as in the domain of subject and andicate. But it is important to remember that (attribute ' is being need in a wider sense than it usually bears : we should not ordinarily cell it an attribute of Mr. Pickwick to have been once impounded a or of Rooky Sharp to have thrown Dr. Johnson's Dictionary out of the carriege window: the word is not ordinarily understood to include actions or the casual relations of one thing to another . but in its present use it includes every predicate. The advantage of using it is this that it explains what we mean by predicate. Things may be related in space, time, quantity, degree, consanguinity, or as cause and effect : all this conveys a pretty definite meaning to us. They may be related in the way of subject and predicate: but what, we may sak is the relation of a predicate to its subject? it is that of an attribute a character attributed or belonging to it. In explaining predicate as attribute we substitute, we may say, a word expressing a real, for a word expressing a logical relation. Blue is an attribute of the gentian really and always: a predicate, only when one sudges that the centian is blue. It is true that in the theory of syllogism we have to do with attributes only so far as they are predicated; but we think of our predicates as attributes.

It has often been held that the syllogism is the type of all

¹ By a domein hore is meant a certain order or system of relations, of a single kind is see might call space a domain in which all material things are related, and time a domain in which all events are related. The domain of subject and attribute is far, less unified than that of space and time. A thing related to one other thing in space, or an event related to one attribute is an extended to one attribute is an extended to one attribute is an earn related to one attribute is the strong the space of the strong that the strong the space of the strong that the strong the space of the space of

reasoning, except the inferences called immediate! No one has done more to dispel this illusion than Mr. Bradley, in his Lopic; though perhaps the zeal of an iconoclast has prevented him from dwelling enough on the fact that the syllogium formulates reasoning which is very frequent in occurrence. But our present business is to become familiar with the theory of syllogism on its formal side. There is a precision and completeness about this theory, which have made logicians dwell on it with something of an artist's concentration; and the truth of science has sometimes been secrified to the nextness of expection.

The business of syllogism is to establish a relation in the way of subject and predicate between two terms, by means of their relations in that way to the same third term. But the judgement which relates two terms as subject and predicate may be universal or particular affirmative or negative. Moreover, we have seen that there are various ways in which the two terms that are to be brought together in the conclusion may be related to a common third term : both may be predicated of it, or it of both, or one of it and it of the other. Therefore a very general problem presents itself to us. which may be stated thus-writing 5 for any subject. P for the predicate which is to be brought into relation to it and M for the third or middle term whose relations with S and P are to bring them into relation with each other. What must be the quantity and quality of the propositions (or premisses) connecting S and P respectively with M. and how must M be related (i.e. as subject or as predicate) to S and P in these premisees, in order to establish in the conclusion a proposition whose terms are S and P, of the several forms A. E. I. and O? In other words, what forms of premisees will prove that all S is P, no S is P, some S is P, or some S is not P, by means of the relations, in the way of subject and predicate, of S and P respectively to M? Or, yet again, what relations in the way of subject and predicate between two terms S and P respectively and a common third term M will establish what relations in the way of subject and predicate between those two terms themselves? This is the question, put in its most abstract form, to which the formal part of the theory of syllogism is an answer.

e. g. Hobbes, Art of Rhetoric, Bk. I. c. i, 'all inferences being syllogisms':
c. Molesworth's ed., English Works, vi. 423.

CHAPTER XII

OF THE MOODS AND FIGURES OF SYLLOGISM

A. Romenolature. 1. In any syllogism, there are two propositions taken as true, and another inferred or following from them.

The latter is called the conclusion (Lat. questio or conclusio, GL. πρόβλημα or συμείρασμα): the former the premisees (Lat. συσείμεια, ΘL. προσέσεια).

It was said, that the premises are taken as true: whether they are true or false, the conclusion which they yield is the same; only that if they are true, it is true, and if they are false, it is probably false. We are not concerned, therefore, in the formal theory of sillogiam, with the truth or falsehood of cour premises or our conclusion, but only with the calidity of our reasoning: we wish to know, if the premises are granted, what must be granted as following from them. If our reasoning be correct, a man cannot admit the premises, and deny the conclusion. Suppose that a man admits that every restriction upon freedom of contract is mischievous, and admits that the marriage laws restrict freedom of contract, then he must admit the marriage was to be mischievous.

It has been made a reproach to the theory of syllogism, that it looks only to the cogency of the inference, and not to that truth of the premisses. We need rules, it is said, by which to determine whether a proposition is actually true, and not merely whether it is true, upon the hypothesis that certain other propositions are so. The theory of syllogism is decried as a Logic of Consistency; for the most that it can do is to furnish rules by which to judge whether different assertions are consistent with one another. In rularly with the Logic of Consistency, some writers have projected

Not necessarily, because, as we shall see, from two false premises may follow a true conclusion. But a conclusion correctly drawn from false pytholeses, implies ignorance in the reasoner, though not ignorance of reasoning.

a Logic of Truth, and offered it to the world under the name of Induction 1 But it has been unfortunately discovered that the 'Industive Methods' that were to test the truth of the premisees from which the doctrine of syllogism enquires what may be informed. suffered from the same defect as the syllogism itself : for they also were processes of inference, in which conclusions were drawn from premises: their conclusions were only true, if the premises were true: they showed themselves quite unable to determine whether their premises were true or not though it was generally just on that point that disputes were most propounced

The fact is, that so far as reasoning can be reduced to fixed forms at all and these forms studied in the abstract_whether or not the forms are syllogistic-we must disregard the truth of the premisees for in expounding an abstract form of reasoning we may even use symbols for terms 2, i.e. we do not trouble ourselves to sale what in particular the terms are at all: and hence we cannot he asking whether the judgement which connects them is true

Gines then the premisees, the conclusion follows necessarily. but it may nevertheless be false, if the premises are false. The premisses however, need not in the first place he given, they may be arantal.

Supposing a man to have admitted that whatever discourages thrift and independence is evil; and to have admitted that an universal system of pensions in old age at the cost of the state discourages thrift and independence : then he must admit as a conclusion that such a system is evil. Here, and to such a man, the conclusion presents itself in the first place as a consequence of what is already granted or 'given'. But supposing a man to be in doubt whether an universal system of pensions in old age at the cost of the state is evil or not, and to be wanting some proof, one way or the other; and that a friend offers him the above 'premisses', as showing that it is evil : then, and to him, the 'conclusion' presents itself in the first place as a question or problem, about which he wants to know whether he is to affirm or deny it; and syllogism is a process of finding proof, rather than of drawing consequences.

It makes of course no difference to the form of premises which

¹ Cf. Mill's Logic, III. iii. 9. ² As J. B. Mill does in expounding his Inductive Methods: but his symbols are very inadequate.

will establish a particular form of conclusion, whether the premises he first known, and the conclusion discovered as a consequence : or the conclusion raised as a problem, and the premises discovered to antile it. And in either case alike the promises are fairen? in the sense of being admitted and not proved in the argument. But they are not always 'given' in the sense of being that with which a man begins: our thought is as often occupied in looking for premises to establish what we believe or suspect, as in looking at premisees to see what follows from them. And that is why Aristotle need the expressions workshour and workdown. For him the conclusion was constally recorded as something to be proved 1: the promises as something proffered in proof of it; and so he saked rather 'What kinds of premisees are required to prove various kinds of conclusion (4. E. I. and O)?' than 'What kinds of conclusion follow from various combinations of premisees?' But so soon as he had answered his question, and said 'Tiese kinds of premisees prove the various kinds of conclusion ', then other people could look at the matter from the side of the premisees first. To them, the premises were something which, if given, necessitated a certain form of conclusion : rather than something which, if a certain form of conclusion were to be established must be given

2. The premisses are called respectively the major and minor premiss. This nomenclature is adjusted to that of the draw in the argument. There are, as we have seen, three terms in a syllogism: two, which form the subject and predicate of the conclusion, and one with which each of the former is brought into relation (in the way of subject and predicate) in one of the premisses. The subject and predicate of the conclusion are called respectively the minor and the major terms: the term common to the two premises is called the raddute term. The major premise is the premise in called the remains.

Or rather, to be presed or disproach: it was a thesis, which might form the subject of debate between two parties; one of them, the oppogner, held out to the other, the upholder, various propositions, which he saked him to admit, in hope to obtain admissions wherefrom there followed syllogistically a conclusion contradictory of the thesis of the upholder.

a conclassor contradictory of the these of the upholder.

These expressions are based upon what occurs in the first figure, where
the major term is commonly of greater extension than the middle, and the
middle than the minor: and the minor premiss, as compared with the minor,
is a more general proposition. But being transferred to the other figures,
in which they cannot say longer be so interpreted, they must be applained
generally as in the text: of infra, pp. 255 seq., where this is explained at
length.

which the major term occurs, and the minor premise that in which the minor term occurs. Thus in the syllogism

All organisms are mortal

the major term is mortal, and the major premiss all organisms are mortal: the minor term was, and the minor premiss was is as

. Man is mortal

organism; the middle term, organism.

It will be noticed that each term in a syllogism appears twice:
the major and minor terms each in its respective premise and in the

the major and minor terms each in its respective premiss and in the conclusion, the middle term in both premisses but not in the conclusion.

In giving examples of syllogism, it is usual to write down the major premise first; but in ordinary life and conversation, no particular order is observed; nor is it seesenrily the major premise that is written first in a logical example. The only mode of determining the major premise is to look for the premise which contains the predicate of the conclusion.

3. Syllogisms are said to differ in figure (σχημο) according to the position of the middle term in the premisees.* (i) The middle term may be subject of the major premise, and predicate of the minor: in this case Aristotle called the syllogism of the first (or perfect) figure. The example just given belongs to the first figure, as also does the following:—

No insects have eight legs Wasps are insects

∴ Wasips have not eight legs.

It is convenient to have a conventional symbolism, in which to represent syllogisms according to their form; we shall use the letters P, M, and S. S (= subject, of the conclusion) will always indicate the minor term, P (= predicate, of the conclusion) the major term, and M the middle. Thus the figure of both these examples (i.e. their form, so far as it depends merely on the position of the terms in the premisess) may be written

M P 8 M . S P

Cf. Locke, Ressy, IV. xvii. 8 (fourth or later edition).
 Cf. c. xi, supra, pp. 226-227.

the latter of the type

If we wished to indicate in our symbols the character of the propositions which compose the syllogism (i.e. whether universal or particular, affirmative or negative), we should have to write our two examples differently. The former is of the type

(ii) The middle term may be predicate in both premises, the figure of the syllogism being indicated as follows:—

e.g.

No insects have eight legs Spiders have eight legs ... Spiders are not insects.

Syllogisms in which the middle term is thus placed were called by Aristotle of the second figure.

(iii) The middle term may be subject in both premisees, the figure of the syllogism being indicated as follows:—

e.g. The Veddahs of Ceylon show great conjugal fidelity

The Veddahs of Ceylon are savages

.. Some savages show great conjugal fidelity.

Syllogisms in which the middle term is subject in both premises were called by Aristotle of the third figure.

(iv) Aristotle recognized only these three figures. But he pointed out 'that the premisees of a syllogism in the first figure would sometimes justify you in concluding to a particular proposition in which the minor term was predicated of the major, even though no

¹ Anal. Pri. a. vii. 29a 19-27 (cf. p. 258, p. 8, infra).

conclusion was possible that predicated the major of the minor. For example, from the premises

Some parliamentary voters are freeholders
No women are parliamentary voters

it is impossible to determine whether any women are freeholders or not (for a reason which will be explained later); but we can conclude that some freeholders are not women.

Again, from the premises

All persons who have the franchise are eligible to Parliament ¹
No woman has the franchise

we cannot conclude that women are not eligible to Parliament (for others might be eligible besides those who have the franchise); but we can conclude that some persons who are eligible are not women.

The famous physician Galen is said by Averrose to have referred arguments of this kind to a separate and fourth figure (sometimes called after him the Gelesian figure), in which the middle term is predicate of the major premise and subject of the minor: the figure being scoordingly symbolisms.

The theory of syllogism has been much darkened by this addition. For in erecting these arguments into a separate figure it is implied that the distinction between major and minor term is arbitrary, one of place and not of function. The meaning of that distinction must be considered next.

4. We have said that the major term is the predicate of the conclusion, and the minor the subject. But why are they called major and minor? Did Aristotle merely want shorter names, to avoid the constant repetition of such cumbrous expressions as 'subject of the conclusion' and 'predicate of the conclusion'? Are the names chosen arbitrary? And would it have been equally appropriate to call the subject of the conclusion the major, and the

If the premise had to be true, the olergy must be accepted.
In the second and third figures, where the middle term occupies the same position in both premises, either premise may be reparted as major, without affecting the situation of the middle sterm: and hence there is no possibility of erecting a separate figure bearing the same relation to them as the fourth does to the first.

predicate the minor term? Or, on the contrary, does the choice of names indicate a real feature of the relation between subject and predicate in a judgement? Is there a reason why the predicate should be called the major term, and the subject the minor?

Azistatle conceived that there was such a reason not indeed in all indocuments but in most and especially in scientific indocuments (i.e. judgements which really express knowledge). We shall do heat to look first at independents in which the distinction of major and minor term is arbitrary 'Some scholars are statesmen' might, he as well expressed by saving 'Some statesmen are scholars': for here the two terms or concepts have no necessary relation : it is only as coincident in the same individual that statesman can be predicated of scholar, or vice versa; and there is no more reason for making one term subject than the other. 'Some noulteress are not fishmonorers' is a judgement of the same kind; the two trades are frequently conjoined, but merely conjoined, and as there would be no more reason for making the sale of fish an attribute of a poulterer, than the sale of poultry an attribute of a fishmonoer, so in the negative judgement, each term is with equal propriety denied of the other. But where the subject of a judgement is a concrete thing or person, and the predicate an attribute : or where, though the subject is an abstract term, yet the predicate belongs to it, and is not merely coincident with it in the same thing: there the two terms cannot equally well be predicated of each other. We say that Caesar was a great general; if we said 'a great general was Caesar', we should still be understood to make Caesar the subject, and to have merely inverted the usual order of words in the sentence. We say that diamonds glitter, rather than that some elittering things are diamonds; that blue is a colour, rather than that a colour is blue.1 To say that a colour may be blue is natural enough: just as it is to say that a stone may be a diamond: but still we predicate the genus of the species, and not the species of the genus: it is not the genus colour, but colour in some particular case, not the genus stone, but some particular mineral that is blue or that is diamond. Commonly, except where they are merely coincident attributes 2, the predicate is a wider term, or more generic,

³ Unless a definite particular colour is meant.
Terms, though they be general concrete terms, like statesman or fishmonger, may yet express only a special or 'abstract' aspect of the nature

than the subject in independent: it is something which belongs to this and may belong to other subjects, not a part of the extension of the subject itself. It is natural to predicate the genus of the species the attribute of the concrete thing. In science especially, whose indosments should be necessary and universal, the predicate, if not commensurate with the subject, must be the wider term. We cannot predicate universally of any term what is only part of its extension. If stone is a wider or more comprehensive term than diamond, other things besides diamonds are stones, and therefore that proposition must be particular in which diamond is predicated of stone. A diamond is a stone, a stone may be a diamond : blue is a colour, a colour may be blue.

In calling the predicate of the conclusion in a syllogism the major term, then, Aristotle chose a name which was appropriate. both when the predicate is related to the subject as attribute to concrete thing and when it is related to the subject as the more to the less generic. And by the name motor he wished to indicate not (as is sometimes said) that the predicate denoted the larger class: for he did not think of a predicate as a collection of things. including a smaller collection (denoted by the subject-term) within it . he meant that it was the more comprehensive notion : embracing as it were all the subjects of which it could be predicated. but as a character in them and not a class in which they were.

of the thing they denote, if they are not in the category of substance:

cf. supru. p. 25, n. 1.

¹ In adopting these expressions, however, Aristotle had not in mind what in the Posterior Analytics he rightly recognizes as characteristic of science, in the Posterior Analysis he rightly recognizes as characteristic of science, that it aims at demonstraining commensurant judgements. Still, there are many scientific judgements which have not that character, and even in those that have it, the predicate, considered apart from the demonstration, in like any other predicate, conceived as what does belong to this subject, and might belong to others. It is only in the demonstration by which it is shown to belong to one subject, that we come to realize it can belong to that subject alone. If we see, for example, in proving that the angle in a semicircle is a right angle, that the proof hinges upon a feature which cannot belong to the angle in another segment (viz that the base of the triangle passes through the centre of the circle), then we see that the redicate is commensurate with the subject: and then also the predicate if I may so express myself) sinks into the concrete nature of the subject, and becomes a necessary part of the subject-concept. While a demonstration is still wanted by us, to show us that the angle in a semicircle is a right angle, we have no ground for supposing that that is not a property of angles in some other segments as well: so soon as we realize that it can be the property of none other, we have incorporated the demonstration with the subject-concept (of the angle in a semicircle) and major, minor, and middle The middle term takes its name not simply from being a point of connexion between the other two, but from being really intermediate concept. This it is, however, only in the first figure. It is only there that the middle term is predicated of the minor, and the major predicated of it. In the second, it is predicate in each premise; in the third, a subject, of which both major and minor terms are predicated. But that which in the first figure is really a middle term between the major and minor everes equally in the others to be the means of establishing that relation between the major and minor which we wish to prove; and the nomenclature that is fixed by the first figure is extended to them all

We can now see that Galen was wrong in adding a fourth figure to the syllogism. Where the same term M is predicated of one term Z and is the subject of which another, X, is predicated?, there X is the more comprehensive term, and Z the less comprehensive: X is really and in our thought the major, and Z the minor. We do not change this fact, by framing a forced and artificial judgement, in which the naturally minor term is predicated of the naturally major. Let utake an example.

> All organisms are mortal Man is an organism ... Man is mortal

is a syllogism in the first figure. But the premisses allow us to conclude that some mortals are men. None the less, man is not really a predicate of mortal; this conclusion affirms of the subject mortal a predicate man, that is naturally related to it as its subject or as minor term to major. Nor is it otherwise, even where the premisses allow no conclusion to be drawn in which the naturally major term is predicate. Take one of the examples given on p. 285; from the premisses

All persons who have the franchise are eligible to Parliament No woman has the franchise

terms have for us lost their isolation. Demonstration, when complete awhile completely realized by the mind, may be said to collapse into a judge-while completely realized by the mind, may be said to collapse into a judge-demonstrated, is still the more comprehensive notion, even in regard to a subject with which it is to be proved commensurate, while if it is not commensurate, it remains the move comprehensive. Cr. 9.30°, it remains the move comprehensive. Cr. 9.30°, it remains the move comprehensive.

commensurate, is that the more comprehensive boots, while if it is not commensurate; while if it is not commensurate; while if it is not commensurate; while if it is not commensurate, it remains the more comprehensive. Of p. 307, infra. I use the symbols Z and X for S and P here, in order not to seem, by taking letters which suggest 'subject' and 'predicate', to prejudge the question, which term should be made the subject.

we can draw no conclusion as to whether women are elicible to Parliament: but we can conclude that some persons eligible to Parliament are not women. Yet what an unnatural indeement is this. To be a woman is not conceivable as an attribute of eligibility to Parliament: but eligibility to Parliament is conseizable as an attribute of women : hence we might properly say that some women are not eligible to Parliament . but it is formed and artificial to say that some eligibles to Parliament are not women 1 Though we say it we feel that we are making that a predicate which should be enhiert and that a subject which should be predicate. It is true that this conclusion is not and is all that can be got, out of the premisses; but it is of no scientific value. Rither the fact is that no one eligible to Parliament is a womanand that ongoht to be expressed conversely, that no women is eligible to Parliament or else if some persons eligible to Parliament are women and some are not, we want to know what women and what men are eligible; but no one who had any knowledge of what qualifies and disqualifies for election to Parliament would express any part of that knowledge in such a proposition as that 'some eligibles to Parliament are not women'.

The introduction of the fourth figure then rests on the erroneous to the position of predicato or subject in a proposition; whereas in fact a term is made predicate or subject in a proposition; whereas in fact a term is made predicate rather than subject when it is in its own nature, by comparison with the subject, a 'major' term: i.e. a term more universal, abstract, generic, or comprehensive, than the other.

But the fourth figure has been taught for so many centuries among the 'moods and figures' of the syllogism, that for the sake of the history of Logic we cannot altogether ignore it, even while we recornize the error in which it had its birth.

The last paragraph spoke of moods and figures of the syllogism.The difference of figures has already been explained to depend on

According to Aristotle, we can only speak so sorth explicitorie. The proper subject of which to predicate attributes was in his view substance, and of which to predicate any genus, its species or the several examples of these. Where this order was insverted, the indepenent did not state what its subject was in its own nature, but to what it was incident. Doubtless this in often what we want to state, as in much a judgement at "no composer was Handel"; but in syllogism a term predicated of that to which another a subject is not naturally made the subject where of to affirm or deny

the position of the middle term in the premises. The difference of mood depends on the quantity and quality of the propositions composing the syllogism. This may be the same in different figures, or different in the same figure; e.g. in the syllogisms

All organisms are mortal

Man is an organism

... Man is mortal :

and No unlicensed body may sell liquor to strangers

A college is unlicensed

.. A college may not sell liquor to strangers :

the figure is the same (the first), but the component propositions are in one case of the form A, A, A, and in the other of the form E, A, E. If the second syllogism be now compared with the following:

No good comrade avoids pleasure All ascetics avoid pleasure

.. No sacetic is a good comrade:

it will be seen that the component propositions are of the same form in both. E. A. E: but the figure is different.

The different moods have received distinct names in the various figures wherein they occur; and hence what are called the 'moodnames' of the various forms of syllogism indicate both figure and mood. What moods are possible in what figures—i.e. what combinations of premises, as determined by their quantity and quality, will yield what form of conclusion (A, E, I, and O) with each position of the middle term—is the general problem to which the formal part of the theory of syllogism has to find an answer. We are now familiar with the technical terms that we shall employ in solving the problem. We must next consider the solution.

B. The only method of originally determining what combinations of premises will yield what conclusion is to try them all, with each position of the middle term, and see. This is what Aristotle did, in the Prior Analytics. But when it has been done, it is possible to review the result, and there recognize the nature of the faults committed in those which are invalid, and the rules which therefore must be observed (whether in all syllogisms, or in those of a particular figure) in order to validity. These rules may then be placed in the

forefront of our exposition; it may be shown, by the help of an example, that the breach of them brings invalidity; and in each figure, out of the whole number of ways in which it is mathematically possible to combine two premises, when each of them may have either of four forms, we can ascertain which in each figure are conformable to the rules that we have found necessary to be observed

in that figure.

The syllogism is now generally taught in the latter manner, which is the more formal and systematic. But the other is the more natural and we shall therefore begin for the first figure, with that.

A valid mood of syllogism is immediately seen to be valid by any one who considers it in a particular example, and though the example is particular, the form of inference is seen to be valid universally. The best way, on the other hand, to show that a mood is invalid, is to produce examples in which the premisees and conclusion are of the quality and quantity which that mood requires, and show by them that while the premisees are true, the conclusion may be indifferently true or false. For if you cannot rely on a form of argument to produce a true conclusion from true premises, it certainly is not a valid form.

Now in the first figure the middle term is subject of the major premiss and predicate of the minor. Let us take the possibilities in order.

1. Roth premises unipersal.

a. both affirmative: the mood is valid, and the conclusion A:

All organisms are mortal	All M is F
Man is an organism	All 8 is M
Man is mortal ¹	∴ All 8 is P

b. both secutive: no conclusion follows:

Sounds have no scent	No M is P	6
Colours are not sounds	No S is M	₽ 😠
Colours have no scent		
Sounds are not visible		
Colours are not sounds		
Colours are not visible !		

With actual terms, an universal proposition is often more naturally expressed without the use of the mark of quantity, All men or No colours. Where this is so, and the content makes it plain that the proposition is

/08 EFE

c. one affirmative and the other meastive : i. the major megatine: the mood is valid, and the con-

alarion R.

No Protestant acknowledges the Pone No Mie P Lutherans are Protestants All Sie M

.. No Lutheran acknowledges the Pope · No Rie P ii. the minor menatine: no conclusion follows:

Luthomne am Protostante A11 W :. D Calvinieta are not Luthemne No Rio M

· Calminista and not Protestante

Lutherans are Protestants Romanists are not Lutherans

· Romanista are not Protestante

2. One premise uninereal, and one particular.

a. both affirmative : i. major unipersal minor particular: the mood is valid

and the conclusion I: What raises prices injures the consumer All Mis P

Some import-duties raise prices Some Sia M .. Some import-duties injure the consumer · Some Sie P

ii. major particular, minor universal : no conclusion follows : Some M is P

Some taxes are levied at death Excise-duties (or Legacy-duties) are taxes All Sia M

.. Excise-duties (or Legacy-duties) are levied at death ... b. both meastine :

i. major universal, minor particular: no conclusion follows:

Starches contain no nitrogen No Mis P Some foods (or flesh-foods) are not starches 1 Some S is not M ... Some foods (or flesh-foods) contain no

nitrogen

universal, it has not been thought necessary to mark the quantity in that way. But with symbols, because there is then no content to guide us, this

is interestry.

It is the second of the following in the second of the s can be M.

•	
ii. major particular, minor universal; no	conclusion follows :
	Some M is not P No S is M :
c. one affirmative, and the other negative:	
 major affirmative and universal, particular; no conclusion fol 	
All living things change (or contain carbon) Some compounds are not living . Some compounds do not change (or do not contain carbon)	All M is P Some S is not M ∴
ii. major negative and universal, mi particular; the mood is v clusion O:	
No political offence is extraditable	No M is P
Some murders are political offences	Some S is M
. Some murders are not extraditable	Some 8 is not P
iii. major affirmative and particular, universal; no conclusion foll	
Some traders are freeholders (or are members of Parliament) No parson trades . No parson is a freeholder (or is a member of Parliament)	Some M is P No S is M ∴
iv. major negative and particular, m universal; no conclusion follows:	
Some plants are not edible Beans (or Monkshoods) are plants Beans (or Monkshoods) are not edible	Some M is not P All S is M
Both premisees particular.	
a. both affirmative; no conclusion follows	:
Some Germans are Protestants	Some M is P
Some Calvinists (or Romanists) are Germans . Some Calvinists (or Romanists) are Protestants	Some S is M ∴

Same Mis P

b. both negative; no conclusion follows:

Some things profitable are not pleasant Some M is not P
Some things popular (or pleasant) are not Some S is not M
profitable

.. Some things popular (or pleasant) are not pleasant

c. major affirmative, minor negative :

Some luxuries are taxed

Brandy (or A cart) for some purposes is Some S is not M not a luxury ... Some S is not P

.. Brandy (or A cart) for some purposes is

d. major negative, minor affirmative :

Some men of science do not study philosophy
Some rich men (or philosophers) are men of
Some S is M
Some S is not P

.. Some rich men (or philosophers) do not study philosophy

This exhausts the possible varieties in form of pramisee, so far as the first figure is oncemed; and we have found only four which give any conclusion, namely (to represent them by the accepted symbols, and add the symbol for the conclusion)

AMA AII

FIR FIG.

Since the thirteenth century, logicians have given to each of these moods, as well as to those in the remaining figures, a separate name, in which the vowels in order indicate the quality and quantity of the major and minor premises and the conclusion. The names of these moods of the first figure are Barbara, Celarent, Darii, Perio: and syllogisms of those types are called syllogisms in Barbara, Celarent, &c. 1

The exliest known work in which these mood-names are found is by William Shyrewood (born in Durhan, student in Oxford, tanglet at Paris, died as Chancellor of Lincolo, 1249; c. Prantl, iii. 10, Abech. rvii. Ann. 19; 'Modi satem 4 sorum reductione retriented his versibur—Barbara, &c. (ib. Ann. 52). They passed into general currency through the Summulas Lepicates of Petrus Hipsana, afterwards Pope John XXI, who was long believed to be the author of them (c. 1289-1277), until Prantl found them in the unpublished MS. of William Shyrawsood in the Library of Paris (vol. ii. p. 284). A somewhat similar memoria fachnica, but less ingenious, because it embodies only the form of the moods, and not the rules for the

But an addition has to be made. If the minor premiss is an universal negative proposition, and the major is affirmative, whether universal or particular, then though no conclusion can be drawn in which the major term is denied (or affirmed) of the minor, it is possible to draw a particular conclusion in which the minor term is denied of the major. Thus in 1, c, if from the premises

Lutherans are Protestants Calvinists (or Romanists) are not Lutherans

it was impossible to infer whether Calvinists or Romanists were Protestants: the former in fact being so, and not the latter. But it is possible to infer that some Protestants are not Calvinists (or Romanistal. And in 2. c. iii. from the premisesse

Some traders are { freeholders members of Parliament

No parson trades

it was impossible to infer whether any parson was a freeholder, or a member of Parliament: none of them, in fact, being eligible in the latter capacity, while a rector or vicar is legally a freeholder. But it is nossible again to infer that

Some { freeholders | members of Parliament } are not parsons.

Doubtless no member of Parliament is a parson, as no Romanist is

reduction of the moods in the second and third figures to the first (s. next. chapter) is found in the margin of the treatise attributed to Minchael Realist (1018-7-1079), Nowlyx dir viv Agarwa Agarwa description (according to Franti, in the same hand as the text, in 2.75, Abech. rx. Ann. 46). Franti believes the work of William Shyreswood to be borrowed from, and that of Petrus Hispanus to be amer translation of, the Shyespes of Faelius. In an article, however, by R. Stappes (De Summilae Legicales des Petrus and Affanderijskeipes Jubildum des destabets, Campo Sonde in Sons, Friburg in Breisgau, 1897, pp. 180 sq.; of, also his Popes Johannes XXI, pp. 180-19, Mantest: w. 1886, reason is shown for thinking that the ascription of the Synopses to Michael Feellus is erroneous, and that it is really a translation of the Chemoster the Aughtury MS. in which the ascription of the Synopses to Michael Feellus is erroneous, and that it is really a translation for the Chemoster the Aughtury MS. in which the ascription of the Synopses to Michael Feellus is erroneous, and that it is really a translation for the Laurense and the Chemoster and the title, which Stapper conceives to be in a hand fifty years later than the bulk of the MS. No other MS. acribes the work to Feellus; all the rest hipparanes as author, and four that of thoughts Scholarius (Genzadius Col., pp. 126, 671 se.; who, however, worke before Franti's work appeared.

a Protestant; and those who know this would not trouble to enunciate the subaltern, or particular, propositions; but our premises do not inform us of the universal; what they do tell us is the twith even if not the whole fruth.

We have thus two further isdirect moods, i. e. moods in which the minor term is concluded of the major instead of the major of the minor, viz.

And there are other indirect moods also. For in Barbara, Celarent, and Darii, it is possible, instead of drawing the direct and natural conclusion, to draw the converse, wherein the major term will be subject and the minor predicate. Thus in 1. a. we might have concluded 'Some mortals are men', in 1. c. i. 'No one who acknowledges the Pope is a Lutheran', in 1. c. i. 'No one who acknowledges the Pope is a Lutheran', in 2. a. i. 'Some things that injure the consumer are import-duties'. There are thus five indirect moods in all: and the whole nine are given in the first two lines of the following hexameters (it is to be noted that the extra syllables after the third, in the fifth and ninth names, are inserted metri-oratia, and have no significance):—

Barbara Celarent Darii Ferio, Baralipton, Celantes Dabitis Fapesmo Friscomorum¹: Cesare Camestres Festino Baroco: Darapti Felanton Disamis Datisi Bocardo Ferison.

The first four names in the third line belong to the valid moods in the second figure: the remainder to those in the third. It would be possible to show what moods are valid in these figures by experimenting with all the combinations of premise possible in respect of quality and quantity when the middle term was respectively predicate or subject in each premise. But any one who has followed the process for the first figure can work it out for himself in the others; and we may proceed now to the enunciation of the rules of syllogism, and the briefer deduction of the valid moods from them.

¹ The indirect moods of the first are the same as the moods of the fourth figure : cf. note, pp. 257-262, infra.

C. The Syllogistic Bules are eight in number, viz.

1. A syllogiam must contain three, and only three terms. The necessity of this rule is manifest; for we have seen that a syllogiam is an argument in which a relation (in the way of subject and predicate) is established between two terms, in virtue of their common relation (in that respect) to a third term. Hence without a third term, there is no syllogiam: and if the terms of the conclusion were not related to the same third term, there would be relation established between themselves, and on again, no syllogiam.

For example, we can draw no conclusion barely from the premises Repities are externate and The croceditie is a fixerd. Any one who knew that lixards are reptiles might infer that the crocedile is vertebrate: but the inference requires the premise Lixards are reptites no less than the other two; and falls really into two syllogiams, each containing three terms: though four terms occur in the whole arroment. viz.

- (i) Reptiles are vertebrate
 - Lizards are reptiles
- (ii) Lizards are vertebrate
 - The emodile is a lizard
 - . The crocodile is vertebrate

If the middle term is used equivocally—i. e. in different senses in the two premises—there will in reality be four terms, and no colution is possible; e. g. it is true that no expetable has a heart: it is also true that a good lettuce has a heart: but to have a heart means something different in these two propositions, and it would be fallacious to conclude that a lettuce is not a vectable.

A breach of this first rule is technically known as the fallacy of Quaternio Terminorum or of Four Terms; and where it arises through the equivocal use of the middle term, as the fallacy of ambiguous

The middle term must be distributed in one premise at least.

It will be remembered that a term is distributed, when used with

'Conversely, the middle term may be really the same, though verbally different, in the two premises; and then there is a syllogism, e.g. Sourians are sertebrate, and the crocodile is a lizard : The crocodile se retebrate.

reference to its whole extension; and undistributed, when used with reference to a part of its extension only. Thus in the proposition Alljaculous mes are suspicious, the term jealous uses is distributed (for I expressly refer to all that falls within the range of it); but the term suspicious is undistributed, for I consider it only as characterizing the jealous, and it may very well have a wider range than that. If again I say that Some jealous mess have killed their wices, in this proposition neither term is distributed.

Now when the middle term is undistributed in both premises, it may refer in each to a different part of its extension; and then the major and minor terms are not brought into relation with the same term in the premises at all: hence no conclusion can be drawn.

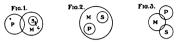
Examples from the three figures will make plain what is perhaps hard at first to grasp in an abstract statement. If a Presbuterian is a Christian, and some Christians think that the order of bishops was instituted by Christ, it does not follow that a Presbyterian thinks this. Christian is a term that includes more than Presbsterian; if all Christians thought that the order of hishons was instituted by Christ, then it would follow that Presbyterians thought so: but if only some Christians think it, how am I to tell that the Presbyterians are among these? Again, in the second figure, from the premisses Birds fly and Eagles fly. I cannot infer that an eagle is a bird : for though birds fly, many creatures may fly which are not birds, and an earle might be one of these. If in either premiss the middle term were used with reference to its whole extension : if nothing flew but birds, or nothing flew but eagles, and if my premise informed me of this; then I could conclude that all eagles were birds, or that all birds were eagles; but as it is, I can make no inference. Inference is as obviously impossible, with the middle term undistributed, in the third figure. Granted that some cripples are Tories,

This is sometimes expressed as follows: though the expression is apt to be maineding (cf. pp. 240, 250). It is aid that the promises assert agreement, of magnessment, if negative between the major or minor, and the major of minor, and the major of minor, and the major of minor is the state of the major of minor, and the major of minor is the state of the major of minor is the state of the major of the state of the sta

and some cripples are tailors: I cannot hence determine whether or not some tailors are Tories: for the cripples that are tailors may not be the same cripples as are Tories, and if not, the inference would be false. But if in either premise the middle term were distributed: if cripples were referred to in the whole extension of the term, and all cripples were spoken of: then a conclusion would follow. For whether all cripples were tailors, and some Tories, or vice verse, in either case the some of whom the one term was predicable would be included among the all of whom the other term was predicable, and then these two terms (tailor and Tory) would be predicable—not universally but in a particular indemend—one of the other.

A breach of this rule is technically known as the fallacy of

It is in the third floure, where the middle term is subject in both premisses, that the necessity of distributing it once at least is most obvious. Plainly, there, to say that it is used with reference to a part of its extension only is to say that only part of what it denotes is spoken of : and if this is a different part in the two premisses, there is not really any middle term. Some vertebrates fly, and some are rodents; but they are not the same vertebrates; swallows e. g. fly, and rats are rodents; and it is obvious that our premisses do not justify the inference that the same thing flies and is a rodent. But where the middle term is not subject, there is a certain awkwardness in talking of its distribution. This has already been noticed in discussing the 'quantification of the predicate'. It was then shown that the predicate of a proposition is never really thought of in extension. And yet in explaining the present rule of syllogism, one is tempted to speak as if it were so thought of. A general demonstration of the rule is wanted, applicable equally to any figure; and it is easy to say that if the middle term is undistributed in both premisses, the major and minor may be brought into relation only with different parts of its extension, and therefore not with the same term at all. Or if we speak of agreement between them and the middle term, we have a more seductive formula; we can illustrate with circles, thus:



¹ Cf. c. ix. pp. 198 sq., supra-

[The inclusion of one area, wholly or partially, within another symbolizes an affirmative judgement, universal or particular: it is plain that the area S may fall wholly within B, and M partially within P, and yet S may like wholly outside P. This is approach to show for Fig. 1, that with an undistributed middle we can draw are conclusion: and the other disarrant are as readily interpreted.

Yet a syllogism does not really compare the extension of three terms, and Euler's diagrams put us into a wrong train of thought. It is true, that unless the middle term be distributed once at least, there is no point of identity in the premisses; and all reasoning proceeds in some way by help of an identity. It is not true that the point of identity need consist in the same objects being denoted—in the reference to the same part of the extension of the middle term in both premisses (for which referring to the whole extension in one of them would be an obvious security). In the third figure it is on this, no doubt, that the inference hinges; but not in the second, or the first. On the contrary, the inconclusiveness of an argument in the second figure with undistributed middle is best expressed by asying that it does not follow, because the same predicate attaches to two subjects, that these can be predicated one necessarily and universally with M, it is clear that what is M need not be P.¹

If this discussion of the Undistributed Middle should seem too lengthy, it must be reamen bered (1) that for ownking purposes, in order to determine the correctness of a syllogism, the main thing to look to is the distribution of terms: and hence (2) that it is forgreat importance, in the theory of syllogistic inference, not to misunderstand this reference to distribution. In a later chapter (c. xiv) it will be necessary to consider whether the different figures of syllogism are really different types of reasoning, or the same; and the present discussion will throw light on that enquiry.]

3. From two negative premises nothing can be inferred. A negative proposition denies between its terms the relation of subject and predicate. It is clear that if the major and minor terms are both denied to stand in that relation to the middle term we cannot tell whether or not they are related as subject and predicate to one another. Russians may not be predicable of rodent, or vice versa: neither carriscorous of russiansit, or vice versa: we cannot infer anything as to the relation of carsivorous and rodent.

¹ The fourth figure has not been considered in this note, but in this matter it raises no question that is different from those that arise on the other figures.

- 4. If either premise is possitive the conclusion must be page. tive. The same kind of reflection will instify this rule as the last Two terms stand in the relation of subject and predicate between one of them and a third term the same relation is denied . if any inference is nossible? it can only be to deny the relation also between the other and the third term.
- 5. The conclusion connect be negative, unless one memies is negative. This rule is the converse of the last, and equally obvious. If both premises are affirmative and if they justify a conclusion at all they must establish and not refute our right to predicate the major of the minor.
- 6. We term may be distributed in the conclusion, which was not distributed in its premiss. For if a term is undistributed in the premises, it is there used with reference to part of its extension only: and this does not justify us in a conclusion which uses it with reference to its whole extension.

A breach of this role is called an illicit process of the major, or minor, term, as the case may be.

[With an illicit process of the minor term, if (as in the first and second figures) the minor term is subject in its own premiss, it is obvious that we are treating information about a part of the extension of the term as if it were information about the whole. If all is P, and some S is M, we can only infer that some S, and not all S, is P. Where the minor term is predicate in its own premise, or with an illicit process of the major term, the matter requires a little more reflection. The predicate of a judgement (and the major term is always predicate in the conclusion) not being thought in extension, there is some danger here again lest we should misunder-stand a reference to its distribution. Take the following example of illicit process of the minor term, where the minor term is predicate in the minor premise:

> To make a corner in wheat produces great misery To make a corner in wheat is cambling

.. All gambling produces great misery.

'It may happen, where the premises justify no inference, that an affirmative conclusion would in fact be true; e. g. if some M is not P, and all S is M, it may be true that all S is P. Here of course the middle term is undistributed, and therefore there is no real point of identity in the argument. However, it is worth while notining that the proof of this rule argument. However, it is worth while noticing that the proof of this rule also is difficult to express in a quite abstract way. The notion of agreement is employed here again, but merits the same protest as before: if one tarm agrees with a second, and that disagrees with a third, the first will disagree with the third; but the relation between subject and predicate is too loosely described as one of agreement or disagreement.

IMv premisses do not primarily give me information about '. sambling: nevertheless if there were no sambling except a corner in wheat, the minor term would be commensurate with the middle and what is predicated universally of the latter could be predicated universally of the former. As it is, however, for all the information that is given me the minor term may be (and in fact it is) of wider extension than the middle: for there are many other modes of cambling besides making a corner in wheat. It is used therefore with reference to a part of its extension only, in the minor premiss; and it is that part which I am told in the major produces great misery. I have no right to extend that information to the whole extension of the term, and say that all gambling produces great misery; my only proper conclusion is that some gambling does so. Again, with regard to the major term; if I argue that productive expenditure benefits the country, and expenditure on art is not productive : and that consequently expenditure on art is of no benefit to the country: I am guilty of an illicit process of the major term. It may not at first sight appear that I have treated information given me about a part of what benefits the country as if it were information about everything that does so. And indeed expenditure which benefits the country is not directly the subject of my thought. Yet it is plain that though productive expenditure may benefit the country. it need not be the only form of expenditure to do so; and hence expenditure on art, though not productive, may be of benefit to the country for some other reason. Yet my conclusion would only be justified if I knew every reason why expenditure could benefit the country, and knew that none of them applied to expenditure on art : whereas my major premiss mentions one ground, and not the sole ground, on which expenditure is beneficial. It is therefore true in effect to say that in the conclusion I treat as referring to its whole extension information which was confined to a part of the extension of the major term : though none the less the extension of the major term is not the proper subject of my thought. 1]

There remain two rules which are corollaries of those already given, viz.

7. From two particular premisses nothing can be inferred, and

¹ Beginners imagine sometimes that the fallacy of illicit process is committed, if a term which is distributed in the premise is undistributed in the conclusion. This is, of course, not the case. I must not presume on more information than is given me, but there is no reason why I should not

It will be noticed, therefore, that no particular conclusion can be vitiated by an illicit process of the major. error : and no affirmative conclusion by an illicit process of the major.

TITE.

8. If either premise is particular, the conclusion must be

The truth of these rules is not evident at first sight; and they can only be established generally—i.e. without reference to mood and figure—by considering what combinations of premisees there are, both of which, or one of them, is particular; and it will then be seen either that there are not enough terms distributed in these premisees to warrant a conclusion at all; or not enough to warrant

an universal conclusion, i. e. one that distributes the minor term. If both premises are particular, they must either be both affirmative (I and I), or both negative (O and O), or one affirmative and the other negative (I and O). But in a particular affirmative proposition neither subject nor predicate is distributed; so that the combination of premises II contains no distributed terms and therefore-since the middle term must be distributed if any inference is to be drawn-will yield no conclusion. From OO, two negative propositions, a conclusion is impossible. From I and O if there were any conclusion, it would be negative; but as the predicate of a negative proposition is distributed, the major term (the predicate of the conclusion) would be distributed in the conclusion : therefore the major term should be distributed in its premiss; and since the middle term must be distributed in the premisses also, we require premisses with two terms distributed in them, to obtain a conclusion : now the combination of a particular affirmative with a particular negative provides only one distributed term, viz. the predicate of the latter (O); and therefore from them also a conclusion is impossible.

A similar line of reasoning will cetablish rule 8; no combination of premises, whereof one is particular, contains enough distributed terms to allow of an universal conclusion. For again, either both are affirmative (A and I), or both negative (R and I) one affirmative and the other negative (A and I). The two negative premisess may be struck out as before. The combination of A with I contains only one distributed term, the subject of the universal affirmative (A); and as the middle term must be distributed if the reasoning is to be valid, the subject of A must be the middle term; hence the minor term will be one of those that are undistributed in the premises, and therefore also in the conclosion (of which it is the subject) it must be undistributed—i. a. the conclusion must be particular. The combinations A and O, E and I both contain two distributed terms; viz. in the former the subject of the universal affirmative and the predicate of the particular negative, in the latter the subject and predicate of the universal negative; but both of them require negative conclusions, in which the major term is distributed; in both therefore the term distributed in the premises must be the major and middle, and the minor term be one of those that are undistributed, so that the conclusion again will be particular.

The above rules are all contained in four rule hexameter lines:

Distribuas medium, nec quartus terminus adsit; Utraque nec praemisea negane, nec particularis; Sectetur partem conclusio deteriorem; Et non distribuat, nisi cum praemisea, necetve.

The third line (that the conclusion must conform to the inferior part of the premises) covers both the fourth and eighth rules; a negative being considered inferior to an affirmative, and a particular to an universal judgement. The fourth line (that the conclusion must not distribute any term, unless the premise does so, nor be negative unless a premise is so) gives the sixth rule, and the fifth.

D. Determination of the moods valid in the several figures. We have seen that syllogisms are distinguished in mood according to the quantity and quality of the propositions composing them; and in figure according to the position of the middle term in the premisses. The validity of a syllogism, and the character of the conclusion that can be drawn, depend very largely on the distribution of the several terms-middle, major, and minor-in the premises; and this again on the question whether the middle term is subject, and one of the others predicate, in a premiss, or vice versa. Hence a combination of premisses which yields a conclusion in one figure, may yield none in another : e. g. All M is P. All S is M yields the conclusion AUS is P; but AU P is M, AUS is M vields no conclusion, though the quantity and quality of the premisses are unchanged. We shall therefore have to take the possible combinations of premises in each figure in turn, strike out those which yield no conclusion in that figure, and ask what kind of T111

conclusion—i. e. whether universal or particular 1—the others yield

Now as there are four kinds of proposition, so far as quantity and quality are concerned—A, E, I, and O—and our premisses must be two in number, there are sixteen combinations of premisses mathematically possible. It is not, however, necessary to try the validity of all sixteen combinations in each figure in turn; for eight can be shown to yield no conclusion on grounds which are applicable to all four figures slike, and without reference to the resistion of the middle term.

The sixteen combinations of premises mathematically possible are as follows: they are indicated by the conventional vowels, and the major remains in all cases by the years which stands first

bromme m	an cases by the	IO AOMOT MITICIT BOND	TOTAL TITLE
44	EA	I _A	0.4
AE	BB	1E	.OE
Δl	BI	AT	OŦ
40	Jeń	10	90

Of these, the combinations EE, EO, OE, OO may be struck out, because both premises of a syllogium cannot be negative; II, IO, OI (and OO again) because both cannot be safferastive; while IE (if we do not consider issisted conclusions) would involve an illicit process of the major term; for the conclusion being negative would distribute the major term, while the major premise is a particular affirmative proposition, and therefore, whether it stood as subject or predicate, the major term would not be distributed in it.

There remain eight combinations of premisses, on whose validity we cannot pronounce without reference to the figure and the position of the middle term. viz.

AA AR AI AO RA RI IA O.

It will be found that four of them are valid in the first figure, four in the second, and six in the third; there are also five indirect moods of the first, or moods of the fourth, figure: making in all minuteen mode.

¹ For this depends on the distribution of terms in the premises, which varies according to the figure: whether the conclusion is affirmative or negative depends on whether both premises are affirmative or not, a point which can be determined without asking where the middle term stands, i.e. what the figure is.

which can be described with the figure in what the figure in a what the figure in a singular to the figure in a figure in the figure in a figure in the figu

- In the first figure, the middle term is subject of the major premiss and predicate of the minor: hence in this figure M P
- 1. The minor premise must be affirmative: for if it were S M negative, the conclusion would be negative, and so distri- S P but the major term P; the major term must therefore be distributed in the major premise; but as it is there predicate, it cannot be distributed unless the major premise is also negative (since no affirmative proposition distributes its predicate); we should thus have two negative premisees, or else an illicit process of the major term.
- 2. The major premises must be unicereal: for since the minor is affirmative, its predicate M, the middle term, will be undistributed; therefore M must be distributed in the major premise; and for this purpose the major premise, of which it is the subject, must be universal.
- In this figure, therefore, the premises AE, AO are invalid, by rule 1: IA, OA by rule 2¹; AA, EA, AI, AO are valid. The conclusions which they yield will be respectively A (universal affirmative), E (universal negative), I (particular affirmative), and (particular affirmative), and quality of the conclusion are indicated, as well as of the premises—are AAA, EAS, AII, AOO. Their names are Barbara, clearent, Daril, Ferio. But in the first three of these moods, as we have seen, the converse conclusions can also be drawn; and with the premises—AE, IE, aparticular conclusion follows denying 8 of P; and so we get also the indirect moods AAI, EAE, AII, AEO, IEO, whose names are Baralipton, Celantes, Dabitis, Fapesmo, Frisesomorrus.
- In the second figure the middle term is predicate in PM both premises: hence in it SM
- 1. One premise must be negative, for otherwise the middle S P term would be distributed.
- 2. The major premiss must be universal: for since one premiss is negative, the conclusion will be negative, and so distribute the major

¹ e.g., from the priminese Contemporary evidence is of great historical value. Tradition is not (or Some interrigitions are not) contemporary endience, it cannot be infarred that Tradition is not (or Some interrigitions are not) of great historical relate (A.E. A.) is from the premises Some pointed are real of four-central, All Gothic arches are pointed, it cannot be inferred that All Gothic arches or pointed, it cannot be inferred that All Gothic arches or to great (IA, OA).

term P: P must therefore be distributed in the major premiss; i.e. as it is here the subject thereof, the major premiss must be universal.

Hence the premises AA, AI, IA are invalid, by rule 1: the premises OA (and IA sgain) by rule 2:; EA, AE, EI, AO are valid. The moods are therefore EAE, AEE, EIO, AOO; their mood-names are Casare Camestres. Festino. and Barcon.

In the third figure the middle term is subject in both MP premisses; hence in it MS

1. The minor premise must be affirmative, for the same reason 8 P as in Fig. 1 (the major term, in both figures, being similarly placed in its premise)

This rule excludes the premisses AE, AO*: the remaining combinations, AA, AI, EA, EI, IA, OA, are valid. But because the minor term in this figure is predicate of the minor premise, and the latter is affirmative, the minor term will not be distributed in it; hence it must not be distributed in the conclusion; and therefore in all cases

2. The conclusion will be particular,

The moods are consequently AAI, IAI, AII, EAO, OAO, EIO: their mood-names are Darapti, Disamis, Datisi, Felapton, Bocardo, Ferison.

[It is impossible at this point to pass over the fourth figure, in which the middle term is predicate of the major premiss, and subject of the minor, thus (1) P M

It is clear, however, that if the premises of a syllogism in the first figure be transposed and the conclusion converted, we get just the same arrangement of terms, (2) S M

e.g. from Some (or All) dainies have a great number of flowers within a single calgy, All (or Some) composite have a great number of flowers within a single calgy it cannot be inferred that Some, or All, composite are adainse (AA, AI, IA): nor from Some annuals are not (or are) hardy, All poppies are hardy to be a form some annuals (AA and AI, IA):

(AA, A.) [A]: not room some annual are not (or are) heavy, an popping are hardy, that Some popping are not (or are) annuals (o.d. A.).

1. a.g., from the premises All astrickes have usings. No astrickes can (or Some astrickes cannot) fly, it cannot be inferred that No creatures that can fly have no usings (AE, AO), and the usings or that Some creatures that can fly have no usings (AE, AO).

-

The only difference being that P is now the symbol for the subject. and S for the predicate of the conclusion, instead of vice versa. Now the order in which the premisses are written down makes no difference to the real relation of the terms in them to one another. In (2) P is still functionally the major term : and the premises are

really premisses in the first figure, MP from which a conclusion is drawn wherein the minor term becomes predicate to the major. Thus any mood in the fourth figure can be looked at as a mood in the first figure, predicating the minor term in the conclusion of the major: in other words as an indirect mood of the first

It was stated at the beginning of the chanter that, according to the authority of Averroes, the first person to regard such moods as belonging to a distinct figure was Galen. Averroes himself disagreed with that view of them, and in this he was followed by Zabarella 2, one of the greatest of the scholastic commentators upon Aristotle, whose De Quarta Figura Syllogisms Liber is still worth reading on the subject; though in the reasons he gives for not regarding the Galenian as really a fourth and independent figure he relies in part upon the questionable analysis which regards all syllogism as an application of the principle called the Dictum de omni et nullo (cf. infra, p. 274).

Aristotle, as already remarked, recognized the possibility of concluding indirectly in the first figure; though only by the way. He remarks in one place3: 'It is clear that in all the figures, when there is no proper syllogism, if both premises are affirmative or both negative nothing at all necessarily follows, but if one is affirmative and one negative, and the negative is universal, a syllogism always arises with the minor as predicate to the major: a.g. if all or some B is A, and no C is B: for, converting the premisses, it is necessary that some A should not be C. And similarly in the other figures: for by means of conversion a syllogism always arises? This covers the moods Fapesmo and Frisesomorum in Fig. 1. With regard to Figs. 2 and 8 it is plain from Aristotle's language that though the major premise cannot be distinguished by the position

¹ Prantl i 570-574.

Pranti, i. 870-574.
And by others, e.g. Lambert of Auxerre, thirteenth century med., quoted Pranti, iii. 80, Alecha. vvii. Ann. 121.
And. Pra. vvii. 2818 Spike bit and ire is distort wite explorer. For any hydroxy And. Pra. vvii. 2818 Spike bit and ire is distort with explorer. Spike bit and irrepresent of the control of the explorer. Spike is distorted by the explorer and depote the printing of the printing of the printing of the printing of the professes debyes up to the spice and arbitrary of \$B\$ first, and of \$B\$ pplent is \$P\$ if distorted printing of the professes debyes up to the spice and the printing of the professes debyes up to the spice and the printing of the pri

[in it of the middle term, since this occupies the same position in both premisees, whether as predicate or as subject of major and of minor terms, yet in his view it was not arbitrary which term is regarded as the major; it would be the term which, as compared with the minor, is of wider extension, or as Zabarella says, higher in predicamental order. Thus if I saw that

Some roses are fragrant The Baroness Rothschild is not fragrant

--4

I can conclude that some roses are not Baroness Rothachilds. Now naturally, rose is a predicate belonging to the particular variety Baroness Rothachild, and not Baroness Rothachild a predicate to be affirmed or denied of rose. We may be said, therefore, to be concluding the minor of the major. But in many and probably in most cases of syllogism in these figures it would be difficult to say which of the two terms was naturally major and which naturally minor, for they are not generally terms belonging to one series in a classification. Hence we can transpose the premises and in any case this produces no appearance of a new figure, as transposing the premises in Fig. 1 does, because the middle term still retains the same relation to what is now treated as major term which it held towards what was before as treated. We now have

The Baroness Rothschild is not fragrant Some roses are fragrant ... Some roses are not Baroness Rothschilds

which is in the accognized mood Festino of the second figure. Similarly AEO would be regarded as Cesare, by transposition of the prunisees; and in Fig. 3 AEO as Felapton, and IEO as Ferison. But in Fig. 1, if we transpose the premisees in the moods AEO and EO, we no longer have the right position of the middle term. They must therefore be regarded either as moods of the first figure concluding indirectly, E being the minor premise; or if E be considered major premise (as containing the term which is predicate in the conclusion) they must be referred to a fourth figure in which the major term is subject of the major premise and the minor term predicate of the minor premise.

Elsewhere 1 Aristotle points out that 'whereas some syllogisms are universal [in their conclusion] and some particular, those which

^{&#}x27;Annal, Pri. S. 1.598 S seed S of pir medical or for real-departure state of \$\overline{a}\$ are the pipe, as pir medical or wires on \$\overline{a}\$ seed, or \$\overline{a}\$ seed to pir mergopasts being of \$\overline{a}\$ country of \$\overline{a}\$ seed to \$\overline{a}\$ seed to pir mergopasts being \$\overline{a}\$ seed to \$

fare universal always have more conclusions than one and so do those which are affirmative among the particular, but those which are negative among them have only the [direct] conclusion. For the other propositions convert, but the [particular] negative does not'. He means that any syllogism concluding to E, No S is P, implicitly gives also the conclusion No P is S, and any concluding to A or I. All S is P or Some S is P. implicitly gives also the conclusion Some P is S. We have therefore here a recognition of the possibility of the first three indirect moods of Fig. 1, Baralipton, Celantes and Dabitis: whose conclusions are merely the converse of those which follow directly in Barbara, Celarent, and Darii, But in Fig. 2 the converse of Cesare is given in Camestres, and vice versa, and according to the conclusion drawn, you would be said to be arguing in one mood or the other. There is no affirmative conclusion in Fig. 2 and no universal conclusion in Fig. 8: but the converse of the conclusion I in the latter figure can be got, if both premisses are universal, by merely transposing the premisses in the recognized mood Darapti : while if one is particular, the converse of Disamis is given in Datisi, and vice versa. This transposition of premisses enables us to refer all these conclusions to recognized moods, while we can still say both that the premise containing the predicate of the conclusion is the major, and that the middle term occupies its regular position in the premisses. But with these three indirect moods in Fig. 1 (as with the other two) we must either give up the rubric, that the premiss containing the predicate of the conclusion is the major premiss, or else allow that we have a new arrangement of terms, in which the middle is predicate in the major premiss and subject in the minor.

It was very early seen that what Aristotle in these massages notices generally about the three figures works out rather differently in the first figure and in the other two: and an explicit recognition of the five indirect moods as supplementary moods of Fig. 1 is attributed to his nephew and successor in the Lyceum Theophrastus.1 If the fourth figure is really the erection of Galen, logicians for some five centuries enjoyed immunity from the burden of it. For it can hardly be doubted that Galen's implies a defective insight into the character of the thought which these forms express, and treats the syllogism more as a matter of verbal manipulation. In the fourteenth chapter an endeavour is made to explain the grounds on which this verdict rests. It is hardly more than the logical issue of the external and mechanical way of regarding syllogism, which underlies the reference of these moods to a fourth and separate figure, when we find some of the later scholastic writers erecting separate moods on no better

^{&#}x27;v. Pranti, i. 365, Abschn. v. Anm. 46, where the passages from Alexander, who ascribes the addition of these moods to Theophrastus, are quoted.

[ground than the order in which the premisses are enunciated, without there being any extral difference in the premisses or conclusion.]

Granted, however, that we are to acknowledge a fourth figure, the following will be the special rules of it: it must be remembered that as referred to this figure we call that premiss the major which as referred to the first figure we should call the minor, and vice versa.

- If either premiss is negative, the major must be universal: for if either premiss is negative, the conclusion must be negative, and will distribute the major term; which in this figure is subject of the major premise; and if it is to be distributed there, the premiss must be universal (cf. Fig. 2).
- 2. If the major premise is offirmative, the minor must be universal: for the middle term, as predicate of an affirmative proposition, will not be distributed in the major premise; it must therefore be distributed in the minor premise, where it is subject; and therefore the minor premises must be universal.
- 3. If the minor premise is affirmative, the conclusion will be particular: for the minor term, as predicate of an affirmative proposition, will not be distributed in the premise, and must not be distributed in the conclusion, which will therefore be particular.²
- Hence the premises OA are invalid by the first rule: AI and AO by the second i^* : AA, AE, AE, BI, II are valid; but AA will afford only a particular, instead of an universal, conclusion. The second are thus AAI, AEE, IAI, EAO, EIO; and their mood-names, as moods of the fourth figure, are Bramantip, Camenes, Dimaris, Pesano. Freshooth.
- The complete memoria technics, with the fourth figure replacing the indirect moods of the first, is commonly given in English textbooks nowadays as follows 3:
- * a.g. Petrus Mantanaus, quoded Praudi, ir. 478. Petrus, in the edition of 1482, gives as an example of a syllogism in Gesare, 'Mullan homo est lapis, omne marmor est lapis, igitur nullum marmor est homo.' If the conclusion drawn is 'Nullus home est masmor', he calls the mood Gearner; but he comes later to Gameetres, as a different mood. By such and other ern more questionable methods, Petrus complies fiftees mood in Fig. 1, attacked in 150 (cd. 1870), who appears to treat the moods of Fig. 4 and the indirect moods of Fig. 1 as two different things.
- "see from the specimen Some change is the motion, All motion is change it cannot be inferred that Some change in not change (OA) in 10 for from All great critics are scholars. Some scholars are pedants, that Some pedants are parties care scholars. Some scholars are pedants, that Some pedants are great critics (A.): 10 or from All members of the Goernment bloom to the party in power. Some of the party in power are not in the Cabinet, that Some of the Cabinet are not members of the Goernment.
- I have not been able to trace this form of the mnemonic verses any further back than to Aldrich's Artis Logicas Rudimenta. A good many writers have tried their ingenuity in devising variations upon the original lines. Watte has a version recognizing only fourteen moods, the indirect

[Barbara Celarent Danii Ferioque prioria; Cesare Camestres Festino Barcoo secundae; Tertia Darapti Disamis Datis Felapton Bocardo Ferison habet; quarta insuper addit Baramatip Camenes Dimari Fesapo Fresison Quinque subalterni; totidem generalibus orti; Nomen habeta tullum nee si hean collici; naum.

The meaning of the last two lines is explained in the next paragraph.]

It will be noticed that in five out of these nineteen moods the conclusion is universal viz in Barbara and Celarent in Fig. 1. Cosare and Camestres in Fig. 2, and Celantes in Fig. 1 (= Camenes in Fig. 4). It is, of course, possible a fortiors to draw a particular conclusion in any of these cases: and the syllogism is then said to have a meakened conclusion or to be in a subaltern mood (because it concludes to the subaltern of the universal proposition that might be inferred from it). Subaltern moods would be used by no one who was asking what could be inferred from given premisses: for it is as easy to see that the universal conclusion, as that the particular can be drawn from them. But in seeking for the proof of some particular proposition, we might very likely find premisses that would really prove the universal : yet, since we are only using them to prove the particular, our reasoning would fall into one of the subaltern moods. Still, we should see that our premisses proved more than we had set out to establish, and substitute at once the wider thesis; the subaltern moods are therefore of little importance, and are not included in the enumeration of valid moods of syllogism.

[It would have been possible to determine what moods are possible in each figure, without enunciating the special rules (as they are called) of the different figure. It might morely have been pointed out, e.g., that in the first figure AA would yield an A conclusion, AE involve an illicit process of the major term, AI yield an I conclusion, AO again involve an illicit process of the major, EA

moots of Fig. 1 appearing neither in that capacity nor as moots of Fig. 4. Six William Hamilton (Dearwaine, p. 568) also offers 'an improvement of the many various casts of the common memonic venes'. But the reader will probably wish for no more. In various modern textbook, Raroco and Bocardo are spolt with a k, in order that ϵ medial may not occur with a different meaning from ϵ initially

[yield an E, and EI an O conclusion, IA and OA involve an undistributed middle. And if it were saked why the mood IAI is invalid in this figure, the proper answer is not because in the first figure the major premise must be universal (though that is the second rule of this figure), but because such a combunation of premises in it involves an undistributed middle; the rule being made necessary to avoid this fallacy, and not the fallacy condenned because it breaks the rule. The rules, however, if the grounds on which there were the rules of the premise from the property of the property of

CHAPTER XIII

OF THE REDUCTION OF THE IMPERFECT

Autovize distinguished between syllogisms which were only valid (bourdo) and syllogisms which were perfect (rdzeo). In the latter, the necessity of the inference appeared sufficiently from the premisese as they stand; in the former, they required to be supplemented, in order that it may be seen. The second and third figures, in his view, were in this plight. Their validity, though real, needed proving, by means of the first figure. By converting one of the premisese in the two imperfect figures, he showed that we might obtain a syllogism in the first or perfect figure, either with the same conclusion or with one from which that could be recovered by conversion; where this direct method of validating an imperfect mood fails, we can still validate it indirectly, by proving, in a syllogism of the first and perfect figure, that the falsity of its conclusion is inconsistent with the truth of its revenimes?

The process of exhibiting by the help of the first figure the validity of syllogisms in the other two (or three) is called Backuction. A knowledge of the method of reducing the imperfect moods to moods of the first figure belongs to the traditional part of the theory of syllogism. The present chapter will explain this; in the next we must ask whether the process of Reduction, though asactified by the tradition of many centuries, is really necessary, in order to validate the innerfect forces.

Directions for Reduction are concealed in the mood-names of 'Barbara Celarent'. Those who have thoroughly mastered the theory of syllogium will see at a glance how a given imperfect mood may be reduced; but the mood-name enables one to do it, as it were, with a mechanical correctness.

¹ This method of establishing the validity of a syllogism per impossibile is applicable to all the imperfect moods; but the direct method is preferred where it is available.

Reduction, as already stated, is either direct or indirect. Direct Beduction of an imperfect mood to the first figure consists showing, from premisess that are either the same as in the original syllogism, or inferred immediately by conversion from these, that the original conclusion, or one from which it can be immediately inferred, follows in a syllogism of the first figure.

As the figures are distinguished from one another by the position of the middle term in the premisses it is plain that to reduce a figure from one of the imperfect figures to the first, we must alter the position of the middle term. In the second and third figures, it occupies the same position in both premises, being predicate in the second. and subject in the third, whereas in the first figure it is subject of the major premise and predicate of the minor. We must, therefore. convert one premise of a syllogism in the second or third, in order to reduce it to the form of the first. In the second we should convert the major, for there it is in the major premiss that the middle term is out of place: in the third, the minor. But it may happen that this would give us a combination of premisses which, in respect of quality and quantity, cannot stand : e. g. in a syllogism in Disamis (Fig. 3), by converting the minor premiss A, we should get the combination II, which yields no conclusion. We therefore have sometimes to transpose the premisses, making our original minor premise the major, and vice versa, and converting in the second figure that which becomes the major, in the third that which becomes the minor. Where the premisees are transposed to make a syllogism in the first figure, they will give a conclusion in which the terms of the original conclusion have been transposed likewise; and it will be necessary to convert this conclusion in order to recover that of the original 'imperfect' syllogism.

By way of illustration, we may take the following example in Camestres, the form of which, as indicated by the vowels of the mood-name, is

If we were to argue that a spider is not an insect because it has not six legs, our argument would fall quite naturally into the above form: Insects have six less The spider has not six less

.. The spider is not an insect Now if we want to get the same conclusion in the first figure, we

cannot convert the major premise: for that would give us a particular major

Some enimals with six loos are insects

and no conclusion as to whether a spider is an insect or not would follow.1 We must therefore convert the minor premiss, which being E can be converted without change of quality; and transposing at the same time, form the syllogism in Celarent :

No animal with six less is a spider

Insects have six less .. No insect is a spider

From this conclusion we can recover by conversion the original conclusion

The spider is not an insect

Had our argument run slightly differently, to the effect that the spider is not an insect because it has eight legs, it would have fallen into a syllogism in Cesare:

No insect has eight less No P is M The spider has eight legs All S is M ... The spider is not an insect · No Sie P

Here the major premise can be converted simply, being E: and transposition is not required. The premisses

No animal with eight less is an insect

The spider has eight legs

are of the form of Celarent, and yield at once the original conalumian

If we consider the indirect moods of the first figure (the moods, as others regard them, of the fourth figure) in order to show that their conclusions (or others yielding them by conversion) can be obtained directly in the first figure from the same premisses (or from premisses which these yield by conversion), we shall see that they fall into two groups. Three, Baralipton, Celantes, and

¹ Though it would follow by an 'indirect conclusion' in Frisesomorum that some insects are not spiders.

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Dabitis, simply draw the converse of the conclusion which the same premisses yield directly; all we have to do therefore is to draw the direct conclusion and convert it. But Fapesmo and Frisesomorum yield no direct conclusion. If every copy of the Times contains an advertisement of the Encyclopacitis Britassics, and the newspaper I buy is not the Times, I cannot infer that it contains no advertisement of the Encyclopacitis Britassics. The only conclusion is that some papers containing an advertisement of the Encyclopacitis Britassics are not the newspapers I buy. Now to get this conclusion directly in the first figure I must transpose the premisses, so that 'newspaper I buy' may be in the major premiss, and 'copy of the Times' in the minor. But this will bring the middle term into the wrong position, unless at the same time I convert both premisses; then indeed I shall get the syllogism

- No copies of the Times are the newspapers I buy

 Some papers containing an advertisement of the Encyclopaedia

 Britansica are copies of the Times
- .. Some papers containing an advertisement of the Encyclopaedia

 Britannica are not the newspapers I buy

which does prove my original conclusion in a direct mood of the first figure, Ferio; though whether it is the most natural way of removing any doubt I may have had about the validity of the indirect inference in Fasesmo must be considered in the next chapter.

If these moods, instead of being regarded as belonging to the first figure, are placed in a fourth, their reduction will be formally a little different. To reduce the first three, we shall simply have to draw the conclusion which naturally follows from the same premisess in the first figure, and then convert it; but this will now be said to involve transposition of the premisess; for what is major regarded as in the fourth is minor regarded as in the first, and vice verus: thus

Fig. 4. Bramantip.

Men of stout heart are free
The free are happy
... Some who are happy are of stout heart are free

The premisses in Baralipton are premisses in Barbara; those in Bramantip are not so, till they exchange position.

^{&#}x27; τὸ εβδαιμον τὸ ελεύθερον, τὸ δ' ελεύθερον τὸ εβψυχον πρίσαντες, Thuc. ii. 43.

[On the other hand, in the last two moods transposition will now be unnecessary; for the fourth figure already regards the universal negative premise in Fesapo and Pression (= Fapemo and Prissonomum) as the major, because it contains the term which is predicate in the conclusion, though it is subject in the premise; conversion will bring it to the position required of the major term in its premise by the first figure; and so with the minor; and our corients conclusion, then follows in Erio.

Whether, in reducing a syllogism of any imperfect mood, the premisses need transposing; which, if any of them, must be converted; whether we have to convert the conclusion obtained in the first figure by the syllogism of reduction, in order to recover the original conclusion; and in which mood of the first figure the validating syllogism will be—all these matters are indicated by the consonants of the mood-names. The significant consonants!

- 1. The initial, always the same as that of the mood in Fig. 1 to which the imperfect mood must be reduced.
- 2. m (= mula), which indicates that the premisses must be transposed.
- 3. s (= simpliciter), which indicates that the premiss, or conclusion², signified by the preceding vowel must be converted simply.
- 4. p (= per accident), which indicates that the same must be converted by limitation.
- 5. c (= per contradictionem), which, occurring medially, indicates that we must employ the process of Indirect Reduction, to be explained immediately.

In order to illustrate the mechanical use of these instructions, it will be enough to work out in symbols the reduction of a single mood, Disamis. That, as the mnemonic tells us, is in Fig. 3; the middle term is therefore subject in both premisess. The major, being indicated by I, is a particular affirmative, and the minor, being indicated by I, an universal affirmative; the conclusion

1 Except the initials, these are explained in the old lines-

Simpliciter verti vult S, P verti per acci, M vult transponi, C per impossibile duci.

If any one is horrified at the doggerel, he may be assured that much worse things could have been quoted in earlier chapters.

1. e. not the conclusion of the original syllogism (which has got to be obtained as it is), but the conclusion of the calidating syllogism.

similarly a particular affirmative. Our syllogism is therefore to be of the type:---

In reducing it, the m of the mood-name indicates that we must transpose the premises, and the s that we must convert simply the premise indicated by the vowel after which it stands; the D that we shall so obtain a relicoism in Davii thus —

The simple conversion of this conclusion, enjoined by the s after the third yowel in Disamis, gives us

Some S is P

This process of Direct Reduction cannot be applied to the two moods, Barcoc and Bocardo. The reason is obvious. In order that the middle term may occupy a different position in the two premises, as the first figure requires, one of the premises in the second and third figures must be converted. In these moods, the premises are respectively an universal affirmative and a particular negative proposition. The latter, O, cannot be converted either simply or per accident; the converse of A is I; and so by converting that we should obtain two particular premises. These syllogisms can, however, be validated by the process of Indirect Reduction.

Indirect Reduction, or Reduction per impossibile, consists in showing, by a syllogism in the first figure, against which no objection can be taken, that the falsity of the conclusion in the original syllogism is inconsistent with the truth of its premisses. This is done as follows:—

Baroco is of the form

All P is M
Some S is not M
Some S is not P

Now if this conclusion is false, its contradictory will be true, i.e. that All natives of Africa are negroes. We can then combine this

with our original major premiss to form a syllogism in Barbars,

All P is M
All negroes have curly hair
All S is P
All natives of Africa are negroes
All S is M
All natives of Africa have curly hair

But the conclusion thus obtained contradicts the original minor premise; hence if the original premises are true, the conclusion we drew from them cannot be false, and our original syllogism is therefore valid

The method of reducing a syllogism in Bocardo is the same: except that here by combining the contradictory of the conclusion with the original minor we reach a result inconsistent with the original major premise; while in the former case, by combining it with the major, we deduced a conclusion contradictory of the minor. The letter c in the mood-name means that the mood is to reduced indirectly by substituting for the premise sinkested by the conclusion.

[All the imperfect moods could be validated in this indirect manner; take, e.g. p. Parapti—All M is p. M is B. S some S is P; if this is false, then N of S is P; and A il M is S; N of M is P, which is inconsistent with the truth of the original major premisa. The first figure, on the other hand, cannot be appealed to in order to confirm tizelf; if we suppose its conclusion to be false, and combine the

It is possible to reliable to mode Baraco and Beards by the direct method, if we employ the processe of permutation, and conversion by negation. From Baraco we obtain a syllogiam in Frinc, thus: Baraco, Neptum 19 is M, Some S, is not M. * Some S is not P: Fren', No not M: P. Some S is not P: Fren', No not M: P. Some S is not P: Fren', No not M: P. Some S is not P: Fren', No not M: P. Some S is not P: Fren', No not M: P. Some S is not P: Fren', No not M: P. Some S is not P. No not P. Some S is not P. Some S is

chapter.

Though for Fig. 4 the syllogism which employs the contradictory of the original conclusion as one of its premisees will yield a conclusion contradicting the concerns of one of the original premisees.

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[contradictory thereof with one of the premisses, it is only by a yllogism in the second or third figure that we can deduce a conclusion inconsistent with the other premise; e.g., in Barbars (All Some 5 is not P, and All M is P; ... Some 6 is not M—which contradicts the original minor; and again, Some 5 is not P, and All S is M ·. Some M is not P, and all S is M ·. Some M is not P, and All S is M ·. Some M is not P. and All S is M ·. Some M is not P. and All S is M ·. Some M is not P. and All S is M ·. Some M is not P. and All S is M ·. Some M is not P. and All S is M ·. Some M is not P. and All S is M ·. Some M is not P. and All S is M ·. Some M is not P. and All S is M ·. Some M is not P. and S ·. Some M ·. Some M is not P. and S ·. Some M ·. Some M is not P. and S ·. Some M ·. Some M is not P. and S ·. Some M is not P. and S ·. Some M ·. Some M is not P. and S ·. Some M ·. Some M is not P. and S ·. Some M ·. Some M is not P. and S ·. Some M ·. S

CHAPTER TIV

ON THE PRINCIPLES OF SYLLOGISTIC INFERENCE

WHEN I argue that because A=B and B=C, therefore A=C, my reasoning proceeds upon the same principle as when I argue that because X=Y and Y=Z, therefore X=Z. This principle is expressed in the familiar axiom that things which are equal to the same thing are equal to one another. In the particular inference, A=B, B=C. A=C, I do not deduce any conclusion from that axiom, as from a major premiss. It has indeed sometimes been contended that the argument is really syllogistic; that it should be written.

Things equal to the same thing are equal to one another A and C are things equal to the same thing

.. A and C are equal to one another 1

But the following considerations will show that this is not the case. Firetly, we may appeal to an analogous argument, in which a quantitative relation is established between A and C on the ground of the quantitative relations of both to G, although the quantities are mone of them equal. If A is greater than B, and B is greater than C. Are we to maintain that this inference should property be written

Things of which one is greater and the other less than the same thing are greater the one than the other

A and C are things of which one is greater and the other less than the same thing

.. A and C are greater the one than the other

The cumbrousness of this would be no reason for refusing to recognize it, if it were correct; and if the other is correct, this must be. Yet where, as in this case, it requires some violence and ingenuity

1 Todhunter's Euclid, for example, is written under the impression that this is the right way of stating such an argument.

to bring a quantitative inference into the form of a syllogism, it is not habitually done : and since men have been content not to force into the form of syllogism the inference A > B, B > C : A > C'. it may be surmised that they would not have an dealt with the inference 'A = B. B = C : A = C', if it had not been for the annarent case of the transformation. But appearances may be decentive . it must therefore be noticed secondly, that in the syllogism which is supposed to represent the latter inference, viz.

Things could to the same thing are could to one another A and C are things could to the same thing .. A and C are equal to one another.

our minor premiss and our minor term are both faulty. The minor premies is not a correct statement of the grounds of our inference : these are, that A and C are both equal to B, and therefore the major required is 'Things equal to R are equal to one another'. And the minor term ' A and C' is not really a subject of which we demonstrate an attribute: it is two subjects, which are shown to stand in a certain relation to each other. Thirdly and chiefly, the so-called major premiss is itself established through the so-called minor and its conclusion. It is because I see that if A and C are both equal to B, they are equal to one another, that I recognize the truth of the general principle or axiom. If I were incapable of recognizing the validity of the inference in the case of the three quantities A. B. and C. or X. Y. and Z. I should not be able to recognize the truth of the axiom. The axiom, therefore, is not one of the premises from which we reason, when we argue that 'A=Band B=C: it is the principle is accordance with which we reason. If it were denied, the validity of any particular inference that conforms to it would be denied also; its truth is therefore involved in that of the particular inferences. But a man may see the validity of the particular inference, without formulating the axiom. This would not be so, if it were really a suppressed major premiss, and 'A and C' a true minor term. In the argument that Silver is a good conductor because it is a metal ', every one recognizes that it is implied that 'All metals are good conductors'; and without this premiss, the grounds of the inference are not apparent. But no one requires any further grounds for inferring 'A=C', than are contained in the premisses 'A=B and B=C'.

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We may therefore dismiss the attempt to reduce this argument to syllogistic form, and recognize in the axiom not a premise but the principle or canon of the argument. But the question then arises, whether there is similarly a principle or capon of syllogistic inference Let us recall what was shown in Chanter XI of which what has just been said is only a corollary. We there distinguished between an argument in which a relation of quantity was established between two terms, through their relation in quantity to a common third term : and an argument in which a relation was established between two terms in the way of subject and attribute. through their relation in that respect to a common third term : the latter being syllogism. Now the axiom 'Things that are equal to the same thing are count to one another ' is a principle of inference in the domain of quantity. It specifies no particular quantities. but states that two quantities will stand in a certain relation (of equality) to one another, if they stand in certain relations (of equality) to a third. May there not be a corresponding principle in syllogistic inference—one which specifies no particular terms, but states that two terms will be related to each other as subject and predicate in a certain way, if they are so related in certain ways to a third term?

Such a principle has been supposed to be furnished in the Dickmede owns if nullo; and a consideration of this, and of other canons which have been proposed in its place, will throw a good deal of light on the nature of syllogistic inference, and the difference between its different types or figures.

The phrase 'Dictum do omni et nullo' is really a short title by which to refer to a principle too long to enumerate always in full; just as we refer to statutes or papal bulls by their first word or two. The principle may be expressed thus—Guod de alique omni praedicatur [dicitur, a. negatur], praedicatur [dicitur, a. negatur] etiam de qualitet eius parte: What is predicated [stated, or denied] about any whole is predicated [stated, or denied] about any part of that whole:

¹ have quoted Zabarella's formulation of the Dictum de Orani, de Quarte Figura Syldysien's Lider, Ogera Logica Coloniae, 1547, p. 1154. The words in square brackets are not his. There are numerous variants of no particular importance. Canckenthorps (III. 18, p. 202) in ed. of 1870) gives "quidquid affirmatur (a. negatur) universalitat de aliquo, idem affirmatur (a. negatur) universalitat de aliquo, idem affirmatur (a. negatur) universalitat de anni firs form seems (see Mansel

If we take syllogisms in the first figure—and it is enough to

remarks of Aldrich's) to be more nearly a translation of the passage in Aristotis's Consporter than of that in his Anderica. The formula' quod valet do combine water taking the signalist; (the reference for which it cannot now ame view is implied in speaking of the middle term as a dos, as a.g. Whately and Bain do.

The passage in Aristotle from which the Dictum de Omni was primarily derived in Anal. Pri. a. i. 24° 28-80 và bi i v She shea irvoor irios sai và sarà derived is Anal. Pri. a. 1. 1842 20-30 vs dd i r ddy r dau irrpor errope au vo anna surrete sarryopeista deripou derivor variethe deru. Arbayur dd vi anna surrete sarryopeistas, fraz publir f hafeiu rier roë brocespirou sad al direpor ed Argógrara: cai r da sarria poderir ésarrier (l'Itala des term should be contained in another sa in a whole is the same as for one to be predicated of all another. And it is said to be predicated of all anything, when no part another. And it is said to be predicated of all anything, when no part [e-logical part] of the subject can be found, of which the other term [the predicate] will not be true; and to be predicated of none, similarly?). Aristotle is here explaining the meaning of expressions which he is about to use in the Anglesic; if mortal is predicated of animal or man series never. to use in the Andrews; is mornian is predicated or animal or man in an in it means that there is no animal (e.g. man) or man (e.g. Socrates) who is not mortal. And no doubt that is involved in the truth of the universal proposition: but it does not follow that Aristotte thought of the universal proposition as no more than an enumerative judgement about every species (or individual) of which the subject-term can be predicated. The fact that he uses the formula rè piece forir le die re "priera sa well as rè repère as well as rè repère saryopiras sarà narrès roi piece to indicate the relation of the miqur to the middle term in Fig. I (and similarly with the relation of the middle to the minor) shows that he looked upon the universal as a whole or unity, and not a mere collection. Again he says of that figure, of yèp tô A sord mortes not a more contention. Again the ways of these injury, it yes to a norm more resile and red B such more resil. I such years to the first properties with the such a such as the what we mean by predicating of all') (Anal. Pri. a. iv. 25° 33-4. 87-40). what we mean by predicating of all / (Anel. Pri. o. iv. 23° 33-4, 37-40). Doubtless if it is involved in aging if all B is A', that every B is A and in saying 'All C is A', that every B is A, and in saying 'All C is A', that every B is A, and in saying 'All C is B', that every C must be A; but the particular. Indeed if it were, each particular C must be already known to B A in making the judgment 'All C is A' and therefore the informer that all C is A' would be unnecessary. Aristothe himself points this out in Asel. B C is A' would be unnecessary. Aristothe himself points this out in Asel. B C is A' would be unnecessary. Aristothe himself points this out in Asel. and a commercial content of the aristothe himself points and he hardly ever most as unumerative judgment about howe perticulars; and he hardly ever uses a singular term to illustrate the minor of a syllogism. As dishough uses a singular term to illustrate the minor of a syliogum. And attoong me must admit that in regarding Fig. 1 as the only perfect figure, and in exhibiting the necessity of the inference in Fig. 1 as he does in the words last quoted, Aristotle lays too much stress on the aspect of extension, and not enough on that of necessary connexion of content within the object, yet he largely corrects this himself in his account of demonstration, and he did not think that the essential meaning of the universal proposition, and what constituted the nerve of the reasoning, lay in the fact that it made an amertion about every particular falling under it.

There is another passage in Aristolle cometimes quoted as the source of the Dictum, viz. Cat. iii. 1° 10 (e.g. Massel' a idrich), 85 note a: Baldwin's Dictionary of Philosophy and Psychology, a roc. Aristolle's Didum). The soction runs as follows: free rispor and rispor zarryophysa is and irensulare, for and row runspopulare highers mirror as is arm's our security phighers, does be plain. All (or No) B is A, All C is B. All (or No) C is A. Here it matters not for what real terms A B and C stand any more than

remainder over the definition of the first state of of depos heyeras: others and brokespieou to heyeras and is brokespieou de others oft' in brancation forty, ofte soft immension kinera (i.e. some thing are predicated of a subject-it is their subject de quo-but do not inhere in any subject; others inhere in a subject, but are not predicated of any others are both predicated of a subject and inhere in a subject: others others are both predicated of a subject and inhere in a subject; others neither inhers in a subject, nor are predicated of any). Here it is obvious that the leading distinction is between vs. of "consequires Airpords and vs. of 'consequires about the tween being redicated of a subject, and inhering in it. The distinction is skin to that between essential and accidental predication. Man is predicated of a particular man, and animal of man is not iscontinuous as the subject de quo, because man is what he is, and animal what man is; as the subject de que, because man is what he is, and animal what man is, remove the predicate, and the subject would not be left; the predicate as it were overspreads the whole subject. In the same way grommer is predicated of Priscian's distinguishing science, and science of prommer is and investigation, because grammar is what his science was, and science is and incomplete, because grammar is what his clience was, and coinne is what grammar is. Here some is a concrete and grussmars in a bettered term; but either is predicated as and incomplete and particulars—they are the subject do quo; and predicates which are of their essence, or tell us what they in themselves are, are predicated see and incomplete are, are predicated see and incomplete are in found in the soul, and colour in a body, as On the other mana, grammar is found in the soul, and colour in a cour, as inhering, as fe bowerships; and if they are predicated of these subjects, we are not eaying what the soul is, or what a body is, essentially; these stributes indeed can only exist in a subject (and therefore Aristotle maxings inness can only exist in a subject (and therefore Aristotle explains ris is overaging on the inharcht as 8 for on pis is price independent of the control of the co The grammatical science of Priscian therefore, though there is no subject The grammatical science of remain tracestors, shough reset is no support of which it is predicable as de quo, is and irrectangulor (for it is a particular instance of that attribute, or universal), yet exists is become, as an attribute in his 'soul'; but Priscian himself is neither predicable of any subject is not becomes universely being a concrete individual), nor (for the same on) does he inhere or exist in anything further.

reason) does he inhere or exist in anything forther. He was the first many think articular proceeds to add the sentence quoted at the Having and this articular proceeds to go the sentence of the first network of the fir

in the axiom it mattered what real quantities were intended. Whatever they are suppose that A can be affirmed or denied of all R it. can be affirmed or denied of each particular subject. C or any other. included in R. Here according to a tradition which has been strong is the fundamental principle of syllogistic inference. In this Dictum is nakedly displayed what is the nerve of our reasoning. whenever we syllogize in the concrete. It is the semurance that A is true of all B. which satisfies us that it is true of this B. viz. of

primarily predicated not of the individual-e.g. the individual man

primarily predicated not of the incivious—e.g. the individual mode of the species sum; we say that a man is an animal, not that Socrates is an animal. Now man is not the irrestigator, but hipprox and therefore it cannot be primarily said of animal that it and irrestigator hipprox. Yet we cannot treat it like a generic abstract term inscription hippers. Yet we cannot treat it like a generic abstract term such as series, and my that it attaches to men in set of invargative and to Scorate in it is increasing. Still less can we treat it like the consequence of the conseque however, is provided for already in Aristotle's list, as something which sat investigation re historia sal le investigates ioris: and animal and its congeners are no less provided for, if we realize that, though predicated primarily of dicates, they are ultimately and really predicated of the subjects of these. The section is therefore far from enunciating the Dictum de owni et aullo The investigator is the concrete individual, and not a minor term (though it is true that it might be also a particular instance of an attribute). The transference of a predicate A from B to C is considered only in the case where A is predicated of B, and B of C, is not foresupino: but the Dictum is innocent of any such restriction. If Priscian was a grammarian, and a grammarian is scientific, Priscian was scientific; but here in the minor remiss it is not true that srepor suff srepor sarryopeiras is saff imassimison. premias it is not true that fraper and fripor carryopoirus six and fracespieco. Il Princian was a man, and all men are jaslous, Princian was jaslous; but here jaslous, in relation to men, is not one of those things for serie voir extrapospositive highests; men is that, for front. Now the Dictum covers these syllogiums no less than the syllogium 'all men are animals, Sortum covers the series in a man. Socrates is an animal—if indeed Aristotle would have called any of them syllogiums (cf. 16/10, p. 289). But the remark which we are considering cannot cover the first two, nor could Aristotle have thought of it for a moment as covering them; the difference between accidental and is for a moment as covering unon; the dimeració octween accidental and essential predication was much too prominent in his mind. There is therefore no ground for mying that this passage enunciates the Dictum; whether he would have accepted the Dictum as a correct expression of the principle of syllogistic inference is another question, to which the answer depends very much on how we interpret the Dictum.

C; the business of reduction is to bring imperfect syllogisms into a form, in which we can see at once that the principle applies to them; and the title of the first to be the perfect figure lies in its admitting of the application of the Dictum do omai et suile.

There are several objections urged against the claims of this formula. In the first place, it suggests the 'nominalist' dortinalist' dortine expressed by Hobbes, when he said that reasoning is but the right ordering of names in our affirmations. It suggests that our ground for affirming or denying that C is A lies in the fact that A is said of all, or no, B, and B is said of C. Clearly it is because we believe that B is A, and C is B—not because B is called A, and C is called B—that we assert the conclusion. However, this nominalist interpretation of the Dictum is not necessary; it is not as thus interpreted that it will be here discussed; and therefore this objection may be disminsed.

It may be said secondly, that if the reduction of the other figures to the first is not necessary, i.e. if the true character of our reasoning in them is not more clearly displayed in the first figure, the Dictum is not the principle of all syllogistic inference. In claiming to be that, it denies any essential difference between the different figures; and those who think them essentially different are so far bound to question the analysis of syllogistic inference which the Dictum implies. This is quite true; but we can hardly discuss the relation of the different figures, until we have settled whether the Dictum expresses correctly the nature of our reasoning in the first. We come therefore to what is the main criticism which has been

we come therefore to what is the main criticism which has been surged against the Dictum is a true analysis of its nature. It is easil that a syllogism would, on this showing, be a patitio principii, or begging the question, as it is called in English, is meant assuming in one of your premisses what you have to prove. Of course, the premisses must implicitly contain the conclusion; otherwise you would have no right to draw it from them, and could deny it, while admitting them: this much is true of every kind of cogent inforence, whether syllogistic or not, though it has been sometimes treated as a peculiarity of syllogism by persons who thought they could find other kinds of inforence not obnoxious to it. But you do not beg the conclusion in the premisees, except where the conclusion is necessary to establish one or other of other for other of

the premisses. For example, I may know that treason is a capital offence; and the law might make it tressonable to publish libels against the sovereign: and in that case, from the premisses, All treason is a capital offerer To likel the sorrerion is treason I could infer that To libel the sovereion is a capital offence. In this argument, there is no actitic principii. I can learn the truth of both premisees by consulting the statute-book and do not need to be aware that it is a capital offence to likel the sovereign in order to know either of the premises from which that conclusion is deduced. But the case is different in such a syllogism as that All reminents part the hoof. and The deer is a ruminant . The deer parts the hoof. I have no means here of accertaining the truth of the major premise, except by an inspection of the various species of ruminant animals; and until I know that the deer parts the hoof, I do not know that all ruminants do so. My belief in the constancy of structural types in nature may lead me to expect that a rule of that kind, found to hold good in all the species which I have examined, holds good universally: but this presumption, so long as it rests merely on the examination of instances, is not conclusive: I should not accept the conclusion

Now it has been alleged that all syllogism is a petitio principii 1: and the allegation has gained colour from the Dietum de omni et sullo. 'That which is affirmed or denied of any whole may be affirmed or denied of anything contained within that whole.' What do we mean by a whole here? If it is a class or collection, if the major premiss is to be understood in extension, then it can hardly be denied that it presupposes a knowledge of the conclusion. If in the proposition All B is A. I mean not that B as such is A. but that all the B's are A. I must certainly have examined the case of C (if that is one of them) before making the assertion; and therefore the major premiss, All B is A, rests (inter alia) on the present conclusion, C is A. According to this view, the major premise of a syllogism is (at least in most cases 2) a statement of fact about the

merely on the strength of the premises, but should seek to confirm it by an examination of the hoof of the deer; the case of the deer

therefore is necessary to establish the rule.

course know them, in advance of any knowledge about the particular acts

¹ Cf., e. g., Mill's Logic, II. c. iii. Mill's own way of avoiding the charge is not very successful.

Where general rules are made by men, as in the case of laws, we can of

whole of a number of particulars; it is really an enumerative, and not a true universal, judgement. We make it, not because of any insight that we have into the nature of the predicates B and A, and into the necessity of their connexion: but simply because we have examined everything in which B is found, and satisfied ourselves that A is could verseath in all of them.

There is indeed another sense in which the major premiss may be understood, and one in which it no longer makes an assertion about the whole of a number of particulars. If I say that all sold is vellow. I need not mean to assert that every piece of metal, which hy other qualities I should identify as gold, is also vellow-a statement for which I certainly cannot claim the warrant of direct experience. I may mean that a vellow colour is one of the qualities on the ground of which I call a substance cold: or, in Locke's language, that it is included in the sominal essence of cold. By a nominal essence. Locke means what J. S. Mill called the connotation of a namethose attributes which are implied to belong to any subject, when we call it by some general name. We may collect together in our thought any set of attributes we like, and give a name to the assemblage of them : and then it will, of course, be true to say that anything called by the name, if rightly called by it, possesses any of the attributes included in the signification of the name. The general proposition ceases, in that case, to be enumerative; but it does not become really universal. It becomes a verbal proposition. Gold is vellow, because we do not choose to call anything gold which is not vellow; but we are not asserting that there is any necessary connexion between the other attributes for which a parcel of matter is indeed to be gold, and this of vellowness. Given such and such attributes, we call it gold; and therefore gold has all these. Let any one of them be wanting, and we should not call it gold : therefore that is not gold which is not vellow : but there may be a name! of matter for all that we mean to affirm, which has all the other qualities of gold, but is of the colour of silver.3

or events to which they refer. Such syllogisms, therefore, as that about libelling the soversign, given in the last paragraph, can in no case be alleged to beg the question. If any other authority (such as revelations, acquaints us with general relate, they will serve as major promises of equally unexceptionable syllogisms. All other general propositions have, by the extremer critics, been interpreted in the way mentioned in the text.

For this distinction; cf. supra, p. 158.
Cf. Locke's Essay, III, vi. 66 6, 19, and also pp. 78 so., supra, on Definition.

xiv) PRINCIPLES OF SYLLOGISTIC INFERENCE

Locke did not suppose that the ordinary man, who says that gold is vellow, means only to assert that vellowness is one of the attributes included by him and others in the nominal essence (or connectation) of the word gold. But he thought that the ordinary man would find it hard to say what precisely he did mean and anyhow that this was all that the evidence and the means of knowledge open to us justified him in meaning. It is not our present business to discuss this; we have not to sak how many of the ceneral propositions enunciated in the sciences have any right to be recorded as really universal propositions, nor what means there are (if any) of proving universal propositions about such matters of fact. We are concerned with the theory of syllogism, and the allegation that it begs the question. We found that if the major premiss be interpreted in extension as an enumerative judgement. the charge is true; and that the Dictum de omni et nullo at least lends colour to such an interpretation. We have now seen that there is another interpretation, according to which the major premise becomes a verbal proposition. On this view, its general truth does not depend on an examination of all the instances included under the subject of it, and may therefore be known antecedently to such an examination. It depends however, on an arbitrary convention about the meaning of names: the syllogism too will still be a petitio principii, though not in the way which the Dictum de omni et mullo suggesta. For though the major premiss will no longer presuppose a knowledge of the conclusion, the minor will do so. If nothing is to be called gold unless it is yellow, I cannot tell that the substance, in which I have found the other qualities which the name implies, is gold, unless I have first seen that it is vellow. Of course colour being the most obvious of the properties of a substance. I am not likely ever to be in the position of inferring the colour of a substance from its name; but the argument is the same as if I took some unobvious quality, like solubility in aqua regia. If that is part of the nominal essence of gold, then I cannot tell that a particular parcel of matter with the familiar weight and colour of gold is gold, until I know that it is soluble in squa regia. I do not therefore infer its solubility from the knowledge that it is cold, but I call it cold because I know it to be thus soluble.1

' It will now be seen why a syllogism was explained to beg the question, if it presupposed the conclusion not in the premises together, but in

We need not dwell longer on the view that a general proposition asserts the meaning of a name, nor on the consequences, fatal enough, which this view would entail on the syllogism. Reasoning is not a mere process of interpreting names; and it is not the principle of syllogistic inference, that whatever a name means meed be affirmed of the subjects called by it. In considering the charge that the syllogism is a petitio principil, it was necessary to notice the view which makes the petitio lie in the major. We must now return to the latter, and to the Dictum which is supposed to counter-

We saw that the crucial question here concerned the nature of the major premiss; is it universal, or merely enumerative? is it based on an enumeration of particulars, or on the connexion of universals? If it is enumerative, and rests on a previous review of all the particulars included in the middle term, the charge of positio is sustained. We should then accept the Distans do ownsid a sulfo as the general principle of syllogism, the 'whole' of which it speaks being understood as a whole of extension, a collection or class; but we should scarcely be able to speak of syllogistic inference.

Now Aristotle, who thought syllogism to be the type of all demonstration, could not possibly have understood the major premise in this way.\(^1\) He thought that, although we might know as a fact that \(^0\)fin A, yet we did not understand it, without seeing that it must be so; and to see that it must be so is to see that in it which makes it so—to see that it is A is wirtse of B. B is a middle term, because it really mediates between C and A; it performs for C the office of making it A, and is the reason why C is A, not merely the reason why C is M, not merely the reason why E show C to be A.

We have already, in discussing the modality of judgements, met with this distinction between the reason for a thing being so and so, and the reason for our knowing it to be so—between the ratio execution and the ratio consoceasi. We not a synthat wheat is nourishing, because it contains nitrosen and carbon in certain proportions. I give

either of them singly; all syllogisms in a sense presuppose it in the premises taken together (though they do not presuppose a knowledge of it).

'The doctrine of the Postrior Analytics must in this respect be taken as overriding the more formal and external treatment of syllogism in the Prior.

the reason for its being nonrishing: it is this constitution which makes it so. When I say that Mellin's Food is nourishing because Baby grows fat on it. I do not give the reason for its being nourishing but only the research for my serving it is so : it is not Raby's condition which makes it nonriching but its nonriching properties which produce Baby's condition. The physical sciences always look for rationes essends, so far as possible : though it may be noted that in what is, in many ways, the most perfect of the sciences, viz. Mathematics, we reason very largely from rationes coonsecreds. If A = B. and R=C then A-C but it is not because A and C are both equal to B, that they are equal to one another, though that is how I may come to know of their equality. The reason why they are equal is that they contain the same number of identical units.1

It is not all syllogisms in which the middle term gives the reason why the major belongs to the minor. It does so only in the first figure and not always there. Because a syllogism falls into the first figure, whenever the middle term really is a ratio executi. Aristotle called it the scientific floure, oving dugranuousdu.2 Why are modest men grateful? Because they think lightly of their own deserts. This implies a syllogism in Barbars. All who think lightly of their own deserts are grateful, and modest men think lightly of their own deserts. But if I try to establish the conclusion by an appeal to instances, pointing out that Simon Lee and Tom Pinch, John Doe and Richard Roe, were modest, and were grateful. I am giving not a reason why the modest are grateful, but reasons which lead me to indoe them to be so: and my syllogism falls into the third figure, not the first: These men were grateful, and these men were modest, therefore modest men are (or at least they may be) grateful. The first figure is scientific, because a syllogism which makes

you know why C is A falls into that figure; but the middle term in the first figure used not be a ratio essendi. Parallel rave of light proceed from objects at a vast distance : the sun's rays are parallel ; therefore they proceed from an object at a vast distance. Here my syllogism is again in Barbara; but the distance of the sun is not due to its rays (at the earth) being (so far as we can detect)

But we cannot give this resson for the equality of the units. * Anal. Post. a. xiv. 79* 17. The rest of the chapter is by no means all of it true.

parallel: their being parallel is due to the distance of the sun from the earth. Nevertheless, the syllogisms in which the middle term does account for the conclusion are enough to show that syllogism is not essentially a process of inferring about a particular member of a class what we have found to be true of the whole class. The importance of the scientific, or demonstrative, syllogism in this connexion, is that it most effectually disposes of this analysis of syllogistic inference. It shows that there are syllogisms which cannot possibly be brought under the Dictum de omni et sullo, thus interpreted. We shall, however, find that even where the middle term is not the cause of the conclusion, in the sense of being a ratio essendi, the Dictum thus interpreted does not give a true account of the nerve of cur reasoning.

For the central idea of syllogism is that it works through concents. or universals. The major premiss asserts, not the presence of A in every B (and therefore in C, among them), but the connexion of A as such with B as such 1: hence wherever we find B, we must find A: if we know, or can show, that C is B, then so inso it is A. B is one thing, present in many; an attribute that is the same in the various subjects in which it occurs, and therefore involves in every case what it involves in any. How we are to discover what B involves is a problem of Induction, in the modern sense of that term. But if we know it, and if we know or discover in a subject C that the condition B is present, we know and conclude that C is A. Where B is only something from which we can infer A. as we infer the distance of the sun from its rave being parallel. B is still an universal, by ἐπὶ πολλών: an attribute which for one reason or another we take as a sure indication of another attribute. and which we look on as the same in the various instances of its existence. There could be no syllogism if the major premise really made an enumerative statement about a number of particulars: the most that we could say of the major premiss then would be what Mill save of it, that it is a note or memorandum to which we subsequently refer in order to refresh our memory and save the trouble of repeating our observations: as if a man intending to dispose of part of his library were to put the volumes, which he did

 $^{^{1}}$ Or the exclusion of A as such from B as such, if the syllogism is negative.

not consider worth keeping, all in one bookcase: he might then infer that any particular volume in that bookcase was not worth keeping, merely because he had made a mental note to that effect about them all, and without looking at the volume again.

The perception that the middle term is not a class but a character. universal and not a sum of particulars, has led to the formulation of a principle intended to express this more estisfactorily than the Dictum de omni et nullo doen: of which it has already been said that it at least lends itself to an erroneous view of the major premiss, as an enumerative proposition, though it was by no means always so intended. The principle is this... Note solar set solar sei iprius (and for the negative. Repuonans notae repuonat rei ipsi): i.e. what qualifies an attribute qualifies the thing nessessing it. Certain objections may be made to this formula also. It suggests that the minor term is always concrete, and that the avilorium refers to a concrete subject (res ipea) what in the major premise is stated to characterize its predicates. It speaks also as if one attribute were conceived to qualify another in the same way as an attribute qualifies a concrete subject. And the conception of a mark or note is no improvement on that of attribute.1 We need not interpret it as a purely external sign, related to what it signifies as a word to its meaning or a letter to a sound. The 'notes' of a thing are its characteristics, as Cardinal Newman spoke of the notes of the Church; they are not the mere indications by which we judge what object is present, but themselves contribute to make it the object that it is. Yet the nature of a thing is no less ill conceived as an assemblace of marks than as a bundle of attributes. The notes of the Church would not exhaust the notion of the Church: the marks of a disease, though elements and features of it, would not give a complete conception of what the disease is, There are predicates of a thing which include too much of its nature to be called marks of it. Nevertheless this formula has the great advantage that it does prevent our regarding the middle term as a class which includes the minor in its extension.2

¹ Cf. Hegel's Logic, § 165, E. T., p. 296: 'There is no more striking mark of the formalism and decay of Logic than the favourite category of the "mark".' J. S. Mill (Logic, I). ii. 4 and note) etnagely mininterpret the maxim Note notes set note rei jessius. He understands by res jose the major term, and by note the minor; so that the whole, instead of meaning that what

Kant said of the syllogism that it subsumed a cognition (i.e. a embiest of knowledge) under the condition of a rule and thus determined it by the predicate of the rule.1 The rule is given in the major premiss, which connects a predicate (the major) with a condition (the middle term): the minor premiss asserts the fulfilment of this condition in its subject; and in the conclusion we determine the subject by the predicate which the rule, in the major premise connected with this condition. This analysis brings out the essential nature of the major premiss, as a rule connecting a predicate with a condition universally, not an assertion that the predicate is found in the whole of a class. It also applies equally where the middle term is, and where it is not, the ratio essendi of the major. And it is free from the objections just project against Nota solar? If we were to frame from it a 'canon' parallel to this and to the Dictum de omni et mallo, it would run somewhat thus. Whatever satisfies the condition of a rule falls under the rule. If B is the condition of the rule of being A. whatever is B-for example, C-will fall under the rule of being A. We may nerhans accent this as a statement of the nature of the reasoning employed in syllogisms of the first figure. We need not deny that the Dictum de omni et aullo, if rightly interpreted, is free from the offences charged against it. If the owns be understood

qualifies an attribute qualifies the subject of it, comes to mean that what indicates the presence of an attribute indicates what the latter indicates. He naturally gets into great difficulties where the minor term is singular. We may treat the attributes of man as a mark or indication of mortality (though this is rather like saying that a bottle of Liebig's Extract is a mark (though this is rather like saying that a bottle of Liebig's Extract is a mark of the presence of a certain familiar signature); but we cannot treat Scenates All seen are mortal, All kings are seen (or Scenates is a man); All kings are seen (or Scenates is and); All kings are seen (or Scenates is a man); All kings are more for Scenates in and); All kings are more for Scenates in and); All kings are more for Scenates in an and); All kings are more for Scenates in the former is paraphrased. The attributes of a king are a mark of the attributes of man, that of the former is paraphrased. The state is not a seen and the major term, the most general or abstract term in the syllogium; and the whole interpretation, which necessitates a measure of the passage in At. Cat. 12 to 12, quoted p. 275, n. 1, sepre.

Krit.d. Vern.**Transcendental Billech, Interd. II R.R. p. 125, Meiklejohu*

¹ Krit. d. r. Vern., Transcendental Dialect, Introd. II. B. (p. 215, Meiklejohn's Translation).

[&]quot;Kant himself applied this analysis to hypothetical and disjunctive arguments also. In a later chapter, these are more strongly distinguished from 'categorical' syllogians than he allows. But this need not prevent the acceptance of his analysis. A stakement may correctly argress the nature of syllogistic inference, even when some arguments, which are not strictly syllogistic, are than alleged to fall under it.

as an unity present in many instances—a whole of intension not a whole of extension—then the principle will serve. But the other puts more clearly the nerve of the inference. And it applies to all syllogisms in the first figure, whatever the nature of the middle term : whether it he a mere sign of the major term, as if we said that 'All men with large hands and small eyes are choleric'where the connexion of the predicate with its condition, though accented de facto, is one for which we can see no necessity : or whether it give, wholly or in part, the reason and the explanation of the major, e.g. in such premisses as that 'All trees fertilized by the wind blossom before their leaves are out', or that 'Men successful in a work that gives full play to all their faculties are happy'. Whatever our particular avilogism is, we shall find it true to say of it, that it brings a subject under a rule, on the ground that it satisfies the condition of that rule: that it affirms (or denies) a predicate of a subject, on the ground that this subject fulfile the condition with which the predicate (or its absence) is universally hatnanna

That this like the axiom of equals, is a principle and not a premise of reasoning, is easy to see. Any one denying it would as readily deny the validity of any particular syllogistic argument; but a man may admit the validity of the inference, in a particular case, without needing to consider this general principle. And, as no one could see that Two things equal to the same thing are equal to one another, who was incapable of seeing the truth of that principle in a given case, so no one could see the truth of the principle that What satisfies the condition of a rule falls under the rale, who failed to recognize that if all organisms are mortal, and man is an organism, man must be mortal. What then is the use of the principle, if it is not a premise of inference? It might be used to stop the mouth of a disputant who denied the conclusion which followed from the premisses he had admitted. We might ask such a disputant, whether he denied the truth of this principle. and unless he was prepared to do that, require him to admit the validity of the syllogism he was disputing. It is true that in consistency he might decline. A man who denies the validity of a given syllogism in Barbara may with equal reason deny the argument which attempts to prove its validity. For that argument will itself take the form of another syllogism in Barbara :

All inferences upon this principle (that what satisfies the condition of a rule falls under the rule) are valid

The syllogism in question is an inference upon this principle · It is valid

Why should a man admit this reasoning if he will not admit that since

All organisms are mortal, and Man is an organism

· Man is mortal?

The two are of the same type, and show that you cannot make the principle of avillogistic inference into the premies of a particular syllogism, without begging the question. Yet a man who disputes in a particular case the conclusion that follows from his premisees may heritate to maintain his attitude, if the principle of reasoning involved is not nakedly before him, and shown to be one which he daily proceeds upon, and cannot disallow without invalidating his commonest inferences. For this reason it may cut wrangling short if we can confront a man with the principle of the inference he questions. Show him, for example, that the inference ascribes to a subject, in which certain conditions are fulfilled, a predicate connected universally with those conditions, and he cannot longer refuse his assent. For to do what it does is to be a sullogism?: and therefore valid.

And there have been writers 2 who thought that the only object of knowing the theory of syllogism was to cut short wrangling. But there is another object, connected with a side of logic which the

Cf. an article on 'What the Tortoise said to Achilles', by 'Lewis Carroll', in Mind, N. S. iv. 276 (April, 1895). It is obvious that the validity of the latter of these two religious cannot require to be deduced from the principle which stands as major premise in the forner. For if until that is done its validity is doubtful, then the principle by which we are to establish it validity is equally doubtful. Benice, what proves the validity of the former, or validating, religious ? The validity of a sylingious cannot be deduced from vanuasing, sylvogum? Ins valuaty or a pyllogum cannot be deduced from its seem major premise; else the fact that all organisms are mortal would show that the syllogism, of which that is the major premise, is valid. If it be said that the validating pyllogism meds no proof of its validity, the same can be said of the syllogism which it validates. But if it needs a proof, the syllogism which validates it will need validating by another, and so ad infinitum. No form of inference can have its validity guaranteed by another inference of the same form with itself; for we should be involved at once in an infinite process.

Cf. Ar. Post. An. B. vi. 92 11-16.

e. g. Locke, Essay, IV. zvii. 4.

same writers for the most part ignore. Logic is not an art. Its business is to know and understand the processes of thought, and not least the true nature of our processes of inference. To this business belongs the question, what is the principle of a certain inference which we make and recognize to be valid? To find and formulate that principle—to extricate it from its concrete setting in the matter of a particular argument, and set it out in abstract. -this is the logician's task. Now men may miginterpret the character of syllogism, and formulate wrongly the principle involved: vet if their misinterpretation is generally received for true, the wrong principle will serve in practice to stop dispute as well as the right principle would have done. Those who are agreed that syllogism is conclusive bowever they define a syllogism, will accept an argument if it can be shown to accord with their definition: and the same misinterpretation which appears in their account of the general nature of syllogism will appear in their view of particular syllogisms, from which that account is of course derived. Therefore, though it be said that a syllogism is an argument which applies to any member of a class what is true of them all. yet even this analysis of it, however faulty, will serve to 'stop wrangling, among persons who accept it. For let a particular argument be exhibited as doing this, and it will be accepted as valid. But the theoretical objections to this analysis of syllogistic inference are in no way lessened by its being practically as useful as any other that men could be brought to accept. The paramount question is, whether it is true : not whether for any purposes it is useful. And the present chapter has been quite disinterested; it has aimed at throwing light on the question. What is a syllogism? i. e. What is the principle of inference which a syllogism exemplifies?

We have ignored of late the imperfect figures, in seaking an answer to this question. They furnished a possible objection to the claims of the Dictsum de owns et satilo¹; for if their reduction to the first figure is unnecessary, then the Dictum, which only contemplates the first figure, cannot be the principle of all syllogistic inference. But this objection was deferred, until the Dictum had been examined on its own ground. We must now return to the subject of the imperfect figures.

1 Cf. supra, p. 278.

It may make things clearer, if the view to be taken in the following pages is given summarily at the outset. There are difficulties in any view of the matter; because the same verbal form may be used where the thought in the speaker's mind is different. The true character of an argument depends not on the verbal form, but on the thought behind it. And therefore sometimes the movement of a man's thought, though he expresses himself, a.g., in the second figure, would be more adequately exhibited in the first. In such a case direct reduction may be defensible, though still unnecessary; and yet it may be true that, speaking generally, the direct reduction of the imperfect figures distorts them, and purchases a show of conformity with the first figure at the expense of concealing the genuine movement of thought in them.

It would seem them that syllogisms in the second and thirdfigures do not as a rule merely present under a disguise the reasoning of the first; they are independent types. Their validity is confirmed, in the second figure, by the relactic ad alserdsms, and in the third, by the method which Arisotte called Relevar, or exposition. The fourth figure (or indirect conclusion in the first) is not an independent type; its first three moods are merely moods of the first figure, with the conclusion converted, as the process of reducing them assumes; its last two moods draw conclusions which are shown to be valid most naturally by reduction to the third.

Let us begin with the second figure. Take the syllogism: all true rores bloom in summer: The Christmas rose does not bloom in summer: It is not a true rose. Surely, if a man heritated for a moment about the necessity of this consequence, he would resource himself, not by transposing the premises, and converting the present minor into the statement that No rose which blooms is summer is a Christmas rose; but by considering, that the Christmas rose, if it were a true rose, would bloom in summer, whereas it does not. The same remarks will obviously apply to a syllogism in Baroco. Nor is it otherwise with the remaining moods. If No

¹ e.g. in this syllogism in Festino, 'No fragrant flowers are scaled, Some genations are not fragrant,' I think a man would probably substitute in thought for the major its converse, 'No exarlet Rowers are fragrant,' and argue to himself in Ferio. With such a premise, where there is no priority as between the two accidents, fragrant and soarlet, that is the more natural way to argue. But this does not show that all syllogisms in Festino ought to be thus treated.
'Called by Aristotio sweepsy's riv difference in the distriction of the state of the st

fish has lungs, and Whales (or Some aguatic animals) have lungs, then Whales (or Some aguatic animals) are not field. A man sees at once that if they were, they would not have lungs; whereas they have.

It might be said that the last conclusion could be as naturally reached in the first figure : that if a man, confronted with the conclusion that Whales are not fish, and not feeling that he was clear about its covency, were to ask himself 'Why not?', he would answer 'Because they have lungs'; and that this implies a syllogram in Barbara, with the major premiss What has lungs is not a feel. Whather this gives the reason why a whale is not a fish (in which case Barbara would be a better way of proving it) we need not dispute: but there certainly are cases where, in what a subject is, we can find a reason for its not being something else. Notes that produce beats are not harmonious: The fourth and fifth produce beats: Therefore they are not harmonious. This argument might be set forth in the second figure : Harmonious notes do not produce beats: The fourth and fifth produce beats; Therefore they are not Agenonious: but here undoubtedly the syllogism in Barbara is better than the syllogism in Cesare : and any one who knew that concord was dependent on regular coincidence in vibrations and discord on the absence thereof, would extricate from the major premiss of the latter syllogism the major of the former, and think in Barbara. Nevertheless it is only this knowledge which makes him do so: and without it he might perfectly well validate to himself his conclusion by considering that if those notes were harmonious, they would not produce the beats they do. If the middle term gives a ratio essendi, we naturally put our reasoning into the first figure.1 The Chinese are not admitted into the United States, for fear lest they should lower the white labourer's standard of living. The likelihood of their doing this is the cause of their exclusion. It would be unnatural to express this in Cesare-

None admitted into the United States are likely to lower the white labourer's standard of living

The Chinese are likely to lower it

. The Chinese are not admitted into the United States.

But we are not concerned to prove that no arguments expressed

¹ It must not be forgotten that most reasoning which explains facts through their causes is not syllogistic at all; but if it is syllogistic, it will be in the first figure.

in the second figure are better expressed in the first : only that there are arguments which are more naturally expressed in the second and which we should not if challenged attempt to validate by reduction to the first. Thus I may argue that Notes which produce beats are not harmonious, and A note and its octave are harmonious. . They do not produce heate: and it is as much a distortion to put this into the first flours by conversion of the major premise as to not the previous example which used that major premise into the second figure by the same means. Again, if I give, as a reason why whales are not fish, that they have not the characteristics of fish, such as breathing through oills, laving eggs, &c., my syllogism may very well be in Camestres All fish breathe through ville, and Whales do not .: A whale is not a fiel : if I still ask myself why not. I should probably answer, Because if it were a fish, it would breathe through wills, which it does not do.' The conclusion states a fact of difference between two things, which the premises prove but do not account for: and the proof in the second figure may be said to be here the primary form.1 Moreover, if I were to recur to the first figure in order to establish this inference, it would naturally be by contraposing the major premiss

What does not breathe through gills is not a fish
Whales do not breathe through gills
Whales are not fish

for the absence of a feature essential to any fish may be treated as explaining why a thing is not a fish. But the syllogism to which Camestres is supposed to be reduced is not the above; it is the following—

What breathes through gills is not a whale

A fish breather through gills

from which the original conclusion that a whale is not a fish is recovered by conversion. Now this argument, instead of relying on something in whales (viz. the absence of gills) to show that they are not fish, relies on something in fish (viz. the presence of gills) to show that they are not whale; whereas whales are really the

¹ Hence the statement, frequently quoted from Lambert (News Organon, vol. ii. p. 189; Dismoislopie, iv. § 229. Leipnig, 1764), that the second figure points us to the differences between things: 'Die sweite Figur führt auf den Unterschied der Dinge, und hebt die Verwirrung in den Begrüßen auf.'

subject of my thought. The same line of reflection may be applied to the argument. Matter containing actine bacilli outrefies: Prozen ment does not mutrefy . It contains no active bacilli: where no one could maintain that non-naturfaction was really the cause of matter containing no estive besilli

Thus the second figure is really different in tune from the first . although reasonings which would naturally fall into the first may he thrown into the second. And the difference is this that the second is essentially indirect, the first direct. In the second we see the validity of the conclusion through the contradiction that would he involved in denvine it: in the first (though of course it would he equally self-contradictory to admit the premises and deny the conclusion) the perception of this is not a 'moment' in our thought. It may fairly be said that the first figure is prior to the second, in the sense that it is involved in the perception of the contradiction which would result from denvine the conclusion in the second. But that does not justify us in reducing the second to the first. For it is an essential part of our thought in the second figure, to see that the conclusion must follow on pain of contradiction; and not merely to see the validity of the first-figure syllogism, by help of which the contradiction, that would follow on denvine the conclusion, is developed. There is therefore a movement of thought in the second figure which is absent from the first. This is what prevents our reducing it to the first, and makes a new type of it; and this is why

It may be saked, is even indirect reduction necessary? Is not the validity of the argument plain, without our being at pains to show that, if it were disputed, we should be involved in a contradiction? Cannot a man appreciate that if No A is B, and C is B, then C is not A, without the necessity of pointing out that C would not otherwise, as it is, be B? The answer is that a man may certainly not require this to be pointed out, inasmuch as he sees it at once to be involved in the premisses. The so-called indirect reduction is really a part of the thought grasped in the syllogism; not something further, by which, when a man has already made his inference, and realized the act of thought involved in making it, he then proceeds to justify his act. It rather brings out what is in the inference, than reduces or resolves it into another. Hence a man may feel it

its direct reduction, representing second-figure syllogisms as only first-floure syllogisms in disquise, is wrong, and therefore superfluous. to be unnecessary, but only because it is a repetition, not because, if he did not see it, the syllogism would still be seen to hold without it.

Yet it must not be supposed that a form of argument is valid only because to question it would involve a contradiction. With equal reason it might be said that unless the argument were valid, there would be no contradiction in rejecting it. Hence the perception, in the second figure, of the contradiction that would ensue if we denied the conclusion, is not the reason for admitting the conclusion, but only involved in realizing its validity. An analogy may help us.



If a straight line, falling on two other straight lines, makes the exterior and the interior and opposite angles on the same side of it equal, the two lines must be parallel. Strictly speaking, this cannot be proved by reasoning; we just see, when we try to draw the figure otherwise, that it

must be so. But this necessity may be brought out indirectly by the consideration, that if BEF were to be greater than BCD, EF and CD would cut AB at a different slant, and therefore incline towards one another; and the perception of this is really part of seeing the necessity of the original proposition. Nevertheless it cannot be given as a reason for the truth of that proposition; for unless the lines were parallel when the angles BEF, BCD are equal, they would not necessarily tend to meet when each cuts A B at a different slant. The confirmation, such as it is, is obtained by looking at the same matter from another side : and so it is in the second figure of syllogism. The truth of one side cannot really be separated from the truth of the other, and therefore the one is not dependent on the other; but it is not fully appreciated without it. The development of the contradiction involved in denvine the conclusion in the second figure is a development of the system of relations between the terms alleged in the premisses, or of the consequences involved in these. It is not, like a suppressed premiss, something without the consideration of which the argument is altogether broken-backed; but it is something involved in the full appreciation of the argument. It follows. if the second figure is not a mere variation of the first, that the principle or canon on which the first proceeds is not that of the second. If the above account of the nature of our reasoning in the second figure is correct, its principle is this, that no subject can possess an attribute which either excludes what it possesses or carries what it avolves

Of the third forms we must give a different account. Its two most noticeable feetures are that the middle term is enhiest in both premisees and the conclusion always particular. For this reseon it has been well called the inductive figure : for induction (whatever else besides their citation may be involved in it) is the attempt to establish a conclusion by citation of instances. The terms of the conclusion are always general. they are what we have called universals. The conclusion declares two general characters to be connected, or (if negative) that one excludes the other: Sailors are handy. The larger carningra do not breed in continity. In the premisees we bring instances of which both characters can be affirmed : or of which one can be affirmed and the other denied; and these instances are our evidence for the conclusion. But the conclusion is not ceneral: we are never justified, by a mere citation of instances, in drawing a really universal conclusion. If All B is A, and All B is C. we cannot say that All C is A: in traditional phraseology, C is

undistributed in the minor premiss, and therefore must not be distributed in the conclusion; and the thing is obvious, without any such technicalities, in an example; if all men have two arms, and all men have two arms, and all men have two legs, it does not follow that all animals with two legs have two arms; for birds have two legs, besides men, and have not arms at all, but wings. Yet, though our instances will never justify a really universal conclusion, they may suggest one; and they will at any rate overthrow one. The instances of Queen Elizabeth or Queen Victoria, of Catherine of Russia or Christina of Sweden, will disprove the proposition that No scowns can be a statement; and truth is often advanced by establishing the contradictory of some universal proposition, no less than by establishing universal propositions themselves.
Now what is the true nerve of our reasoning in such arguments?

It is the instance, or instances. We prove that some C is A, or some C is not A, because we can point to a subject which is at once C and A, or C and not A. Unless we are sure that the same subject is referred to in both premises, there can be no inference: done arisinal are quadrapeds, and done assimals are overlevates; but they might be different animals, and then there would be no instance of

a wortehrate that had four love. But if either premise is universalif a c. with manual as our middle term, we take the premises flower mammale are anadouneds and All mammale are perishrates—then it follows that Some pertalegates are anadeuneds: for the 'some' mammals of the major premise are included among the 'all' of the minor, and therefore we could nick out, from among the latter, instances of animals that were both vertebrate and quadruped. The instances. however, instead of being vacually indicated as 'some' of a whole class or kind, may be specified by name : and then the nature of our reasoning is unambiguous; we are manifestly arguing through instances. In order to show that A woman may be a statesman, we can anneal to the four queens mentioned above : these were statesmen, and these were women; and therefore some women have been (or women may be) statesmen. But whether the instances in which C and A are united, or C is present without A, be cited by name, or only indicated as 'some' of a whole class, in both cases alike it is on them that the reasoning hinges, and it is by producing them that a scentic could be confuted, who refused to admit the conclusion.

Aristotle called this production of the instance by the name Influence, or Exposition. He conceived that the proper mode of validating a syllogism in the third figure was by direct reduction 1. but added that it was possible to validate it per impossibile or by 'exposition': 'if all S is both P and R, we may take some particular S. say N: this will be both P and R. so that there will be some R which is P 1'; and what is possible where both premisses are universal and affirmative is equally possible in any other mood. This seems to exhibit the real movement of thought in the third figure better than the artificial process of direct reduction. For, in the first place, if the middle is a singular term, as in this figure it often is (though Aristotle took little note of such cases), the conversion of a premiss is forced and unnatural. In words I may say that since Queen Elizabeth and Queen Victoria were statesmen. and some women were Queen Elizabeth and Queen Victoria, therefore women may be statesmen; but in thought, Queen Elizabeth and Queen Victoria will still be subject in the minor premiss. And secondly, even where the middle is a general term, direct 1 Except, of course, where the major premiss is a particular negative and the minor a universal affirmative proposition (Bocardo), in which case we can only proceed per impossibile or by exposition. Anal. Pri. a. vi. 28s 15-21.

**Anal. Pri. a. vi. 28° 24-28.

reduction often conceals rather than expresses our thought. No ostrick can flu. All ostrickes have wings .. Some winged animals cannot Are here though it is possible to substitute for the minor premise Some winced animals are ostrickes, the other is the form in which we naturally think . the more concrete term stands naturally as the enhiert of our thought.

It may be admitted that there are cases where direct reduction is unobjectionable. No clerownen may sit in Parliament, and Some electronen are electors to Parliament .: Some electors to Parliament may not sit in it. Here it would be as natural to say that Some electors to Parliament are electorumen: for the franchise, and the clerical office, are each an 'accident' of a man, and either can equally be the subject of the other. But the character of the argument seems changed by this alteration. Clerowers are no longer the instance which shows that a man may be entitled to vote without being entitled to sit: the middle term is now a status in virtue of which certain voters cannot sit. The point contended for is not that there may not be syllogisms in the third figure, whose conclusion could be equally well, or even better, obtained with the same middle term in the first: but that the movement of thought characteristic of the third figure is not, and cannot be reduced to, that of the first; and that reduction, as a general principle, is therefore superfluous and misleading; the true confirmation of the validity of the syllogism lying in the perception that there actually are instances of its truth.

One objection to this view of the third figure needs consideration. It may be said that the production of a particular instance in support of the conclusion does not do full justice to the grounds on which we accept it, in cases where the middle term is general and both premisees universal. All horned animals ruminate, and they all part the hoof : this, it may be urged, is better ground for concluding that cloven-footed animals may be ruminants, than if I merely appealed to the case of the cow in my paddock. To settle this, let us look for a moment at the two meanings, which (as we saw before) may be intended by a particular proposition. If I say that Some C is A. I may either mean to refer to certain unspecified but definite members of the class C, and predicate A of them; or without any special thought of any particular case, I may mean to declare the ¹ Cf. supra, pp. 158-160, 179,

compatibility of the two characters, C and A, in one subject. In the latter case, I can also express my meaning by the problematic judgement C may be A; which contains no doubt the thought of unknown conditions under which it still be so. Now supposing I understand the proposition in the latter sense, the cow in my paddock is as good a middle term as borned animals generally; supposing I understand it in the former sense, then my conclusion, that the conservation of the content of the content of the when for middle term I refer only to a cow or two in a neighbouring paddock. But it is also really a different conclusion; the 'some' intended are a larger number of unspecified animals in the one case than in the other; and it is only by the production, or 'expection', of all the instances to which our 'some' refers, that the reference to them all, in the conclusion, may be justified.

It may fairly be said that the argument, in this view of it, does not really amount to a syllogism: it comes to this, that if all horned animals ruminate, and all part the hoof, then all clores-footed assistate that are horsed ruminate. If the exact sphere of the conclusion is thus borne in mind when we say that some cloves-footed assistate ruminate, and we means by some all that are horsed, there is not really and in thought that elimination of the middle term in the conclusion which is characteristic of syllogism. It would not be reckoned a syllogism five argued that since Wolsey was a cardinal and Wolsey was chancellor, he was both chancellor and a cardinal i, neither is it a syllogism (though it is inference) to argue, from the premisees above, that all horned animals are both ruminant and cloven-footed i from which it follows that all cloven-footed animals that are horned are ruminant.

We may admit the view of the last paragraph to be the right one. Supposing that when we conclude, in the third figure, that Some B is (or is not) A, we refer in thought, though not in words, just to those particular instances, and no others, which in the premisses were stated to be both B and A (or not A), then we have not got a proper syllogism. Still our conclusion rests entirely on the production of those instances, few or many, beyond which our thought refuses to travel. The true and characteristic syllogism in the third figure, however, intends its conclusion in the other sense:

¹ Cf. Bain's Logic, Deduction, p. 159 (ed. 1870).

as a problematic judgement, a statement of the compatibility of two attributes, or the possibility that one may exist without the other. And to establish this too it relies on the production of an instance - nor are many instances really more sufficient than one to establish mere compatibility except as minimizing the risk of malohervation. The instance need not indeed he an individual. it may be a kind. If we want to unwe that an evergreen may have conspicuous flowers, we can cite the rhododendron and we may mean by that the species, and not any particular specimen 1. But very often, and mostly where one premise is particular and of course always where the premisses are singular, it is on an individual instance that we rely; and one instance, whether individual or species, is enough. Therefore it is by exposition-by a production, not of course in hadily form, but in thought, of one instance—that we justify the inference to ourselves; we actually make this appeal in our minds, if we realize the ground of our conclusion. Persons familiar with a type of reasoning may draw conclusions from premisees as it were by precedent, and without realizing the evidence on which they act: but whenever we are fully conscious of what we are about, there is, in the third figure, the recognition that the conclusion is proved by its exemplification in a case cited, or included in what we cite.

Of course there is a way in which the number of instances makes a real difference to the conclusion which we are inclined to draw. The case of Prince Bladud is alone enough to show that a man who washes in the waters of Bath may recover of a disease. The two events, however, may be accidental and unconnected. But if cases were multiplied, we should begin to suppose there was a connexion between the use of these waters and the cure of certain ailments: or if the ailments which disappeared after taking the waters were of

¹ It may be objected that it is only in some particular specimen that the coincidence of these two characters is ever actually realised, and that there rei it is to a specimen that we must at bottom be referring. This raises a question that is not peculiar to the third figure. If I argue that the rhodocadron is popular because it flowers brillandly, it may be said that this truth is only realized in particular shrubs. The relation of the universal truth to particular artistence, here raised, is important; but it need not

crust to particular antennes, new raised, is important; but it need not complicate the present issue.

* Not always, even there; I may argue that all breeds of dog are domesticated, and some are sewage, and therefore some domesticated breeds of animal are sewage (Disamis). Here I am speaking, and thinking, throughout not of individual salminals but of their kinds.

all sorts, we might begin to look on Bath waters as a nanacea. For establishing a connexion between two attributes the numberand variety of instances are matters of great importance; but for establishing competibility one instance is anough. Now the third forme does not prove more than a competibility and never can prove a connexion however many the instances are and though the number of instances may make a connexion highly probable. vet we are influenced in reaching such a conclusion by other considerations besides the instances themselves. For example a man who observed in several cows the combination of the cloven foot with the ruminating stomach would be much less inclined to suppose that there was any general connexion between these characters in nature, than if he had observed the same thing in an equal number of beasts belonging to as many different species. For we are accustomed to find peculiarities constant throughout one species, and failing when we go beyond it: so that the accumulation of instances would be discounted by the fact that they all belonged to the same kind. Again, we might meet a Privy Councillor in a light suit and yet not be led to regard the next man we met in a light suit as a Privy Councillor; but if we met a Guardsman in a breastplate, we should very likely suppose the next man in a breastplate to be a Guardsman. The readiness with which we infer connexion is controlled by our general knowledge of the kind of attributes that are connected; such considerations do not appear in our premisses, but greatly influence our thought. Hence it is, that those who are thoroughly familiar with the facts of a science, or of some historical period, can make inferences from isolated facts which to persons ignorant of the field of investigation, and the controlling principles applicable to it, appear foolhardy. But all this belongs to rather a different department of logical theory, the Logic of Induction. It remains true that so far as we bring no extraneous considerations to bear, and are guided only by the facts contained in our premisses, we can infer no more than the compatibility of two characters (or the possibility that one may appear without the other) from any number of instances; and we can infer thus much from a single instance.

It should be noticed, before leaving the consideration of the third figure, that it always argues from a ratio cognoscendi. It is not because the rhododendron has brilliant flowers, that this attribute can be combined with evergreen foliage: if it were not that there is no incompatibility between them, the rhododendron could not exhibit both. Our instance merely teaches us that the two are competible, it is the ground of our essertion not the ground of the fact asserted. And this in itself is enough to show that there is a real difference between the nature of our reseasing in the third figure, and in the first-at least when our syllogisms in the first figure are scientific; and that the attempt to reduce all syllogisms to one typical form imposes an unreal appearance of conformity upon aronments which are essentially disparate

The fourth figure of syllogism remains for consideration. 1 It has this peculiarity, that its premisses as they stand, if we transpose them, present the arrangement of terms required by the first tigure. And three of its moods (Bramantip, Camenes, and Dimaris). when thus regarded as being in the first figure (= Baralipton, Celantes. Dabitis), afford conclusions of which those drawn in the fourth figure are merely the converse; but the other two moods (Fesapo and Fresison) yield no conclusion in the first figure, from which the conclusion in the fourth might be obtained. Are we therefore to repard this figure as presenting a separate type of inference from the first, or was Aristotle right in disregarding it?

Let us look first at the moods which are reduced to the first figure by a mere transposition, and without any alteration, of the premisses. In the premisses All nitrogenous foods are flesh-forming,
All grains are nitrogenous, if we treat flesh-forming as the major term. we have a syllogism in Barbara; but if we treat grains as major term, our syllogism is in Bramantip, and the conclusion is that Some flesk-forming foods are grains. It is surely true that the cogency of this inference, as compared with the other, is peculiarly unobvious. The conclusion is not what we should naturally draw from the premisses; and we need to look a little closer, in order to convince ourselves that it necessarily follows. And this conviction comes to us when we realize either that from the given premisees it follows that all orgins are flesh-forming, and our other conclusion follows by conversion from that : or else that if no fleshforming foods were grains, no nitrogenous foods would be grains ; and that in that case grains could not all, or any, of them be nitrogenous. The same remarks would apply mutatis mutantis to syllocisms in Camenes or Dimaris: and we may therefore conclude that

¹ This note may, of course, be equally well regarded as a discussion of the indirect moods of the first figure. But if a new type of inference were movied in them, the erection of a fourth figure would be justified. As that is the question under discussion, it seems fairer to call them moods of the fourth figure at the outset.

these moods are not evidently cogent without a further act of thought than their formulation in the fourth figure displays. Are we therefore to treat them as belonging to the first figure? The reason for doing this is, that the simplest and directed way of justifying the inference which they contain is by drawing a conclusion in the first flower from their newsies, and converting it.

The two remaining moods, Fesapo and Fresison, are less easily disposed of. As the same considerations apply to both, it will suffice to take an example of the former. No animals indigenous to Australia are mammals. All mammals are vertebrate .: Some pertebrates are not indicenous to Australia if we transpose these premisses no direct conclusion follows: we cannot tell from them whether any of the animals indigenous to Australia are vertebrate, or not : so that if our argument requires validating, we must validate it either by direct or indirect reduction, or by exposition. That it does need velidating seems to follow from the fact, that in its present form it is no more obvious than the three preceding moods of the fourth figure: no one ever argues in the fourth figure, and that shows that it does not adequately exhibit the movement of thought in inference. Aristotle exhibited the validity of this mood 1 by converting both premisses (i. e. by direct reduc-tion): No mammal is indigenous to Australia, and Some vertebrates are mammale: and this is a more natural way of putting the aroument. But there are cases in which conversion would substitute a less natural mode of expression in the premisses : e. g. from the premises No mineral scaters are alcoholic and All alcohol is taxed 2 we can infer that Some things taxed are not mineral waters : it would be less natural, although it would vield the same conclusion, and that in the first figure, to say that Nothing alcoholic is a mineral water, and Some things taxed are alcoholic. Again we may proceed by indirect reduction: we may argue that if all vertebrates were indigenous to Australia, then since no animals indigenous there are mammals, no vertebrate would be a mammal; we thus reach a conclusion inconsistent with the premiss All mammals are vertebrate. and that shows that our original argument cannot be disputed ; but we should more naturally say that No mammals are vertebrate than that No vertebrates are mammals: and the former contradicts more directly the premise that All mammals are vertebrate; and still more do we feel this, if we apply indirect reduction to our other example; there, if Everything that is taxed were a mineral water, then since No mineral waters are alcoholic. Nothing taxed is alcoholic: it is clearly more natural to say that No alcohol is taxed,

i.e. of Fapesmo and also Fresison - Frisesomorum: v. Anal. Pri. a. vii. 29-21-27.

³ It would complicate the illustration too much to make the exception required by methylated spirits.

fand that exhibits better the contradiction with our premise. If we employ the method of Enferce or exposition, we must convert the premies No asimale indicenous to Australia are mammale: then we have it given that mammals in any instance that we like to take are not indigenous to Australia, and are vertebrate: from which it follows that an animal is sometimes vertebrate, and not indigenous to Anstralia. Similarly we may convert. No mineral scatters are alcoholic.

Thus we have in this mood an argument undoubtedly valid, yet lacking something to be obvious; it is possible to validate it in several wave either bringing it into the first figure by conversion of both premisses, or into the third by conversion of one, or leaving the premises and showing as in the second figure that the falsity of the conclusion is inconsistent with their truth. Which of these methods is preferable? and to what figure should the mood be referred? or is it really of a fourth sort? That it is not of a fourth sort is shown by the fact that without one of these methods of validation its conclusiveness is not apparent, and they bring it under one of the other figures. Perhans the first of these questions will be best answered, if we ask in what way, by the use of the same middle term, the conclusion of the given syllogism could most naturally be reached. How are we to prove that Some vertebrates are not indigenous to Australia, using mammals as our middle term? or that Some things taxed are not mineral waters, using alcohol as middle term? In both cases we should appeal to an instance in point; the mammals may be cited to show the former, and alcohol to show the latter. It would seem therefore that exposition is the natural way of validating the argument: or in other words, that we realize its cogency most readily if we realize that in the major premise there is involved a converse, from which the conclusion follows at once in the third figure.

Are we then to reakon the mood to the third figure, and not (with Aristotle) to the first? Aristotle would, of course, have said that since the third figure itself needed validating through the first, we had stopped half-way in reducing it to the third; but if, as has been held above, the third figure is really a different type of inference, our question cannot be settled thus. Let us recall the meaning of the distinction between major and minor terms. The distinction is not purely formal and external. A term is not really the major term because it is made the predicate, and minor because it is made the subject, in our conclusion. It is the meaning or content of the terms themselves which determines which owalf to be subject, and which predicate, and therefore which is major and which minor. Otherwise, Aristotle would have recognized the fourth as a separate figure. We may take a syllogism in Darii, and by transposition of the premises produce one in Dimaris; e. g.

The premises White is conspicuous at night. Some flowers are white whose natural conclusion is that Some flowers are conspicuous at sight, furnish instead, if we transpose the premisees, the conclusion that Some things conspicuous at night are flowers. But this is an abvious inversion for it is the flower which is conspicuous and not the conspicuous as such, which is a flower. It is true that there are cases where either conclusion is squally natural, as there are propositions which may be converted without contortion. These who are friendless are unhappy, Some rich men are friendless ... Some rich men are unhappy; or, in Dimaria. Some unhappy men are rick. Here the conclusion in Darii is the natural conclusion to draw, because the premisses give the reason why a rich man is sometimes unhappy, but not why an unhappy man is sometimes rich : vet. considered apart from the premisses, either conclusion is an equally natural form of judgement. But the reason is, that the concrete subject men is retained throughout : in the conversion, the attributes rick and sudgery change places, but the subject of which they are attributes is retained in its place. Now these are merely coincident attributes, and neither is properly the subject of the other; we feel this in making the judgement; and instinctively convert Some rich men are unhappe not into Some unhappe are rich men (where the concrete term 'rich men' could not be predicated of 'unhappy' as such) but into Some unhappy men are rich. When, however, this is not the case-when the subject-concept contains the ground of the predicate-concept, or is the concrete whole in which the latter inheres as one feature—then the former is essentially the minor and the latter the major term, and no verbal artifice which inverte them can alter what the fact is for our thought.

Hence in the first three moods of the fourth figure, reduction to the first does no more than recognize in outward form as major and as minor terms what we must acknowledge to be so in our thought. But in Ferano and Freeison, the conclusion is the same as what we should draw in Ferio after their reduction, and not its converse. we have therefore no ground so far for giving a preference to the expression of the argument in the first figure. But the same considerations which make it not an arbitrary matter, which term is major and which is minor in the conclusion, will help us to determine the right position of the middle term in the premisees. If then the premises of a syllogism in Fesapo or Fresison were both of them inversions of what would naturally be expressed in the converse form, we should instinctively think them back into the form required by the first figure, in drawing the conclusion. This can hardly be the case with Fesapo ; for bad logic, as well as verbal contortion, is required in order to express a particular affirmative by an universal converse; and therefore the minor premise A cannot be an inverted way of stating I: the original of Fempo cannot be

[Ferio. With Fresison it is more possible; that is to say, a syllogism in Fresison may be reached by converting both premisees of one in Ferio (or Celarent); and then it is possible that our thought may validate the conclusion by converting them back nomin. Gold does not tarnish. Some ancient ornamente are of cold: we may, however, say, if we like, that What tarnishes is not cold. and Some things of gold are ancient ornaments, and from these premises draw the same conclusion as from the others, that Some ancient ornaments do not tarnies; yet our thought, justifying to itself an inference made by outward rule, may fly to the other forms of premiss. If so, it is hard to say that we are not really arguing in the first figure, and in such a case the syllogism which wears externally the carb of the fourth belongs really and is rightly forced by direct reduction to show that it belongs, to the first. It is, however, possible even here to convert only the minor premise in thought, and reach the conclusion in the second figure : by realizing that ancient ornaments, if they tarnished, would not be of gold. But the important cases are not such as these, where the premises are palpably in an unnatural form, and would be restored to

natural form by conversion. They are those in which the position of the middle term, as the predicate of the major premiss and subject of the minor, is the natural position. For here conversion to the first figure produces a result as unnatural as there conversion to the fourth figure produced in the premisses of an argument anturally belonging to the first; No misrard sector are accessful and All alcohol is taken are propositions put in their natural form; Nation alcoholic is a misrard water and Nome Lancel Listes are

alcoholia are not. And if that is so, there is only one ground on which we can justify Aristotle in reckoning these moods to the first figure. It is, that what is essentially the major term—that is, the most general and comprehensive—does stand as predicate in its premiss, and what is essentially the minor term—that is, the most concrete and specific-as subject. Hence looking to the character of the premisees. we may fairly say that our syllogism is of the first figure. And it follows that Aristotle is right when he says that we prove the minor, not universally but partially, of the major; for major and minor, as we have seen, are such intrinsically, and not barely in virtue of their position in the conclusion; so that where the two criteria lead to opposite results, it is right to base our nomenclature on the former. It was through overlooking this, and taking a purely formal and external view of the notion of major and minor terms, that some of his successors were led to add a fourth figure to the three of Aristotle. But if we recognize these moods as of the first figure, we must no less recognize that they need validating; and the most natural way of realizing their validity is by the I process of exposition which we found to be the characteristic method for the third. We need not on this account any that the roy of the characteristic process of the characteristic process. The cocurrence of a syllogism of the characteristic and impossible by which we validate the second did not lead us to resolve the second figure into the first. Exposition too, though the most natural, is not the only way in which we can realize to cursalves the validity of these arguments; so that the third figure could not receive them unchallenged. We must be guided, therefore, by the character of the premisers, and assign them to the first; but admit that the conclusion is not really drawn without a further act of inference than appears upon the face of them.]

We may now sum up the results of our enquiry. There are three figures, each with a distinctive character, and the 'imperfect' figures are misrepresented by reduction to the first. The first is the chief because the demonstrative but not because the only figure Arguments in it need not be demonstrative, but when they are, our thought is moving on a higher level of intelligence, though not of copency than in the other figures. In realizing the validity of the second figure, the inconsistency involved in denying the conclusion is a more prominent 'moment' in our thought than the necessity of admitting it. The third figure appeals not to relations of concents, but to experience of the conjunction of attributes (or their disjunction) in the same subject, and from that argues the general possibility, under conditions unspecified, of what is exhibited in a given case. There is no fourth floure: but in the first three moods of the first floure we may also argue to the converse of their conclusions; and two moods may be added, with an universal negative minor premise, in which, while the major term cannot be denied of the minor without fallacy, the minor can be denied of the major; though such a conclusion is only particular, and realized by the help of exposition or of conversion or reduction ad impossibile. It must always be remembered that the character of an argument is determined not By the form into which it is thrown in words, but by that which it assumes in our thought. This is our justification for recognizing the figures as distinct types. In particular cases, a syllogism may not belong to the figure into which it has been verbally compelled : in others, it may be possible with the same terms to construct syllogisms in more than one figure; but then there must be a real movement of thought in the process of conversion by which the change is effected. The theory of syllogism ought not to be regarded as a lesson in the manipulation of symbols and the application of the formulae. What we have to look to is the character of the thinking involved in it, and to that end wo need to realize our symbols and see how the varying character of our terms, and of the relations between them in judgement, affects the inference. If our enquiry has done anything to bring this lesson home, its lenth and intricacy will not have been altocether win.

One more remark may be made about the first figure. We have seen that the charge of petitic fails, unless the major premise be enumerative : but suppose that it states a connexion seen to be necessary between A and B as such : may it not be urged that in this case no one can judge that C is B without co ipeo recognizing it to be A as well? and that if so, there will be no such act of 'subsumption', bringing C under the condition of a rule, as we found the first figure to involve? To this we must answer yes; with complete insight we should go straight from B to A in the subject C. and the major premise as an independent sule would not he wanted and would be represented only by the recognition that a connexion of A with B. which we see to be necessary, is therefore universal. Thus it will be found that in geometry we never syllogize except when we rely on the results of a previous demonstration whose steps we do not realize in the case before us. The triangle in a semicircle has the square on the hypotenuse equal to the squares on the other two sides, because it is right-angled; but if we realized at once the constructions of Euclid i, 47 and iii, 81, the proposition that in a right-angled triangle the square on the hypotenuse is equal to the squares on the other two sides would appear rather as generalized from what we saw to be true in the triangle in a semicircle, than as a rule applied to that case. The subsumption in avilorism belongs therefore to thinking which has not complete insight into the grounds of all its premises at once.

CHAPTER XV

OF HYPOTHETICAL AND DISJUNCTIVE REASONING

THE form of argument which we have been examining under the name of Syllogism has for its premises only categorical propositions; but there are forms of argument to which the name has been extended, in which this is not the case. In what have been called Hypothetical and Disjunctive Syllogisms, hypothetical and disjunctive propositions figure in the premises. For reasons to be considered later, it appears, however, better not to call them syllogisms, but to speak rather of hypothetical and disjunctive arguments. They are processes of argument that recur with great frequency both in ordinary thought and in the reasonings of serience.

In a hypothesical argument, one premise is a hypothesical proposition, connecting a consequent with a condition or autocedent: the other is a categorical proposition!, either affirming the antecedent or denying the consequent. From these follows as conclusion a categorical proposition, either affirming the consequent or denying the antecedent. In the former case, an argument is said to be in the moduse ponens or constructive: in the latter case, in the modus tollens or destructive. Examples will make this clear.

1. The modus posens is of the form

e.g. If the soul is uncreated, it is indestructible
The soul is uncreated

.. It is indestructible

or

If all men are born equal, slavery is unjust All men are born equal

... Slavery is unjust.

1 But of. infra, iii, p. 810.

The following points should be noted further :--

i. The subject of the minor premiss may either, as in the foregoing examples, be the same as the subject of the antecedent in the major premise (if we may retain the name of major for the hypothetical and of minor for the categorical premises in this form of argument), or it may be a term that we recognize as included therein, falling under it. Thus we may arout that:

If a heautiful thing is rare it is costly

Diamonda are rare

... They are costly.

Here it is implied and recognized that diamonds are beautiful things.

The argument might of course be expressed

If anything is at once beautiful and rare, it is costly Diamonds are at once beautiful and rare

.. They are costly.

But diamonds are still 'subsumed' as a special case under a rule that applies beyond them; the condition in the major premise does not concern them is particular.

ii. We saw in a previous chapter that the distinction of affirmative and negative has no application to hypothetical judgements—for every hypothetical judgement connects a consequent with a condition, whether that consequent itself be expressed in the form of an affirmative or of a negative statement: it would be no hypothetical judgement to say that 'If the weather changed at full moon, it does not follow that the change will last'! Hence the character of the modus powers is unaltered, whether the antecedent or the consequent (and therefore the conclusion) be affirmative or negative. I may argue

If the North American colonies were unrepresented in Parliament, they ought not to have been taxed by Parliament

They were unrepresented in Parliament

.. They ought not to have been taxed by Parliament.

Here my conclusion is negative; but the argument is still in the modes posses: for by that is meant not the mood which is affirmative in its conclusion, but the mood which establishes the consequent set down in the major premiss. The reader will easily see that if

¹ This is the denial of a hypothetical judgement, but not itself hypothetical: being equivalent to saying 'It is not true that if', &c.

the antecedent were of the form 'If A is not B', it would still make no difference to the character of the argument.

iii. It is possible to argue with both premises and the conclusion

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If A is C, it is D or If C is D, B is F

If A is B, it is C If A is B, C is D

... If A is B. it is D ... If A is B. E is F
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e.g. If the price of an imported article rises, those who manufacture
the same article at home will charge more for it.

If a tax is imposed upon the importation of an article, the price
of the imported article rises

.. If a tax is imposed upon the importation of an article, those who manufacture the same article at home will charge more for it.

The remarks made in the last paragraph apply mutatis mutandis to this form of the modes posses also; and the subject of the antecedent may be in one premise the same with that of the consequent, and in the other different. It is unnecessary to illustrate all these variations.

2. The modus tolleus is of the form :-

If
$$A$$
 is B , it is C or If A is B , C is D

A is not C C is not D

This not C A is not C

e.g. If matter is indestructible, it is uncreated

· It is not indestructible

or If the earth did not rotate, the winds that blow from the poles
to the sountor would not be deflected westward

But they are deflected westward

. The earth does rotate

It is plain that the observations made above with regard to the modus poneus are equally applicable, mutatis mutandis, to the modus tollens.

Thus, given a hypothetical proposition, we can proceed to draw an inference whenever we have a further premiss given us, either affirming the antecedent or desping the consequent. But from the affirmation of the consequent, or the denial of the antecedent, no conclusion follows. Arguments of the form If A is B, it is C
A is C
∴ It is B
A is not B
∴ It is not C

are invalid. It is true that if a member of the Commons House of Parliament is declared a hankrunt he loses his seat but it is not true that if he loses his seat, it must be because he has been declared a bankrupt, or that if he is not declared a bankrupt, he may not still lose his seat. For the connexion of a consequent with a condition does not preclude the possibility that there are other conditions upon which the same consequent may follow: so that the fact of the consequent having occurred is no proof that it occurred in consequence of this particular condition: nor is the fact that this particular condition is not fulfilled any proof that the consequent has not occurred in virtue of the fulfilment of some other condition with which it is connected. Obvious as these considerations are vet these are among the commonest errors to occur in men's reasonings. We are all of us ant to conclude, that by disproving the allegations advanced in support of a proposition, we have disproved the proposition itself or that by showing that facts agree with the consequences of some hypothesis which we have formed, we have established the truth of that hypothesis. We do not realize that it would be necessary to show, not only that the facts agree with the consequences of our hypothesis, but that they do not agree with the consequences of any other. The Teutonic races have during the last three centuries increased and expanded faster than those which speak languages of Latin stock; and some may be inclined to attribute this to the fact that the former in the main embraced, while the latter rejected, the principles of the Reformation. Grant that the facts are consistent with the hypothesis that this difference of growth is due to a difference of religion : yet if there are other ways of explaining it, what ground has yet been shown for accepting that way? When facts are equally consistent with the truth and with the falsity of our hypothesis, we have so far no reason for believing it true.

It is then fallacious to draw any inference from the affirmation of the consequent, or the denial of the antecedent, in a hypothetical argument. It is sometimes said that to do the former is to commit the fallacy of undistributed middle; and to do the latter, to commit the fallacy of illicit process of the major term: for that the argument

and the argument

... A is not C

may be exhibited in the form A B is C

And valid hypothetical arguments, it is said, may be similarly 'reduced' to categorical syllogisms; when it will be found, that the modus poneus is really a syllogism in Barbara, and the modus tollens one in Camestrea.

It seems to be an error thus to identify hypothetical reasoning with syllogism. In syllogism, as we have seen, a relation is established between two terms in the way of subject and predicate, by means of their common relation in the way of subject and predicate to a third or middle term. Hypothetical reasoning rests upon another relation than that of subject and predicate—the relation of logical dependence; and there is not necessarily any middle term. Where antocedent and consequent, in the hypothetical premiss, have the same subject—where that proposition is of the form 'II A is B, it is C'—a middle term may at times be found, and the reduction effected; but where that is not so—where it is of

¹ A number of modern textbooks teach this doctrine. For an older authority of Zabarella, in Lib Prior. Anal. Tabules, p. 158, 'syllogiamus hypotheticus as valest neces cognosciur per cius reductionem ad categoricum.' — Oprus Logine, Coloniac, 1587.

the form 'If A is B, C is D'—there a middle term is wanting, and the violent nature of this process of reduction becomes manifest.

'If the value of gold is affected by the amount of labour needed to obtain it improvements in mining machinery must miss prices The value of gold is affected by the amount of labour needed to obtain it. Therefore improvements in mining machinery raise prices. We are not concerned here with the truth of this hypothetical proposition. So many circumstances, many of them varying independently of one another, combine at any time to affect the comme of prices that it would be hard to rest on observation the effect which it is here asserted that improvements in mining machinery quest to have. Our concern, however, is with the character of the argument: it is clearly difficult to reduce it to a syllogism. There is nothing seserted of improvements in mining machinery, which in turn is asserted universally to raise prices; the connexion between the value of gold and the amount of labour needed to obtain it is not a predicate of improvements in mining machinery, nor is raising prices a predicate of that connexion. It is a consequence of it: but that is another matter. Attempts have indeed been made to get round this difficulty. It is said that the major premiss may be expressed in the form 'The case of the value of gold being affected by the amount of labour needed to obtain it is the case of improvements in mining machinery raising prices. The existing case is the case of the value of gold being affected by the amount of labour needed to obtain it. Therefore the existing case is the case of improvements in mining machinery raising prices.' But such linguistic tours de force do not alter the nature of the argument which they conceal. What does that major premiss mean? Interpreted literally, it is undoubtedly false. Modification in the value of gold, because gold has become easier or harder to obtain, is not a rise in prices due to improvements in mining machinery. The one fact may be dependent on the other, but the one is not the other. It is not therefore until we mentally substitute for this premise the hypothetical proposition it attempts to supersede, that we assent to it at all: the 'reduction' is purely verbal; our meaning remains unchanged, and cannot be put into

¹ Had I written, for the case, all cases, the proposition would have been still more absurd. But the contention should be examined in its strongest form.

the categorical form. Nor does the minor premise stand criticism any better. What case is 'the case of the value of gold being affected by the amount of labour needed to obtain it? To my the existing case is useless, unless we are told what the existing case is a case of If it is a case of the value of gold being affected by the amount of labour needed to obtain it, the proposition becomes tautological and the conclusion will only repeat the major premise 1: if it is a case of something else, we ought in the first place to have that something stated, in order that we may know what the proposition means; and in the second place, when it was stated, we should find the proposition had become false, in the same way as the major premiss, literally interpreted, was false, It is clear then that this syllogism is far from exhibiting more correctly the true character of the hypothetical argument in question: on the contrary, the hypothetical form exhibits the true nature of the argument thus violently forced into a syllogism.

Had we indeed taken an example in which the subject of the antecedent was the same with the subject of the consequent in the major premise—in which, to put it otherwise, the major premise was of the form 'If A is B, it is C': then the process of reduction to syllogism would not have appeared to be so difficult or violent. For then the condition on which it depends that A is C is a condition fulfilled in A. 'If the moon rotates in the same period as it revolves, it must present always the same face to the earth. 'If the control is the control in the same period as it revolves. Therefore it does present always the same face to the earth.' 'If Christian nations had the spirit of Christ they would avoid war. They do not avoid war. Therefore they have not the spirit of Christ.' There is little change made, if we substitute for these arguments the following syllogisms:

A body rotating in the same period as it revolves in round another body presents always the same face to the other

The moon rotates in the same period as it revolves in round the

.. The moon presents always the same face to the earth

^{&#}x27;The case of A is the case of B: the existing case of A is the case of A: therefore the existing case of A is the case of B.
'It will be seen that in this minor premise not only is the meon 'unbeumed' under the more general notion of a body rotating, &c.: but

Those who have the spirit of Christ avoid war Christian nations do not avoid war

... Christian nations have not the spirit of Christ.

Indeed, if it be granted that the hypothetical premiss is unaltered. otherwise than in verbal form, by reduction to the form of a catecorred proposition we must grant that the argument is unaltered by reduction. And there are logicians who have contended that all universal independents are really hypothetical 1: from which it would follow that there is no real difference between a syllogism in Barbara or Camestres, when it has a genuinely universal (i.e. not a merely enumerative) major premiss, and a hypothetical argument in the modus powers or the modus tolleus—though the former rather than the latter would demand reduction. Yet there do seem to be some independs which, in their context, intend to affirm the existence of the subject about which assertion is made, and not merely to assert that something would be true about it if it existed. To say that, if Christian nations had the spirit of Christ, they would avoid wer leaves it an open question whether any have that spirit: to say that those who have the spirit of Christ avoid it. naturally implies that there are such. The reduction of a hypothetical argument to a syllogism is no merely verbal change, if it substitutes one of these forms of statement for the other

Attention ought to be called to one other change incidental to this reduction in the last two examples. Our hypothetical major concerned the moon and the earth, or Christian nations; in the syllogism, the major concerned any two bodies in which certain conditions are utilifiled, or any in whom the spirit of Christ is found. Thus in the syllogism, a principle is stated in more general form than in the hypothetical proposition. Here again, more than a merely formal change is involved. It is true that no one could assent to the

the sorb is also subsumed under the more general notion of the other body. Hence it is difficult to arpress the argument completely in symbols. Suppose that we write 'tany X is Y, the moon is X', the moon is Y'; now here in the major premiss. X = 'body rotating in the same period as it revolves in round another body'; in the minor premiss X= 'body rotating in the same period as it revolves in round the earth 'j and similarly with Y. The argument is none the less a syllogiam; the difficulty is linguistic; but we are wally bringing the case of the moson in its relation to the sorth under the condition of a rule. Aristotle recognizes this: of. Post. As. β . xi. 94° 38-19.

1 Cf. p. 166, n. 1, supra.

proposition that if the moon rotates in the same period as it. revolves in it must present always the same face to the earth. without seeing that its truth has nothing to do with the fact that the hodies in question are the moon and the earth but holds equally for any two hodies - so that the more general form of the universal esterorical proposition given shows is obviously instified. Yet it is not the mere form of the hypothetical indoment which enables us to see this and it might be contended in the other case that the more general form of the categorical judgement is not justified, and that we quotit not to have said more than that 'Nations who have the spirit of Christ avoid war'. It might be said that if a Christian nation had the spirit of Christ, it would avoid war: but that an individual may be morally bound to take part in warfare, though he has that spirit, when the nation to which he belongs has it not. Now there is, doubtless, in every true hypothetical independent of the form 'If A is B, it is C', some comeral principle involved : we may express this as 'a B is v'. But if A is some determinate individual, or case of a particular kind, and if the condition B is similarly determinate, we may know that if A is B, it is C, without knowing generally what conditions 8, occurring in what kind of subject a, will involve the predicate v. Where this is the case the hypothetical form is more natural to the expression of our argument than the syllogistic.

We find, then, that even when antecedent and consequent have the same subject in a hypothetical major, reduction of the hypothetical argument to syllogiam may mean a real change in the nature of the argument used; and that where they have different subjects, such reduction can only be effected to outward appearance, and by violent means; for here the condition on which it depends that C is D is not a condition asserted to be realized in the nature of C itself: in other words, there is no middle term. In

¹ The inference in a hypothetical argument might hence be called immediate; but each as expression would readily give not be misunderstanding. It is immediate in the sense of having no true middle term; and in the it differs from syllogism; it is also immediate in the sense, that gives the premises, nothing more is needed in order that we may see the accessity of the conclusion; and in sense, syllogism, and indeed every step of valid argument when fully stated, is immediate. But it was in yet another sense that the processes of conversion, &c., were called immediate, and distinguished from syllogism: vis. that in them we passed from a superposition to another inferred therefrom, without anything further being

doubt there is an unity embracing both condition and consequent . they belong to a system of which it might be said that when affected by the condition of exhibits the consequence. Sometimes this admits of ready agreement. (If the rainfall is deficient the hav-crop is light': we may express this by saving that 'Grass which is insufficiently supplied with moisture makes only a small growth that can be used for hav '. In other cases, the interconnexion of facts within a whole does not admit of being stated except in And anyhow, it must be contended that hypothetical form. hypothetical reasoning is not identical in character with syllogism. and that we ought not to pretend to validate it by reducing it to syllogism, nor to identify the fallacies involved in argument from the denial of the antecedent or the affirmation of the consequent with the syllogistic fullacies of illicit process of the major term or undistributed middle.

In a disjunctive argument, one premise is a disjunctive proposition; the other is a categorical proposition, affirming or denying one of the alternatives in the former. From these follows as conclusion a categorical proposition, denying or affirming the other atternative. In the former case, the argument is said to be in the

required as a means of reaching the conclusion. Hypothetical arguments are not immediate in this sense. Given that 'If A is B, it is C.' I conclude that A is C, unless A also know that A is B, nor could I conclude that A is C, from the fact that A is B, without the hypothetical premiss. I can, however, conclude from 'If A is B, it C to 'If A is not, it is not B', without any further knowledge: and to this we saw that some forms of so-called immediate inference amounted.

The conditions of ralled hypothetical reasoning are of course recognized by Aristotle (et. a., Tap. B. t. 1111 17-23s et al.), but he does not speak of hypothetical syllogisms. The term only-sepak of isordiorses has a different meaning—it. as syllogism proving the antecedent of a hypothetical proposition, and therefore, by series of the acceptance of that Appendient, proving which proves that A is B will by rittee of this agreement stabilism also that C is D: but without such agreements, it would not have been shown at all that C is D: that is therefore said to be proved only as hypothetic. In a recent case between University College, Orford, and the City of Orford. These of Joly 1994 having out of a chim by the College to put called Logic Lane without payment of any acknowledgment to the City and college to put called Logic Lane without payment of any acknowledgment to the City and power to make); the arguments advanced on behalf of the City and power to make); the arguments advanced on behalf of the City and power to make); the arguments advanced on behalf of the city had power to make); the arguments advanced on behalf of the city had power to make); the arguments advanced on behalf of the city had power to make); the arguments advanced on behalf of the city had power to make); the arguments advanced on behalf of the city had power to make); the arguments advanced on behalf of the city had power to the theorems, the College showed by the same arguments that it was entitled to erest the bridge without schowledgment.

modus ponendo tollens: in the latter case, in the modus tollendo ponens. Examples and observations follow.

1. The modus ponendo tollens is of the form

A is either B or C or Either A is B or C is D

A is B

.. C is not D

Either A or B is C

A is C

- e.g. 'Possession by devils' is either a form of mental derangement,
 - It is a form of mental derangement
 - .. It is not supernatural
- or Either the interests of religion require the maintenance of the Temporal Power, or the Popes are actuated by worldly
 - motives in continuing to claim it
- The interests of religion do require its maintenance

 The Popes are not actuated by worldly motives in continuing
 to claim it.
- or Either Newton or Leibniz invented the calculus
 - Newton invented it
- · Leibniz did not
- 2. The modus tollendo ponens is of the form

A is either B or C Either A is B or C is D Either A or B is C
A is not B or A is not C

A is not B or A is not B $\therefore \text{ It is } C \qquad \therefore C \text{ is } D$

∴ Bia C

e.g. The belief in a golden age rests either on history or on hope It does not rest on history

... It rests on hope

Either God is unjust, or no man is eternally punished God is not unjust

.. No man is eternally punished

or Either Aristotle or Eudemus wrote Bks. v, vi, vii of the

Eudemus did not write them

.. Aristotle did write them.

The following points should be noted :-

i. It is sometimes contended that the modus ponendo tollens is invalid: that the affirmation of one alternative does not justify the denial of the other. This will depend on the interpretation given to the disjunctive proposition. If the alternatives therein stated are matually exclusive the argument is valid . if otherwise it is not Whether they are so intended can only be determined in a given case by reference to the context and the matter of the judgement. but mutually exclusive alternatives may exist, and therefore a valid aroument in this mood is possible. Of the examples given above. the third is clearly the most open to objection: for Newton and Leibniz may well have invented the calculus independently, as is now believed to have been the case. In the first, it is implied that if we can otherwise account for the phenomena of demoniscal nossession, we shall not attribute them to supernatural agency : and the aroument may be considered valid, provided that we are justified in that view.1 The second is more doubtful; men may do from had motives what ought anyhow to be done, and the motives of the Popes in maintaining their claim to temporal power might be worldly, even though their possession of it were required in the interests of religion. The premises do not really prove the unworldliness of their motives: but they show that we need not assume the contrary, in default of further evidence. The validity of the present mood of disjunctive aroument will, in fact, depend on what hypotheticals are implied in its disjunctive premise; for we have seen (p. 167, supra) that the disjunctive judgement 'A is either B or C' may imply, though it is not reducible to, the hypothetical indocuments 'If A is B, it is not C', 'If A is C, it is not B,' 'If A is not B, it is C,' and 'If A is not C, it is B'. If the alternatives are mutually exclusive, all four will be implied, and the modus nonendo tolleus will be valid. If not, we cannot get, out of the proposition 'A is either B or C', the propositions 'If A is B. it is not C'-' If A is C. it is not B'. To say that 'Either the interests of religion require the maintenance of the Temporal Power. or the Popes are actuated by worldly motives in continuing to claim it' will mean that if the interests of religion do not require it, they

¹ The argument may be valid even though the conclusion be false: the truth of the conclusion further presupposes that of the minor premiss.

must be so actuated; but not that if the interests of religion do require it, they cannot be so actuated; and therefore to argue from the premise that the interests of religion do require it is to argue from the denial of the antecedent in a hypothetical assument.

Here we might leave this matter with this as one result_that the validity of the modus powendo tollows depends on the alternatives in the disjunctive premies being mutually exclusive, and that there is no way of determining on merely formal considerations whether they are so 1 . that the form of argument is not universally invalid. because they may be so; but not universally valid, because they may not. It is, however, worth while noticing that quite independently of this doubt about the validity of the modus ponendo tallens in any given case the modus tallenda noneus is of more importance on other grounds. We are more often interested in proving one alternative by disproof of others, than vice versa. A prisoner indicted on a charge of murder may indeed be content to show that, whoever committed the crime, he did not : and his ends may be satisfied by proving an alibi. But the ends of justice are not satisfied except by discovering the murderer. And so it is with disjunctive argument generally; its use lies more in what it can establish than in what it can overthrow.

ii. As in hypothetical, so also in disjunctive argument, the major premiss may make a more general assertion, which in the conclusion is applied to some special case. Thus a man might argue

Every man at forty is either a fool or a physician My son at forty is not a physician

... He is a fool

or from the premiss 'Either God is unjust, or no man is eternally punished', I might have concluded that I shall not be eternally numished 2

'It might be said that we could give an unambiguous form to the argument by writing it thus: 'A is either \$0 only, or Conly, or both \$B and C: Bit B only, 'It is neither Conly, nor both \$B and C: But here there can be considered to the constant of the latter point, and only know that A is B, we cannot tell whether it is Cornot; and this information is all that we have; we must not substitute for not; and this information is all that we have; we must not substitute for the minor premise 'A is B' of different one, 'A is B only.'

'The subsumption involved may be appreciated if we like in a separate

iii. The mood of a disjunctive argument is not affected, any more than the mood of a hypothetical argument, by the quality affirmative or negative—of the minor premise or the conclusion. Arguments of the type

are in the same mood as those of the type

$$A$$
 is either not B or not C

· It is not C

I establish one alternative by way of rejecting the other, equally whether from the premises

A diplomatist must either be insincere or be a failure

Bigmarck was not a failure

I conclude that he was insincere, or whether I conclude that he was not honest from the premises

A diplomatist is either not honest, or not successful Rigmarck was successful

Attempts have been made to reduce disjunctive arguments also to syllogistic form. We have seen that a disjunctive proposition implies two or perhaps four hypotheticals; and every disjunctive argument can be exhibited as a hypothetical argument using for major premis one of these. But as hypothetical argument is not syllogism, we do not thereby make disjunctive argument into syllogism; nor do we really identify it with hypothetical argument; for the hypothetical major premise supresses only a part of the meaning of the disjunctive propesition, from a perception of the relations involved in which a disjunctive argument proceeds to

draw its conclusion.1

Every man at forty is either a fool or a physician

. I am either a fool or a physician: but I am not a physician, &c. and having reached the conclusion 'No man is eternally punished', I can with the minor premiss 'I am a man' draw the conclusion that I shall not

with the munor premise '1 am a man 'draw the conclusion that I said not be elemently punished. This act of subsemption is a different act of inference from the disjunctive argument.

'The term hypothetical was long used (following Boethius) sense lations, to cover both what have in this chapter been called hypothetical and what 'course 'Y

have been called disjunctive arguments; and for hypothetical, in the narrower sense employed above, the term conjunctive. Conditional—originally equivalent to hypothetical in the vider sense—has by some who retained the wider sense—has by some who retained the wider sense for the latter been used as equivalent to conjunctive (cf. fix W. Hamilton and the sense of the proper sense of the sense which did not be the sense of the denial of the second, or from the administion of the first to the denial of the sense of the denial of the first.

2. A disjunction may contain more than two members: e.g. it may be of the form A is either B or C or D. In this case, if the minor is categorical. the form A is either $F \circ C \circ P$. In this case, if the minor is eategorical, the conclusion will be disjunctive; and in the modes posseds offens, a disjunctive minor will give a categorical conclusion—A is either $B \circ C \subset A$ is and D. But the minor A is suither $B \circ C \subset A$ which is needed in order junctive proposition. But such details involve no fresh principle of reasoning, and need not be pursued, any more than it is necessary to work out all the variations that are possible according as the disjunction is between two predicates of the anne subject, or two subjects of the same predicate, or two such parts of the same predicate of the or A is either $B \circ C \subset A$ is either $B \circ C \subset A$ is either A is or A is either A or A is interest of A is interest of A is interest of A in the A is a such a proper containing the predicate of the form A is either A or A is contained to A in the A is a such A in the A is a such A in the A is a such A in the A is a contained to A in the A in the A is a contained to A in the A in the A in the A is a contained to A in the A in the A in the A is a contained to A in the A in the A is a contained to A in the A is a contained to A in the A in the A is a contained to A in the A

CHAPTER VVI

ENTHYMEME, SORITES, AND DILEMMA

This chapter deals with certain forms or modes of stating an argument which introduce no new principle of reasoning beyond those now already discussed, but for one reason or another deserve a special name and martin.

An enthymeme indeed is not a particular form of argument, but a particular way of stating an argument. The name is given to a syllogism with one premiss—or, it may be, the conclusion sympressed ! Nearly all syllogisms are as a matter of fact stated

¹ By Aristolia the term Inthiuspa is used in quite a different senae: the defines it as exhapsengle the discharge of optimer, Anal. Pr. 8, Exrii. 700 10. Its nature is discussed in that chapter and in various passages of the Bhotonic Council of the Council

as enthymemes, except in the examples of a logical treatise, or the conduct of a formal disputation. It must not be supposed. however, that we are the less arguing in syllogism, because we use one member of the argument without its being explicitly stated. Syllogism is an act of thought and if in order to perform this act, we need to recognize in thought all three propositions that when formally expressed it contains, we are aroning syllogistically whether we enunciate the whole syllogism or not. That we do recognize a suppressed premise may be shown by the fact that, if any one were to deny it, we should feel that he was attacking our argument, though we had not expressly apparted it

The empressed member may be the major premiss, or the minor, or-less frequently-the conclusion. Medes, in Ovid's play of that name, asks Jason-Servare potus, perdere an possim roggs: here the major premiss. One servare, perders possunt, is understood: Medea supplies only the minor, and-in the form of a rhetorical question—the conclusion.1 If I aroue that 'those cultivate the land best who have a personal interest in its improvement, and therefore peasant proprietors are the best cultivators '. I omit wet I clearly use for to deny it would destroy the aronment—the minor premiss, that 'peasant proprietors have a personal interest in the improvement of the land . The conclusion may be

^{&#}x27;scientific'): where it could, the argument -as Aristotle recognizes -is not really valid; it may be true that persons in a fever breathe rapidly, but I cannot safely infer that a person who breathes rapidly has fever (ib. 1857) 19); there are, of course, symptoms of disease that are of doubtful interpreta-19); there are, of course, symptoms of disease that are of doubtful interpreta-tion. The *eld-paper is said to be a ristorical demonstration, or relatorical syllogism (Bhet. a. i. 1855 * 6, ii. 1856 * 4), because public speakers make use of the appeal to such probable premisses or signs, and do not aspect or provide more strictly demonstrative or scientific arguments. We might say the same of the enthymmen in the later sense of the term, in so far sai tis not held necessary, except in the most formal statement of an argument, always to cannot also both premises and the conclusion. It is possible that always to enunciate both premisses and the conclusion. It is possible that the later sense scross through ministerpretation of the passage in also I. Fri. 5. XXVII. 707-24-25—da a per dos 5 µis 1 XXVII premisses, organizar pierra places, the Action Interface of the Acti or only implied.

¹ This example is used in the *Port Royal Logic*, Pt. III. c. xiv.
¹ I am inclined to think it would be found that the major premise is more

omitted from motives of delicacy, or sometimes for nurposes of effect, as in the Greek counlet

> eal role Durnhillow Adores rarel and A who he h' of Advers Ayan Hookysone, and Hookyshe Words

It is of course possible that an enthymeme may be contained in what promunities lie is only a single centence as in Goneril's address to King Lear .

You as you are old and reverend should be wise or in Recan's, later in the play .

I near you father being week seem so 2

A syllogism, whether expressed in full or as an enthymeme, is a simple act of inference; it may be analysed into premisees and conclusion, but not into parts which are themselves acts of inference. The premieses may however be themselves in turn conclusions reached by other acts of inference; and the conclusion may itself serve as premiss to a further act of inference. A syllogism proving one of the premises of another syllogism is called in relation to that, a prosvilogism : and a syllogism using as a premiss the conclusion of another is called in relation to it, an enterlloetem : where the prosyllogism is expressed in the form of an enthymeme, the whole argument is sometimes called an enighetrema. The following argument contains both a prosvilogism and an episyllogism, and as the former is expressed in abbreviated form, it is also an epicheirema. Those who have no occupation have nothing to interest themselves in, and therefore are unhappy; for men with nothing in which to interest themselves are always unhappy, since happiness depends on the success with which we frequently suppressed when the conclusion of the enthymeme is put in the forefront, the minor when we begin with a reason. If we begin with a

ferefront, the minor when we begin with a reason. If we begin with a reason, we like to lay down a genural principle.

And this of Eucepities: The Lorinan both men, not his one only and this of Eucepities: The Lorinan et al. 1997.

The tarm enthymene has more commonly been applied to a yilogism omitting one of the premises, than to one omitting the conclusion. Sir W. Hamilton (Diesember, pp. 184-185) traces the antiquity of the non-Aristottian use of the term. If goes back to the oldest of the commentators.

A. Manuel's Alfrich, D. 97, note: and Trendelsburg's Element Lopicus.

Aristotelioce, note to § 83, cited by Manuel. The term intropps was differently defined by Aristotle, who called it outhorsouth Statement, Top. 6, xi. 162-16; it was an assault upon a position maintained in disputation by the respondent.

advance the objects in which we are interested; and so wealth is no guarantee of happiness.' Here the central syllogism is

All who have nothing in which to interest themselves are unhanny

Those who have no occupation have nothing in which to interest themselves

.. Those who have no occupation are unhappy.

The major premiss is proved by a prosyllogism to this effect :

Happy men are those who succeed in advancing objects in

which they are interested Men who have nothing in which to interest themselves do not succeed in advancing any object in which they are

.. Men who have nothing in which to interest themselves are not hanny

And an episyllogism is added thus :

Those who have no occupation are unhappy

Rich men may have no occupation

... Rich men may be unhappy.

We have in such a case a train of aroungst, of which the several steps are not each set out in full, though the premises necessary to complete the sequence of thought are readily supplied, as in an enthymeme. Trains of argument may, of course, be of any length, and vary indefinitely in composition, according to the nature of the senarate steps into which they can be broken up; and it would be useless as well as impracticable to invent names for every variety. But there is one well-marked variety to which the name of Sories has been given by logicians.

A Soritee 1 may perhaps be defined as a syllogism in the first floure with many middle terms: or if it be thought that nothing should be called a syllogism that contains more than one act of inference, as

¹ The schoolmen gave the name of syllogismus crypticus to a syllogism which lay so concealed in the wording of an argument, that some process like conversion, or other substitution of equivalent propositions, was necessary in order to show clearly the terms of the syllogism, and their relation: as, here, 'rich men may be unhappy' is taken as equivalent to 'wealth is no guarantee of happiness.
The name is derived from guess = heap.

a polysyllogiem 1 in the first figure with the intermediate conclusions suppressed. Schematically, it is of the form

D is E

where it will be observed that we start with the minor premiss, and each subsequent premiss is, in relation to that enunciated before it, a major 2

There must be, at least, two steps, and therefore three premises; and there may be any number of steps more than two; the premises and there may be any number of steps more than two; the premises will always be more numerous by one than the steps into which the argument can be resolved. Short sorties are of common cocurrence. A well-known example occurs in Romans viii. 29, 30, 'For whom he did foreknow, he also did predestinate to be conformed to mage of his Son. . . . Moreover whom he did predestinate, them he also called; and whom he called; them he also justified: and whom he instified them he also justified:

But long specimens are less common, not because long trains of A series of syllogisms, one proving a premise of another, is called a polysyllogism: while each single step of syllogistic reasoning is called

a wigner of the control of the presence of the control of the cont

of ward is found a regular place in fogurar includes a reasonable.

1. Sories est syllogismus multiplex ... Est enim sories progressio enthymematics, syllogismos continens propositionibus (= prasmissis) uno tantum pauciores. Downam's Commentarii in Patri Rami Dialecticam, 1510, p. 658.

reasoning are rare, but because the successive steps do not generally continue for long together to be of the same form. Leibniz, in the second part of his Confessio Naturas contra Atheistas, written in 1668 (and containing doctrines as to the nature of matter which he subsequently abandoned) offers a proof of the immortality of the human soul in the form of a continuous sorites : but even so many of the propositions are supported by reasons that do not enter into the series of premises constituting his sorites. In the following transcription the premisses that do not belong to the sorites are placed out of line to the right; and some of them are omitted.

The human coul is a thing whose activity is thinking.

- A thing whose activity is thinking is one whose activity is immediately apprehended, and without any representation of parts therein
- A thing whose activity is apprehended immediately without any representation of parts therein is a thing whose activity does not contain parts.
- A thing whose activity does not contain parts is one whose activity is not motion:
- A thing whose activity is not for the activity of a body is motion is not a body : What is not a body is not in space: for the definition of body is
- What is not in space is insusceptible of motion.
- is indissoluble : What is indissoluble is incorrup-
- for corruption is dissolution tible . of the inmost parts.
- What is incorreptible is immortal. ... The human soul is immortal.
 - ¹ s. Erdmann's ed., p. 47.

for all motion is divisible into parts.

always a motion.

to be extended.

What is insuscentible of motion for dissolution is a movement. of parts

XVI

We may ness from examples to a consideration of the form of the argument, and the rules of its validity. It will be observed that the predicate of each premise is the subject of the next, while the subject and predicate of the first and last premies are the subject. and predicate of the conclusion. For each premies is minor to that which follows and major to that which precedes it: and as we start from the minor premiss of the whole aroument, each middle term is predicate of one premies and subject of the next. It follows that (i) no premise except the first may be particular and (ii) none except the last pegative; for in the first figure the major premies must be universal and the minor affirmative: now each premise except the last is a minor, in relation to a premies following it, and must therefore be affirmative: and each premise except the first is major, in relation to one preceding it, and therefore must be universal. This will be easily seen if we resolve the sorites into its constituent syllogisms:

1. beginning from the minor

It is clear that if the first premiss were particular, the conclusion of the first syllegism would be particular; this stands as minor to the third premiss in the second syllegism, whose conclusion could therefore again be particular, and so would ultimately be to conclusion of the whole sorties; but if any other premiss were particular, there would be an undistributed middle in the syllegism into which it entered.

2. beginning from the major

Here, if the last premise (E is F) were negative, the conclusion of the syllogism in which it stands as major would be negative: this as major to the premise C is D would make the next conclusion negative, and so ultimately the conclusion of the whole sorties; but if any other premise were negative, there would be an illicit process of the major term in the syllogism into which it entered. The rules of a sorties are thus nothing but the special rules of the first fieum.\(^1\)

A sorites is distinguished from other chains of reasoning by the fact that not only is one of the premises suppressed, at every step of the argument except one, but the intermediate conclusions, by which the final conclusion is reached, are all suppressed; for the conclusion of one argument is the suppressed premise of the next. This is perhaps, what has led look cinant to give special attention to it.

The Dilamma combines into one argument hypothetical and disjunctive reasoning. Generally it is an argument in which one premise is a disjunctive proposition, and the other consists of hypothetical propositions connecting with either alternative in the disjunction an unpalatable conclusion. In one case, however—that of a simple destructive dilemma *—the disjunction may be in the consequent of the hypothetical premise, and the other be a categorical premise denying both alternatives in the disjunction. We may

¹ Either as E or an I proposition may be converted simply. With an a premise for the first, if it be converted, the sorties may be broken up into a series of syllogisms in the third figure; with an E premise for the last, if it be converted, the sorties may be broken up into a series of syllogisms in the second figure. Yet, except for the premise that converted, the middle in the second figure. The series of the series with the series premise, we should be larried in quantum of the series of the

though its resolution may involve the second or third.

See below, p. 832-884.

The hypothetical premise is sometimes called the major, in accordance

therefore define a dilemma, to cover this case, as a hypothetical arysment offering alternatives and proving something against as oppoment is either case. The conclusion may be either the same, whichever alternative is accepted, or different; in the former case the dilemma is called simple, in the latter complex. It is called constructive, if it proceeds from affirmation of antecedent in the hypothetical premiss to affirmation of consequent; destructive, if it proceeds from denial of consequent to denial of antecedent.

1. Simple Constructive.

Troops with a river behind them have sometimes been placed in a dilemma none the less painful because it is simple. If they stand their ground they die—by the sword of the enemy: if they retreat they die—by the flood; but they must either stand or

retreat; therefore they must die.

2. Complex Constructive.

Thus we might argue—and this too is unfortunately a dilemma from which it is not easy to see an escape:

If there is censorship of the Press, abuses which should be exposed will be hushed up; and if there is no censorship, truth will be sacrificed to sensation

But there must either be censorship or not

.. Either abuses which should be exposed must be hushed up,

or truth be sacrificed to sensation.

3. Simple Destructive.

with the nomenclature used also of hypothetical reasoning: and the other premiss the minor.

premise the minor.

'Antecedint and consequent may, of course, all have the same subject (if
A is B, it is D; and if it is C, it is D); or the same subject in one case and
different subjects in the other; and the minor premise will vary accordingly.
It would be bediene to give each time all these varieties, which involve no
difference of principle.

Of this character was one of the arguments used by Zeno to disprove the possibility (or perhaps we might say, the intelligibility) of motion:

If a body moves, it must either move in the place where

it is, or in the place where it is not
But it can neither move in the place where it is, nor in the
place where it is not

. It cannot move

Again. If A is B. C is D and E is F

But either C is not D or E is not F

.. A is not B

A Liberal, convinced in 1885 that Gladstone's Home Rule Bill was dangerous to the best interests of the country, and too much devoted to his leader to enter into opposition to him, might well have argued:

If I am to continue in politics, I must feel able to support

But now I must either act against my convictions, or oppose my party

.. I cannot continue in politics.

4. Complex Destructive.

If A is B, E is F; and if C is D, G is H

But either E is not F, or G is not H

... Either A is not B. or C is not D

. A nation having colonies like those of Great Britain might fairly uroe:

If we give our colonies self-government, we shall make them powerful; and if we attempt to control their use of it, we shall make them hostile

But either we ought not to make them powerful, or we ought not to make them hostile

.. Either we ought not to give them self-government, or we ought not to attempt to control their use of it.

[It is sometimes said that a destructive dilemma is always complex, and such arguments as those given under (3) above would not be allowed to be dilemmas. Mansel's definition (which follows Whately, and has been adopted by others since) definitely excludes (the simple destructive; according to him (e. his Addrick, p. 108, n.) a dilamma is 'a syllogism having a conditional major premiss with more than one antecedent, and a disjunctive minor'; as the destructive dilemma proceeds from denial of consequent to denial of antecedent, if there is more than one antecedent its conclusion must be necessarily complex. A number of writers, however, have admitted the simple destructive dilemma; and it essens very difficult to calculude asamples of the second form above given, at any rate. The simple constructive (If A is B, B is F; and if C is D, B is F) are a borrillers.

If A is B or C is D, E is F But either A is B or C is D

The simple destructive runs

If A is B, C is D and E is F
But either C is not D or E is not F

A is not B

It may be said that there is a disjunction in the hypothetical premise of the former, and not of the latter : but this does not seem to constitute an essential difference, such as would render one a dilemma and the other not. In the former, one or other of two alternatives must be affirmed, and whichever be affirmed, the same conclusion follows. because it is logically a consequent of affirming either alternative: in the latter, one or other of two alternatives must be denied, and whichever be denied, the same conclusion follows, because it is logically a consequent of denying either alternative. The essence of the dilemma seems to lie in the fact of confronting a man with alternatives at once includtable and unpleasant : of the definition quoted by Mansel from Cassiodorus, loc. cit.: 'Dilemma. auod fit en duabus propositionibus pluribusos, en quibus quidauid electum fuit, contrarium cose non dubium cet. And therefore the other example given above-Zeno's argument about motion-seems also to be fairly called a dilemma. It is true that its second premiss is not disjunctive at all, but denies a disjunctive proposition; it does not assert the truth of one of two alternatives, but the falsity of both. But the whole argument is a combination of the hypothetical and the disjunctive, and drives a man into a corner by way of alternatives between which his choice is alleged to be confined. If we are to maintain that a body moves, we have to assert one or other of two propositions which are both self-contradictory; and that seems a good example of being placed between the devil and the deep sea. The simple constructive dilemma is a hypothetical argument in the modus ponens; its hypothetical premiss has a disjunctive

¹ So Minto takes it. Logic. Inductics and Deductive, p. 224.

fantecedent and a simple consequent, and therefore the other premise must be disjunctive and the conclusion simple. The simple destructive dilemma of the form given first above is a hypothetical argument in the modes tollens: its hypothetical premise has a simple antecedent and a disjunctive consequent; the other premise must therefore be the denial of a disjunctive proposition, and the conclusion the denial of a simple one. But the denial of a disjunctive proposition is a categorical, whereas the affirmation of it is of course a disjunctive proposition. Hence the difference which has led to refraing the name of dilemma to this form of aroument. vet its parallelism with the simple constructive seems correct and clear. It may be asked why there are two types of simple destructive dilemma, against one type of simple constructive. The answer seems to be this. In the destructive dilemma, I may overthrow the antecedent, either if its truth involves two consequents, one or other of which I can deny, or if its truth involves one or other of two consequents, both of which I can deny : and each case involves a disjunction. In the constructive dilemma, I can establish the consequent, either if two antecedents involve its truth, both of which I can affirm, or if either of two antecedents involve its truth. one or other of which I can affirm. But here the former case does not constitute a dilemma, because no disjunction is involved anywhere: If A and B are true, C is true; but A and B are true .. C is true. It would appear therefore that so far from there being no such thing as a simple destructive dilemma, there are two forms of it, against only one form of simple constructive dilemma.]

A dilemma is sometimes spoken of as if it were a peculiarly unsound form of argument. It shares with all inference the property that it is of no material value unless its premises are true; but formally it is quite sound, and if there is about it any special weakness, it must is in some special difficulty in getting true premises for it. Now it is generally difficult, except where one alternative is the bare negation of the other, to get an exhaustive disjunction; it is here that any one 'in a dilemma' would look for a way out; and it is this difficulty which inspires mistrust of the dilemma as a form of argument.

To show that there is some other alternative besides those, on one or other of which your opponent attempts to drive you, is called escaping between the horns of a dilemma: the alternatives being the horns on which you are to be 'impaled'. In reply to Zeno's dilemma to show the impossibility of motion, it is often said that a body

need not move either in the place where it is or in the place where it is not: since it may move between these places. It may be questioned whether this is a very satisfactory solution of the peradox . for those who offer it might find it hard to say where the hody is when it is between these places: if it is not in some other place the continuity of space seems to suffer disruption But however that may be we have here an attempt to escape between the horns of Zeno's dilemma.

The other two ways of meeting a dilemma also bear somewhat nicturesone names : we may rebut it, or we may take it by the horse To rebut it is to produce another dilemma with a contradictory conclusion. The old story of Protagoras and Eusthlus, without which a discussion of Dilemma would hardly be complete, furnishes a good example of rebutting. Protagoras had acreed with Enathlus to teach him rhetoric for a fee, of which half was to be paid at the conclusion of the instruction and the remainder when Eusthlus won his first suit in court. Observing that the latter delayed to practice Protecores thought he was endeavouring to evade nevment and therefore himself brought a suit for the recovery of the second half of his fee. He then aroued with the jury that Eusthlus quot to new him, in the following way :

If, he said, he loses this case, he ought to pay, by the judgement of the court: and if he wins it, he ought to pay, by his own agreement

But he must either lose it or win it.

... He ought to pay.

Eusthlus, however, rebutted this dilemma with the following :

If I win this case, I ought not to pay, by the judgement of the court: and if I lose it. I ought not to pay, by my own agreement

But I must either win it or lose it

.. I ought not to pay.

It will be seen that the rebutting dilemma is produced in this case by transposing and negating the consequents in the major premiss. With a destructive dilemma the parallel procedure would be to negate the antecedents. But this is not the only way of rebutting: you rebut whenever you produce a dilemma with contradictory conclusion, and you may do that with quite different premises. Nor can every dilemma be rebutted in this way or in any other way . not in this for the alternative conditions are not always such with which you can connect the contradictory of each other's consequents. And if a dilemma can be rebutted, one of two things must follow. Either there must (as in the last example) be some element of contradiction involved in the situation : and some of the ancients spent much incenuity in imagining situations of this kind, in which our reseon was entangled by finding that two contradictory solutions of a problem could apparently be maintained with equal force of this nature are the well-known conhisms of the 'Liar' and the 'Crocodile': Epimenides the Cretan said that all Cretans were liars: if they were, was he lying, or was he speaking the truth? 1-s crocodile had stolen a child, and promised the mother he would restore it, if she could guess rightly whether he intended to do so or not; 2 if she said he would not restore it, she could not claim the child by his promise, because her taking it would make her guess wrong; if she said he would restore it, she could not claim it, for she guessed wrongly: what was she to my? Or if there is no such element of contradiction involved in the situation, then a dilemma can only be rebutted because its premisses are unsound, and premisses equally or more plausible can be found for another dilemma proving a contradictory conclusion. In this case, it would be possible to attack the original dilemma directly. either by showing that you can escape between the horns of it, if the disjunction is not complete, or in the third of the ways mentioned above, by 'taking it by the horns'.

To take a dilemma by the horse (or by one of them) is to accept the alternative offered you, but to deny that the consequence, which the opponent attaches to its acceptance, follow. Perhaps the following will serve for an example. It is held by many naturalists, that species are modified in the course of descent only by the accumulation of many slight variations, and not per saltss: variations not being directly adaptive, but being distributed, in respect of frequency and degree, in proportions that follow the well-known 'curve of error' on either side of the standard represented in the

¹ The solution is easy unless we suppose that no Cretan ever spoke the truth; in which case the situation imagined contradicts the assumption which it makes.

¹ Cf. Lucian, Vit. Auct. § 22 (cited Mansel's Aldrick, p. 151).

parents. Against this it has been aroued, that though the cumulative effect of many slight variations might be useful it will often happen that in the incipient stages, while the distance traversed in the direction of some new necessiarity is still very slight, the varies tion would be velocless and therefore not tend to be perpetuated . so that the begin for accompletion would not exist. This line of objection has been applied to the particular case of protective colouring in insects in the following argument. If it is said the slight variations with which the process of mimicry in insects must. as alleged begin are of no use in leading hirds to mistake the individuals exhibiting them for members of some protected species. then they will not be preserved by natural selection, and no accumulation can take place; while if they are of use, any further and more exact resemblance to the protected enecies is unnecessary, and could not, if it occurred be preserved by natural selection. Now against this dilemma we may answer that it does not follow that, because a slight degree of resemblance is useful, any further degree would be superfluous. On a particular occasion a particular insect no doubt needs no greater resemblance than what has actually enabled it to escape : but with a large number of insects over a long series of occasions, it may well be that the percentage of escapes would be higher with those in whom the resemblance was closer. Thus the dilemma is 'taken by the horns': but that does not settle the important question at issue as to whether variation ever does proceed per saltum or not. We saw before that a thesis is not disproved by the refutation of any particular argument brought forward in support of it.

¹ See an article on The Age of the Inhabited Earth, by Sir Edward Fty, in the Monthly Review for January, 1903.

CHAPTER XVII

THE BODY AND WATTER OF INFERENCE

So for we have considered and examined some of the commencest types of inference-syllogism, hypothetical and disjunctive reseming and certain complications of these. We have not pretended. what has nevertheless sometimes been maintained wither that the letter can be reduced to syllogism, or that syllogism, even if the term be extended to include them, is the type to which all valid inference must conform . though we have maintained, and it will appear more fully in the second that they are forms of great frequency and importance in our thought. Were Logic a purely formal acience, the analysis of these forms would be, to those who thought that all reasoning really moved in one or other of them, the end of the task imposed upon that science: to those who did not think them the only form in which men's reasoning moves, no other task would be left than to offer a similar analysis of the remainder. But if it is impossible to understand fully the form of thinking without reference to the nature of that about which we think, then the task of Logic is obviously harder. It will not suffice to work with symbols. We cannot make abstraction of the special character of our terms. Already we have found this to be the case. We saw that syllogism in the first figure, and in the highest form which it can assume in that figure, rests upon a perception of the necessary relation between certain notions, or universals; while in the third figure such a perception of necessary relation neither need be given in the premisses. nor can be reached in the conclusion. We saw too how hypothetical reasoning, where it differs most from syllogistic, differs because it establishes a connexion between subject and predicate in the conclusion by means of a condition which is apparently extraneous to the nature of the subject; and yet how our thought recognized that there must be some wider system to which the subject and that condition both belong, and through which it comes about that the fulfilment of the latter should affect the predicates of the former. None of these things could be explained or understood merely through symbols: examples were needed not only to show that the arguments symbolized were such as we do actually often use, but because only in suitable examples could those facts of our thought with which we were concerned be realized. The symbols are the same, but do not symbolize the same thing, when some terms in our syllogism are particular concrete objects, whose attributes are set down as we find them, and when they are all universal characters of things, between which we person's connection.

It will be said that if the form of thought be thus bound up with the matter, an understanding of the form must wait upon a knowledge of the matter, and the task of Logic will not be complete until we have finished the investigation of what is to be known. In a sense this is true. It may be illustrated by the case of mathematics: no one can understand the conditions on which the corency of mathematical reasoning depends except in the process of thinking about number or space or quantity : they cannot be seen in application to beterocepeous subjects. And it consists with the position which we have taken up from the outset, that Logic is the science which brings to clear consciousness the nature of the processes which our thought performs when we are thinking about other things than Logic. Nevertheless we must bear in mind one or two facts. which may make the task of Logic seem a little less hopeless than it would appear to be, if it had to wait altogether upon the completion of knowledge.

In the first place, the dependence of the form of thought upon the matter is consistent with some degree of independence. It may be impossible to greap the nature of mathematical proof except in application to mathematical matter; but an analysis of one or two examples of geometrical reasoning may serve to show us the nature of geometrical reasoning in general, and after that the form of it will not be any better understood for tracking it through all our reasonings about every figure and space-relation. So also it may be impossible except in examples of the relation of subject and predicate to grasp the distinctive character of syllogistic reasoning; but we may grasp it there universally, and realize that it will be the same for all terms that stand in those relations. If this were not so, science would be impossible; for science seeks to reduce a multiplicity of facts to unity of principles. Thus our apprehension of the forms

of thought has not to wait upon the completion of our knowledge so far as that completion means only its extension to fresh matter of the same kind. If some branch of our knowledge is defective in point of extent as it would appear for example that the evience of number must ever continue to be because the numerical series is by its nature inexhaustible—yet its further extension may involve no change in its character; and so soon as all the main branches of nossible knowledge have been discovered—that is, knowledge about all the main departments of fact.the forms which thought assumes in them can be studied even while our knowledge is incomplete in its extent. The main departments of fact must, of course, be taken to include not merely those which form the subject-matter of the physical sciences, but equally those of which philosophy treats, and not least the relation of the world to the mind that knows it. It would be man to assert that this stage has been reached in the progress of knowledge. The completion of our knowledge may yet require not only its extension, but in large degree its transformation. Yet we may severt that a great deal of our ignorance forms no har to the completion of the investigations of Logic.

And in the second place though Logic is in the main a reflection upon the nature of knowledge already gained, there is this paradox short knowledge, that we seem to some extent to know what knowledge ought to be, before we know anything as we ought. We have an ideal, of which we are sufficiently conscious to realize the imperfections of the actual, though not sufficiently conscious to be able to put it clearly and fully into words. This paradox is not confined to knowledge; it occurs in art and in morality also. We may recognize defect in an aesthetic whole without being able to rectify it, and yet we may be able to say in what direction its perfection must lie; we may know that 'we have all sinned', without having seen 'the glory of God', and still be able to prescribe some of the conditions which that must realize. So also we may know that the form of our thought, even when we think best and most patiently, often falls short of the full measure of knowledge: that our way of thinking-our way of looking at things, if one may put it so-is wrong because it fails to escape contradictions and satisfy all doubte: and that there must be some way of thinking (if the world is as a whole intelligible at all) in which contradiction and uncertainty will vanish. We may know all this, and know that we have

not found that better way (for if we had we should certainly not remain in the worse); and still we may be able to say something short it though we have not found it to lay down conditions which our knowledge of any enhiert must estisfy because it is knowledge_i.e. to prescribe to some extent the form of knowledge. not only as a result of reflection upon instances of subjects perfectly known or by abstraction from the activity of knowing perfectly in the concrete, but by way of anticipation, out of reflection upon instances in which we know subjects less than perfectly, and know the imperfection of our knowing. The extent to which we can thus anticipate is not unlimited: a man must get some way in science, before he will realize what science should be, and that it is not what it should be: just as a man must get some way in virtue. before he will realize how much more it requires of him than he has achieved. Yet it remains true that thought can in some degree anticipate a form of knowing a matter which it has not exercised therein : and it is the husiness of Logic to set this form forth. So far again Logic has not to wait, in order to complete its task. until our investigation of what is to be known has been completed.

If this is true, we may say on the one hand, that no study of the nature of inference can be adequate which treats it as an operation performed with symbols, or one intelligible at any rate when we work with symbols. On the other hand, we may recognize that there are recurrent forms of inference, whose nature is the same in their different occurrences1, and they occur commonly in application to matters in many respects very diverse; we may also recognize an ideal of what inference should be if it is to convey knowledge: if we are to feel in making it not merely that the conclusion follows from the premisses, but that we are getting at indubitable truth.

Our discussion of inference up to this point must therefore be incomplete, in so far as (a) we have failed to deal with all those distinguishable recurrent forms of inference whose universal nature can be realized in an example; (b) we have failed to make plain the conditions of knowledge as well as the conditions of cogency.

As to the first count, there are certainly forms which have not

¹ Some might maintain that it is never quite the same when the matter is different, any more than the nature of man is quite the same in any two individuals. I do not wish to subscribe to this view; but even its upholders would admit that such differences may be negligible.

been examined. For example, there is the a fortiori argument. 'If a man love not his brother whom he hath seen,' asks St. John, 'how shall be love God whom he hath not seen?' And there is mathematical reasoning, of which we have only said that it is not syllogistic; this from its importance may chaim rather fuller consideration. But perhaps more remains to be done in the way of showing how far inference of these different forms enters into the building up of our knowledge, and what other operations of thought enter into it.

As to the second count: it is a charge brought against the analysis of syllogism, and the other inferential forms considered above that such analysis only shows us the conditions of consistency in reasoning, and not the conditions of truth. To reason consistently is very different from discovering truth : for the consistent resenver will reproduce in his conclusion the error there may be in his premisses. Those who have brought this charge have sometimes supposed that what is wanted is other and better forms of inference. It would be much truer to say that what we want is to realize how much besides formal validity of inference must be present in an argument which is to convey knowledge. To realize what is needed is not indeed the same thing as to supply it : but Logic cannot belo us to more. The critics of the Logic which was content to analyse the conditions of validity in some of the common inferential forms (and which often supposed—it must be admitted that there were no other forms of inference) have not always believed this. Many of them, as has been said in an earlier chapter, still looked on Logic mainly as an instrument for the discovery of truth about any matter on which we might propose to reason, and hoped to find a new and better instrument than what the Logic which confined itself to such analysis afforded. This was the object with which Bacon wrote his 'New Instrument' or Novum Organum; and J. S. Mill, though he defines Logic as a Science, wrote his famous treatise in the hope that familiarity with the methods of reasoning used successfully in the physical sciences would enable men to prosecute the study of the moral and political sciences with more success.2 Logic is not a short cut to all

¹ Though formally a true conclusion may be got from false premises, the error still infects the mind, and will lead to a false conclusion somewhere. ¹ Cf. Logic, VI. i. and Autobiography, p. 226.

other branches of knowledge. But this we may say, that men who know the difference between consistency and demonstration, who know what is required before it can be said that they have know-Ledge about things in the full and namer sense of that term are less likely to remain content with the substitutes that commonly ness muster in men's minds for knowledge. By a study of the conditions of demonstration we may be led to see how far from being demonstrated are many of the beliefs we hold most confidently. To know what we do know, and what we do not-what, out of the things we suppose ourselves to know, we really know and are rationally justified in believing: this, as Plato long ago insisted 1 is neither a small thing, nor an easy; and until we have some idea of what knowing a thing means and requires, we are not likely to schieve it. This is why Logic should do more than present us with a study of the forms of consistent reasoning, and should attempt to exhibit the nature of knowledge and demonstration; not because such an exposition of the form of knowledge is itself an instrument for bringing our thoughts upon any matter into that form, but because it stimulates us to use such instruments as we have, and to appraise the results which we have so far attained.

Now the most obvious criticism that can be made upon a Logic which confines itself to setting forth the formal conditions of valid infarence is that it ignores the material truth of the premises; the validity of the reasoning affords no guarantee that these are true. It is no doubt possible to direct men's attention so exclusively to the form of argumentation that they will bestow little upon the truth of the principles from which they argue. It has often been complained that the study of Logic did this—or, as its critics would say, the study of Deductive Logic. The epithet, however, implies a misunderstanding; it is a disproportionate statention to available to form in general which the critics cought

¹ Charmides 171 D.

[&]quot;The popular satisfues between Deductive and Inductive Logic has been for a worlded, and that deliberately; we shall have to consider presently what the nature of the difference between deductive and inductive reasoning is but it may be said at once that it does not lie in uning the forms of inference that are commonly expounded under the titles of Deductive and of Inductive Logic respectively. For inductive veasoning uses forms of another that the commonly expounded under the titles of Deductive and the said of Logic respectively. For inductive veasoning uses forms of another than the containing the contractive discuss forms of inference which are certainly inductive.

to deprecate. Validity of form is a thing worth studying, not only for its own sake, but in some degree lest we infiringe it; yet it appeahologically possible, by studying it too much and too exclusively, to become distracted from due care about truth of matter. It is, however, probable that in the times when men have been most remiss in the examination of their premisses, the state of the study of Logic has been as much a symptom as a cause of this; and however that may be, so far as it lies with Logic to provide a corrective, it is very important for the logician to be clear as to the nature of the corrective he is to provide. And for that purpose he must distinguish two questions; he may try to show what kind of premisses knowledge requires, or by what process of thought we may hope to get them. In modern times, the former of these constitutes have been too much neglected.

These last remarks may be a little expanded. And first as to the causes which for many centuries made men remiss in the examination of their premises; one sometimes finds the blame for this thrown upon the futility and misdirection of the scholastic Logic, which absorbed during the Middle Ages, and even later, so large a part of the energy of men's minds. It would be hard to deny that much energy was misdirected; but it is as likely that energy went into this channel because others were temporarily closed to it, as that others were robbed of it because it ran in this; though no doubt there is action and reaction in such a case, and a habit which certain influences tend to form may in turn strengthen those influences.

It has been said that the mandate issued to the age of Plato and Aristolle was Bring your beirgin into harmony wild non another; that the mandate of the Mediaeval Spirit was Bring your beirgin into harmony wild doyme; and that the mandate of the new spirit which rebelled against the authority of the Church was Bring your beirgin into harmony with fact. Such a mode of putting things may suggest own false ideas. It is impossible to bring one's beliefs into harmony with facts, except so far as the facts are known to us, and therefore by the way of bringing them into harmony with one another; and it would be wrong to suppose that Plato and Aristotle forget that among the beliefs they had to harmonize with one another were the beliefs they held about matters of daily experience, or that they

¹ Minto, Logic, Inductive and Deductive, p. 248.

were indifferent to the necessity of correcting and enlarging those beliefs by more or less systematic observation : Aristotle in particular added largely to men's knowledge of facts. Again, it is clear that to bring one's beliefs into harmony with dooms is to bring them into harmony with other beliefs; and that those who rated highest the importance of that task would least have doubted that they were bringing them into harmony with facts. Facts can only be expressed in judgements which are matter for belief; and such judgements need not cease to express facts because they are presented as dogmas. But it is true as Minto wishes to bring out in the chanter quoted, that dogma and the spirit which accepts dogma did during the Dark and the Middle Ages play a part in the history of thought far greater either than they played in classical antiquity or than they have come to play since the revival of learning. And such dogma was not necessarily ecclesiastical dogma; it came from the scientific works of Aristotle, or other great men of old whose works were known, as well as from the Bible and the Church: just as to-day there is orthodoxy in science, against which new scientific ideas find it at times a little difficult to battle, as well as in theology.

The schoolmen knew, as well as Bacon or any other of their critics, that the study of the syllogism was not all-sufficing : that no syllogism could guarantee the truth of its premises; and that for a knowledge of the most general principles to which deductive reasoning appeals we must rely on something else than deductive reasoning itself. Bacon refers to the 'notorious answer' which was given to those who questioned the accepted principles of any science—Cuique in sua arte credendum.1 And there are seasons in the process of learning when that is a very proper answer; men must be content at many times and in many matters to accept the expert opinion of their day. But this is only tolerable if in every science there are experts who are for ever questioning and testing. When tradition stereotypes doctrine, it is as bad for knowledge as close guilds and monopolies are bad for the industrial arts: they shut the door upon improvement. Authority plays, and must play, a great part in life-not only in practice, but also in things of the intellect. But the free spirit is as necessary, which insists on satisfying itself that what is offered upon authority has claims on its own account upon our acceptance.

1 Nov. Org. I. 82.

Why was it that for so many centuries so much was accepted upon authority which afterwards fell to pieces in the light of indenendent enquiry? Much knowledge of the human mind historical and philosophical would be needed in order to answer this question adequately. If a few observations may be made upon it here, it is with a full consciousness of the inadequate equipment of knowledge upon which they rest. And it may be doubted whether we can hope fully to explain why some periods and places are richer then others in men of fruitful and original thought: at most we can hope to show what conditions are favourable to such men's work when they arise. Now to us, looking backward across the Middle Ages to the more brilliant days of Athens and of Rome. and looking also at the great increase of knowledge which the last three centuries have brought, the stagnation of the sciences in the period intervening is ant to seem a thing surprising. But how long was it before ancient science began to appear and to advance? The power of tradition and authority over the human mind is the rule rather than the exception.1 And in the break-up of ancient civilization there perished not only much knowledge, but much material wealth: men were of necessity for long absorbed in the task of restoring this and restoring order: and it is not wonderful that they had little time to spend in questioning such scientific principles as had survived. Moreover, during the darkest times. the most powerful and the most beneficent institution that stood erect was the Church: the most comprehensive and well-reasoned theory of the world was that which the Church taught: the strongest minds, almost the only minds that thought at all, were enlisted in the ranks of the clergy (which was why independent thought took so largely the form of heresy), and the interest of men was directed rather to what concerned the soul than to nature around them. To this it must be added, that through a series of historical accidents, a great part of the literature of Graeco-Roman civilization had perished; but that of the works of Aristotle some few were known continuously, and the rest recovered, at least in translations, by the end of the first quarter of the thirteenth century.2 The works of Aristotle, by their encyclopsedic range. by the effort after systematization displayed in them, and by their

1 Cf. Barehot. Physics and Politics

^{*} e. Pranti, Geschichte der Logik, III. p. 8.

extraordinary intellectual power, were peculiarly suited to rivet themselves upon the mind at a time when shility was not wanting. but when detailed knowledge was slight, and there was little else to serve for an educational discipline. It is not surprising, if Aristotle and the Church (especially when the Church pressed Aristotle's philosophy into its service) acquired a preponderant influence over men's minds. Indeed, it is hard for us to imagine what self-confidence and courses were necessary, in order to question any part of that closely concatenated fabric of belief, upon appearing to accept which depended a man's comfort in society and perhaps his life in this world, and upon really accepting it-unless he could find for himself something better-his confidence with regard to the next. It is no small testimony to the inexpurpable power of reason, that this system broke down. And it began to break down largely through the recovery of other monuments of ancient thought and learning besides the works of Aristotle. This doubtless stimulated, though it could not produce, the powers of those men by whom the foundations of modern science were laid-men like Construent Galileo Harvey Gassendi Descartes. It was not the reform of Logic which liberated the mind, any more than it was Logic which had bound it.

It is, then, rather to the habit of believing on authority, the strength of which it has been attempted in some degree to account for, than to the prevalence of an erroneous Logic (whose errors were not really what the 'inductive' logicians supposed), that the stagnation of science for so many generations must be attributed. Given that habit, it was natural that men should spend time and thought upon a barren elaboration of the more technical parts of Logic, and leave the traditional assumptions both of it and of the natural sciences unexamined. When the overmastering influence of authority began to decay, the science of Logic shared with other sciences in the revivingation that comes from thinking out a subject freshly and independently.

But, as was said above, the particular matter which first attracted the attention of the reforming logician was the barrenness of an exclusive attention to the forms of valid inference; and the particular improvement proposed was the establishment of a Logic that should do for the discovery and proof of scientific principles what had already in part been done for the drawing of conclusions from them. This at least is how Bacon looked at the matter; and others have so looked at it after him, in this country more especially. Now it is a very interesting question, how sciences get their principles, and when they may be considered proved; but it is not quite the same as the question, what kind of principles knowledge requires.

The works of Aristotle dealing with inference are three-the Prior Analytics the Posterior Analytics and the Tonics Speaking generally the first of these deals with syllogism from a formal point of view-it nevs no attention to the nature of the premises. but only to the validity of inference; the second deals with knowledge, or demonstration: it asks not when a man is bound by the acceptance of certain forms of premise to admit a certain form of conclusion, but when he can be said really to know a thing absolutely, and not merely on the assumption that certain premises are true; the third asks how positions can be established or overthrown, what sort of considerations are useful in weighing their claims to acceptance, and on what sort of grounds men may be content to accept their principles in matters where certainty is not attainable. In the first and in the third of these treatises, Aristotle was analysing and formulating the actual procedure of his contemporaries: he did not, upon the whole, go shead of the science. the disputation, the rhetoric and the pleadings of his day. In the second, he was doubtless guided also by a consideration of the highest types of scientific knowledge then existing; but he was guided also by an ideal; he was trying to express what knowledge ought to be, not merely what the form of men's reasonings was.

It may be said that in acholastic Logic, the problems of the Prior Asslytic bulked too large; that those who revolted against this raised, without realizing it, problems of the same kind as Aristotle had already discussed in the Topice; but that for a long time the questions of the Posterior Asslyticer received insufficient attention. It is these last which are the highest, and go despest into the philosophy of the subject. The physical sciences sumploy many principles of great generality which they try to prove; but they accept without asking why they accept them. As instances of these may be mentioned what is called the Law of the Uniformity of Nature—the principle that every change has a cause upon which it follows in accordance with a rule, so that it could not recur in the same form unless the same cause were present, no fail to recur when precisely the same cause recurred: or again, the principle that matter is indestructible: or that the laws of number and space hold good for everything numerable or extended. There are other principles less general than these, such for example as the Laws of Gravitation, of which, as aforesaid, science offers proof; but whether the proof of these amounts to complete demonstration, and whether the assumption of the truth of those is justified—these are publems with which the special sciences truolle themselves little, and which will not be answered merely by analysing the nature of the inferential processes that do as a matter of fact lead scientific men to accept the general propositions which they conseirs themselves to have nowed.

This is only an elementary book, and makes no pretence to give a complete answer to that most difficult of logical questions, Nota is knowledge, is the project forms? But from what has been said in the present chapter, it follows that there are two problems to which some attention ought to be given. One is the question how, as a matter of fact, we do get our premisses: the other, what are the requisites of demonstration. The first of these may be called the problem of Induction.

CHAPTER XVIII

OF INDUCTION

Two history of the word Induction remains to be written: but, it, is certain that it has shifted its meaning in the course of time, and that much missinderstanding has arisen thereby. The Aristotelian term drawns of which it is the translation, signified generally the process of establishing a general proposition not by deduction 1 from a wider principle, but by appeal to the particular instances in which its truth is shown. From what sense of the verb dudyers this use of the word surang is not clear; there are two namages? Where the verb in a logical context which makes it clear that the procom of drawny is referred to takes a personal subject; as if it were meant that in the process a man is brought face to face with the particulars, or perhaps brought, and as we could say induced. to admit the general proposition by their help. In another place it is the universal proposition which is said to be 'induced' or brought forward or brought up (whatever the best translation may be); and perhaps the not infrequent antithesis of draywy and συλλογισμός might suggest that the usual object of the verb is the inductively obtained conclusion; the conclusion is certainly what is 'syllogized', so that the conclusion may also be what is 'induced'. It has, however, also been thought that the process of bringing up or citing the instances, by means of which the conclusion is to be established, is what the word was primarily intended to signify 4: and anyhow the process described is one in which a general conclusion is established in that way, by citing the instances of its truth.

¹ The history of the term Deduction also remains to be written, dwaren's in Aristotle meant something very different (v. Anal. Pri. 8. xxv: there is also the use cited p. 290, n. 2, supre), and the nearest Aristotelian equivalent to Deduction is συλλογισμός.

3 An. Post. a. i. 71° 21, 24: a. xviii. 81° 5.

Top. a. vviii. 108° 11 : cf. Soph. El. vv. 174° 84.

So apparently Bonitz: v. Index Aristold., a. v. iraywyi.

Induction then meant primarily to Aristotle, proving a proposition to be true universally, by showing empirically that it was true in each particular case: or, proving something about a logical whole hy anneal to the experience of its presence in every part of that whole : as you might show that all horned animals reminete or that whenever the tail of a fish is unsymmetrical (or heterocornal) it is vertebrated, by a dissection of the intestines of every kind of horned heast, or of the tail of every kind of heterocercal fish. In such a proof, it would be assumed that the nature of each eneries of fish or beset might be judged from the single specimen dissected: and it is to be noted that Aristotle thought that the process of induction becan with the infima species: the species in his view (as we saw in discussing the Predicables) being essentially the same in every one of its particulars. This form of argument he described in his own technical language as proving the major term of the middle by means of the minor - and he showed how it could be expressed as a syllogism. From the premisees

The cow, the sheep, the deer, &c., ruminate
The cow, the sheep, the deer, &c., are horned

I cannot, as they stand, infer that all horned animals ruminate, because there may be other horned animals besides all that I have

¹ Induction certainly starts in one sense, according to Aristotle, with individuals, for it starts with what we can perceive with the senses, and only the individual can be perceived: cf. a.g. Am. Flost. a. xviii. 81° 5-8. But it may be said that what we supprehend in the individual is in character or appeal: cf. As. Flost. a. xviii. 81° 5-9. But it may be said that what we supprehend in the individual is in character or appeal: cf. As. Flost. a. xviii. 81° 29. In As. Flost. g. xviii. 81° 1-20, In As. Flos

enumerated : but if I know that this is not the case : if the members in my enumeration taken together are commensurate or couste with the term 'horned animals', then the possibility which forbids the general conclusion is excluded, and I may infer that all borned animals ruminate : as is shown by the fact that the minor premies may be converted simply: I may say that all the homed animals are the con and sheep and deer &c : and my syllogrient becomes formally correct. In such a syllogism we are said to prove the major of the middle by means of the minor, because (se we saw) the minor means to Aristotle not primarily the subject of the conclusion, but the term of least generality and nearest to the individual: it is by the particular instances that the predicate ruminant is proved of the subject torsed animal. And if we might record the mesession of horns as the cause of ruminating, then it would be the proper middle term by which to demonstrate runingst of cow or sheep or deer: in Aristotle's own example, where longevity is proved of gall-less animals by means of man, horse, mule (and any other particulars that oneht to be mentioned -though for brevity they are not enumerated), it is supposed that the absence of gall is the cause of longevity.

In symbolic form then we may express Aristotle's Induction thus:---

A B C D, &c. are P A B C D, &c. are all the M \therefore All M are P

This, which he calls δ & ἐπαγωγῆς συλλογισμός, is commonly called now the Inductive Syllogiam. If it is to be valid, our . minor term must, as Aristotle says, comprise all the particulars; ἡ γὰο ἐπαγωγὸ διὰ πάστων.¹

We have now seen what Induction, as a formal process, meant in the mouth of the first author who used the term; and when Aristotle insisted that it must proceed through all the particulars, or (as it was afterwards put) by complete ensureration—the requirement which, to Bacon and the 'inductive logicians' of modern times, has given so much offence—he was quite right; for if you are going to establish a general proposition that way, you will clearly not be justified in making it general unless you Asse made

^{&#}x27; 'For induction proceeds through all': Anal. Pri. S. xxiv. 685 15-29.

sure that your summeration of the particulars is complete: though, as has been said, it is not really an universal proposition then, but only 'enumerative': a thing which Aristotle fails to point out. The burden of the charge against Aristotle is however, not that he held that, if a general proposition is to be established by enumeration of particulars, the enumeration must be complete: but that he recognized so other mode of establishing general pronositions. And if this be so, then his Logic falls to pieces. For syllogism needs a general proposition for its major premise and us Aristotle himself insists we cannot be said to know the truth of the conclusion, unless we know first the truth of the premies! doubt of that will involve doubt of what is stated in the conclusion, so far as this is arrived at by inference, and not by direct experience independently of the inference. Now how can this condition be fulfilled, if our knowledge of any general principle rests on nothing better than an enumerative assurance that it holds good in every particular case? Let us take the principle that all matter gravitates, and symbolize it in the form 'All M is G'. If it is possible to know this without experience of its truth in every parcel of matter, we may use it in order to prove that this book must gravitate; and therefore may refrain from adding the book to one's kit in going up a mountain, or laving it upon a flower that is for show, or on the other hand may use the book to keep one's papers steady in a wind or as a missile against a neighbour. But if the principle can really only rest upon a complete enumeration, we must experiment with this book, before we can assert it : and then we shall know that this book gravitates by direct experiment, and our deduction thereof from the general principle will be superfluous, even if the enumeration be completeas it would only be, if this book were the last parcel of matter to be experimented with but even so, the deduction would be but a hollow show, and begging of the question. For let us symbolize any particular parcel of matter by µ. We propose to prove that μ is G, because all M is G, and μ is M; how do we+ know that all M is G? Only because u. u., &c. up to u. are G. and $\mu_1, \mu_2, \dots \mu_n$ are all the M, and therefore all M is G. Hence we use the fact that μ is G to prove the principle by which we prove that u is G. And the upshot of this is that we can never prove 4 An. Post. a. ii. 724 25-14.

anything by reasoning, until we already know it by direct experience : so that the use of reasoning, in order to infer that which we have not learnt by direct experience, must disappear. If we still try by anneal to any general principle to prove enything which we do not already know, we shall be appealing to a general princinle which we do not know to be true in order to prove a particular conclusion which we do not know to be true; for an Armstheri our knowledge of the truth of the general principle depends upon the knowledge of what occurs in the particular case in question among others. Such a procedure hardly commends itself to a same man. And if again it were said that however little we may be logically justified, in advance of experience, in drawing inferences about some particular from a general principle, yet our experience when it comes is constantly confirming the inferences we thus draw this. far from being a solution of the logical difficulty in which we have found ourselves, one ht only to be matter of perpetual astonishment. to a creature that reflects at all about his experience.

Such is the difficulty that arises, if there is no other means of proving a general proposition than by enumeration of all the particulars to which it refers 1; and to this criticism Aristotle is obnoxious, if he recognized no other 7 means. But did he recognize no other 7

Now Aristotle undoubtedly says that we arrive at our first principles by a process of Induction? He draws a famous distinction between the logical order and the order of experience; in the logical order, the general principle is prior to the sensible fact; in the order of experience, it is the reverse. To us, the particulars of sense are known first: the intelligible principles by which these are explained are known affart-arised; but Nature may be conceived as starting with principles or laws, and with these in her mind proceeding to the production of particular objects or events. Induction proceeds from what is first in the order of experience to what is first in logical order: from the apprehension of the sensible facts to the apprehension of the general principles, out of which we subsequently construct the sciences. Without sense-experience, there is no knowledge of intelligible principles; and the process of obtaining that knowledge out of sense-experience is Induction.

¹ Cf. what was mid above, in discussing the Dictum de omni et nulle.

See e.g. An. Post. B. xix. 100° 4.
 λόγφ οτ φύσει πρότεραν and ἡμῶν πρότερον : cf. p. 78, supra.

And this, taken together with his analysis of the Inductive Syllogism, might seem to settle the question; if only we could suppose Arisothe capable of overlooking the difficulty in which his whole system would thereby have been involved. But so far from overlooking, he shows in one passage that he had considered it, and uses his distinction between what is logically prior, and prior in the order of our experience, in meeting it. His view seems to have hear this.

The husiness of any science is to demonstrate the properties of a kind-anch kinds for example, as peometrical figures, species of animals or plants or the heavenly hodies. As we saw in the chapter on the Predicables he was influenced much by the fact that peometry and biology were the two most progressive sciences of his day. Science is concerned with kinds, as what are identical in their many members, and eternal. In demonstrating their properties, it starts from a knowledge of their definitions; such definitions cannot themselves be demonstrated; and for them we are dependent on experience, which familiarizes us with the nature of any kind, or of its properties, by means of particular cases. But though experience may thus acquaint us with the definition of anything, yet the essential nature of a thing (which is what a definition gives) cannot possibly be an empirical fact. It may be an empirical fact that all sailors are superstitions: but how can it be an empirical fact that a triangle is a three-sided rectilinear figure? For to say that anything is an / empirical fact implies that it might (so far as we can see) have been otherwise : and certainly we can conceive that a sailor may be either superstitious or not superstitious; but we cannot conceive that a triangle should not be a three-sided rectilinear figure, since if that-which is its essence-were removed, there would be no triangle left to be anything else. It will be asked, how do you know what constitutes the essence of anything? The answer is. that the intellect sees it; sees it, as we might say, intuitively, as something necessarily true: and this is the source of our assurance. in virtue of which we know the principles from which our demonstration proceeds more securely even than the conclusions we draw from them. But the intellect does not perceive it at once : experience of things of the kind is necessary before we can define the kind.

The use of these particular is, not to serve as the proof of a principle, but to reveal it: as the counters, for example, which a child used in learning the multiplication table, though one among immunerable instances of the fact that three times three is nine, are to be appealed to not because the general proposition could not be asserted unless it were tried and found true in the case of these counters as well as of all other countable things: for had the child learned with note, it would have been quite unnecessary to confirm the generalization by an examination of the counters; but because they serve as material in which the child can be brought to realize the truth of a numerical relation, which it apprehends forthwith with a generality that goes far beyond these particular counters. They are a means used because some countable material is necessary in order to realize the general truth; but the general truth is not accepted simply because it is confirmed empirically by avery instance.

Now we need not selv at the moment whether the sort of intellectual insight with which we do apprehend the necessity of numerical or spatial relations 1 can really serve us in determining the essence of gold or of an elephant or a tortoise; our present purpose is only with the nature of Induction, and the different senses in which the term has been used. And the purpose of the preceding personanh is to show that in spite of the analysis which Aristotle gave of Induction as a logical process, yet when he said that we get our first principles by induction, he had something else in his mind. Where your units are species, and you want to prove something about the genus to which they belong, there you may proceed by appealing to the fact, that it is found true of every species in the genus; there your reasoning may be thrown into the form of the 'inductive syllogism',-which is inconclusive unless every species is included in the premisees. But even there, from the fact that he regarded the conclusion as an universal and not merely an enumerative proposition, we must suppose Aristotle to have

There are philosophers who would not agree with what has been said of the nature and grounds of our assurance of the truth of mathematical principles. Some hold that they are only generalisations from experience, desrings their high degree of certitude from the great number and warrely of the instances in which they have been found to be true. This doctrine is maintained in a well-known passage of Mill's Lopic, Br. II. cc. -v-ii, to which be refers in his Jadobography as a crucial test of his general philosophical position. For a partial examination of the passage, crushing on far as it goes, see Jorosa's Part Lopic and other Minor Works, pp. 204-221.

thought that the mind grasped a necessity in that relation between the terms of the conclusion, at which it arrived by a process of enumeration: directly or indirectly, the connexion of longevity with call-learness was to be seen to be necessary and freed from the anneal to man or horse. And where your units are individuals and you want to discover the essential nature of the species to which they belong there you do not work by an inductive syllogism that summons all the instances to hear witness to the truth of your definition : for how could you summon the numberless members of a species? There is still a use for experience: we may still say that we know these things by induction : but the induction now is a nevelological rather than a logical process: we know that our conclusion is true, not in virtue of the validity of any inductive syllogism, drawing an universal conclusion in the third figure because the subject of the conclusion is coextensive with the particulars. taken collectively by means of which we neave it has in virtue of that apprehension of the necessary relation between the two terms. v which our familiarity with particulars makes possible, but which is the work of intellect or noise.

Such seems to have been Aristotle's doctrine and thus be avoided the bankruntov that would have enmed had he tangent that all syllogism rested on universal propositions, and that universal propositions rested on nothing but showing by enumeration that they held true in every particular instance that could be brought under them. But it may be said that thus he only avoids the Charybdia of moving in a logical circle to be snatched up by the Scylla of an arbitrary assumption. We are to accept the general propositions upon which every subsequent step of our inference rests. because our intellect assures us of their truth. This may satisfy the man whose intellect gives him the assurance; but how is he to communicate that assurance to others? If a principle is not arrived at from premisses which another admits, and between which and it he sees a valid process of inference to lie, why should be accept that principle? No evidence is offered, whose sufficiency can be tested. The inve dimit of an incommunicable intuition takes the place of any process of reasoning, as the means whereby we are to establish the most important of all judgements—the general propositions on which the sciences rest.

Of this charge Aristotle cannot altogether be acquitted; yet we

may say this much in his favour. Such an intellectual apprehension of the necessary truth of the principle from which demonstration is to start forms part of our ideal of knowledge 1; doubtless it seldom enough forms part of the actuality. But Aristotle idealized; he spoke of what, as he conceived, science in the fullest sense of the term involved, and forgot to state, or failed to see that the sciences did not realize it. And the prominence which he gave to the question 'What sort of premises does knowledge require?' led him to relegate to an inferior position the question 'How can the sciences as the var varidated their premises?'

He did not overlook this last question altogether: indeed he devotes to it a considerable portion of the longest of his logical treatises, the Topics: for when he asks by what sort of considerations you can prove or disprove that a proposition gives in its predicate the definition, or a property, of its subject, he is saking how you can prove ecientific first principles. And he know this: and among the nees of Dislectic or of the disputation whose methods he elaborates in the Topics, he places as its most peculiar use the examination of the truth of scientific principles. But he ought to have seen that, outside mathematics, we seldom have any other means of establishing general propositions upon the evidence of particular facts than those of the kind which he discusses in the Tonics. For the rest, his account of the logic of the reasoning by which the sciences do as a matter of fact support the general principles which they accept contains hints which are in advance of much modern 'inductive logic': though there is much in his conception of the character of the general principles which science seeks to establish. that is now antiquated. Science seeks to-day to establish for the most part what are called 'laws of nature'; and these are generally answers rather to the question 'Under what conditions does such

¹ With this provise, that for perfect knowledge all the parts of turth cought to seem nutually to involve each other. In mathematic, where slow we seem to achieve this insight into the accessity of the relations between the parts of a systematic body of turth, we find our theorems reinprecally examinated a relations would be revolutionized. Yet we do not need to wait till we discover how all other numerical relations are bound up with the truth that twice two is four, before we are as fully convinced of this truth as we are capable of becoming. Whether in every science we should desire when cut off from its implications, may be doubted.
Of.Top. a. 10.10** \$\frac{4}{3} \text{.}\$
Of.Top. is 10.10** \$\frac{4}{3} \text{.}\$

and such a change take place?' than to the question 'What is the definition of such and such as subject?' or 'What are its essential attributes?'! It is more in respect of the problems to be answered, than of the logical character of the reasoning by which we must prove our answers to them, that Aristotle's views (as represented in the Topica) are antiounted.

We may briefly indicate the nature of 'dialectical' reasoning, as Aristotle conceived it, and of the 'tonics' which it employed. Dialectic is contrasted with evience. Every science has its own neculiar subject-matter: geometry investigates the nature and properties of space, seology the conditions which determine the character and distribution of the materials which form the crust of the earth, physiology the functions of the organs and tissues of living bodies, &c. Each science, in explaining the facts of its own department, appeals to special principles, or Busy dayal: to the specific nature of its own, and not another subject-matter-to laws in accordance with which that particular class of facts is determined and not another class. The geometrician makes use of the axiom of parallels, of the notion of a straight line, of the definition of a cone or circle : but the nature of chalk or granite is indifferent to him. The geologist will use such principles as that stratified rocks are sedimentary, or that mountains are reduced by denudation; but he draws no conclusions from the definition of a cone. The physiologist in turn has his own problems to explain, and his own principles to explain them : that every tissue is composed of cells which multiply by division is a physiological principle of which we hear nothing in geology, while the laws of denudation contribute nothing towards the explanation of the growth of living bodies. Dialectic on the

I think this contrast is substantially true; though it is possible to bring many scientific investigations to-day under one or other of the types of question which Aristotle says we enquire into, yet looking to his example, one must confess that (see is satural) be put the problems of science to himself in a very different manner from that in which scientific men put himself in a very different manner from that in which scientific men put intervalued. Organize the property of it. 18 box, if it was viet in the contraction of the contraction, organized the property of it. 18 box, if it was vietnes.
One science does often to some attent use the results of another. In particular, of course, all the other sciences receive all they can into terms

One science does often to some extent use the results of another. In particular, of course, all the other sciences resolve all they can into terms of chemistry and physics. Yet looking (say) to Physics, Chemistry, Physics, Olemistry, Olemistry, None of the Chemistry, Olemistry, Olemistry,

contrary, has no peculiar subject-matter; all the sciences submit their principles to its investigation; the dialectician may ask whether a geometer would be right in saving that it is a property of a triangle to have its exterior angles count to four right angles : whether the geologist has rightly affirmed all stratified rocks to be sedimentary: whether the physiologist would do well to accept Spencer's definition of life, as 'the continuous adjustment of inner to outer relations'. And in debating such questions, the dialectieian will invoke not enecial, but common principles, sound doval 1i.e. not principles whose application is confined to the science be happens to be investigating, but principles of universal application: as, for example, that what is common to the genus is not a property of the species whence it follows that since all rectilinear figures have their exterior angles count to four right angles, this is not a property of a triangle, or in other words, that it is because a figure is rectilinear, and not because it is three-sided, that this can be predicated of it: it is for the permeter to show that all rectilinear figures have their exterior angles sonal to four right angles: the dislectician's business is to show that it cannot therefore he called a property of a triangle, as such. Or again, the dialectician may sak, with regard to Spencer's definition of life, whether the distinction between 'inner' and 'outer', on which it rests, is clear : for he knows that the terms of a definition should be clear, though he does not necessarily know physiology; and if Spencer, or his

him from illustrating it as it would be illustrated now, and his remarks on the subject are open to a good deal of criticism. Cf. As. Post. a. xiii. 78b 82-70e i8

Let Assel. Fost. a. x 79: 11-22, xi. 77: 26-24, xxxii. 88: 81-83, %-9-29.
In the second of these passages, aristotle gives as examples of 'common principles' the Law of Contradiction, that the same proposition cannot be at once true and false, and the mathematical atom that the differences of the contradiction of the contr

disciples could not show precisely what it means he would say the definition must be faulty; and if they replied that 'inner' meant within the organism and 'outer' outside it he would ask whether all material eveterns which changed inwardly in response to changes ontride them are living bodies: for he knows that a definition should not apply to anything except the species defined, and if this expression does it cannot be a definition : or he might ask whether many of the peculiar processes of living bodies are not apparently initiated from within the body : and if the answer was affirmative. he would again object to the definition: for though it is not his business to know whether any of the peculiar processes of living bodies are initiated from within or not (and therefore he has to ask the physiologist how that matter stands) it is his business to know that a definition must include everything essential to the thing defined : so that if there are such processes, a definition of life which excludes them must be a wrong one. Or lastly the dislectician might ask the conlocist if there are not some igneous make that are stratified . not knowing as a dislectician, the answer to that question, but knowing that, since igneous rocks are not sedimentary, the existence of igneous rooks that are stratified would unset the geologist's proposition; while if the geologist were able to answer the question in the negative, he would so far have come out victorious under examination.

All these general principles, to which the dialectician appeals, are called topics?: it is a topic, that what belongs to the genus is not a property of the species; or that what in some particular instance is absent from a species is not a property of it; or that the terms of a definition must be precise, or that it must be commensurate with what is defined. All these principles hold good in any science; it matters nothing what the species may be, or what the property, or what the definition. A man therefore whose mind is stocked with principles of this kind has points of vantage, as it were, from which he may proceed to attack or defend any definition, any predication of a property; they are topics in common, 'common_applaces,' points of view whence you may approach to the consideration of the statements of any science. Just as a man who knows nothing of the truth of its premises may be able to detect a law in a sylic girm, so the dislectician, without a scientific knowledge of a subject, girm, so the dislectician, without a scientific knowledge of a subject,

1 rónos, loci, communes loci,

may know what sort of questions to ask, if he wishes to test a scientific man's right to affirm the principles he enunciates.

Aristotle's Tonics is written with reference to his doctrine of Predicables. He regards every proposition as asserting (or denvine) some accident, property, differentia, genus or definition, of its subject : and he asks, to what considerations are you to look, if you would know whether such and such a predicate does stand to such and such a subject in any one or other of these relations? Each of these considerations is a tonic. He details an astonishing number of them. They are of very different degrees of importance and value. Some are drawn from language. Look, he says, for example, to conjugate terms if noble is a property of just, then enable is noble; perhaps a man who affirmed generally that justice is noble might admit that it is possible in some cases to act justly and not nobly.1 Others are based on the principle that contrary things have contrary properties: so that you cannot say that the just is the equal, unless you can say that the unjust is the unequal. Some aim only at enabling you to determine whether an expression is elegant, according to accepted rules. But others are principles of great importance. For instance, there is what we might call the topic of Concomitant Variation 2: that is not a property of a subject which does not increase or decrease with an increase or decrease in the subject, and conversely, if you find two things increasing and decreasing together you may assert such connexion between them.3 Considerations of this kind enable you to judge how different concepts are related to one another; and relations between concepts furnish the principles with which the special sciences work.

It may be admitted that this treatise contains much that is trivial; that it throws together considerations, or principles, of great and of little cogency: that the problems of science assume other forms than determining the definition of a subject, its properties, or its accidents (although these problems occur too, and many problems which we should not express in those forms can be translated into terms of them). It may also be admitted that Aristotle had his mind fixed too exclusively upon debate. The answers to the questions asked were to come from the respondent the other disputant; but in building up the sciences, they must

Cf. Top. ε. vii. 186^b 15.
π τόπος ἐκ τοῦ μάλλον καὶ ἦττον.
s.g. Top. ε. viii.

tome from the field and from the laboratory. Aristotle would have a man test any scientific doctrine that is not forward by interrograting its maintainer; the man of science must test those which he himself or a fellow worker puts forward by interrogating nature. It would be easy to do Aristotle an injustice on this head. It may be assumed after all that the respondent testifies to what he has seen; and Aristotle was alive to the importance of collecting and recording facts.1 But the Topics is a treatise on the art of disputation · dimutation sime after all more at silencing an opponent than at establishing truth . and though we are told that Dislectic has its use as much in the examination of the principles of the sciences as in the conduct of a disputation, it is in the latter enirit that it is expounded. Nevertheless, in the distinction drawn between scientific and dislectical reasoning, as illustrated above, and in its account of the general nature of the considerations to which one must appeal in any defence of the principles of a science. the Topics is a work of great logical value.

What, then has Aristotle to say about Induction?

- 1. He gives the name to a formal process of inference, by which we conclude a proposition to hold universally of some class, or logical whole, because an enumeration shows it to hold of every part of that whole. This is what has been since called Induction by Complete Essumeration, or Perfect Induction; and he shows how it might be thrown into the form of an Inductive Selfogism.
- 2. He points out that our knowledge of scientific principles springs historically out of our experience of particular facets; though its certainty rests ultimately upon an act of intellectual insight. And he gives the name of Induction to the process in which the particulars of our experience suggest to us the principles which they exemplify. But this is not a formal logical process from premises to conclusion; and it is not the induction (in this sense) which leads us at the end to accept such principles, but our intellect, or row.
- 8. He shows where (presumably in default of the necessary insight and searmance from our intellect) we may look for reasons for accepting or rejecting any principles which a science puts forward. He does not give to this procedure, which is of a formal logical kind, the name of Induction, but calls it Dialectic; nevertheless what he says on this head is of much the most importance from the Assach Pris. 3.11.

point of view of scientific method, and comes much closer to what modern writers understand by Induction.

Thus he admitted that our knowledge of general principles comes from our experience of particular facts, and said that we arrive at them by Induction; but the only formal logical process which he described under the name of Induction was that 'Perfect Induction' which clearly neither is nor can be the process by which the sciences establish general propositions; while the kinds of process which they really do employ, so far as they appeal merely to the evidence of our experience, he described under a different name. It is not surprising that some confusion has resulted.

The critics of whom Bacon is the corvohacus, recognizing with Aristotle that we discover universal truths by induction, attacked him for saving that we only discover them by complete enumeration. which he had not said; and finding the name of Induction given to no other formally valid process than this 1, supposed he had nothing else to say of the processes by which such truths are reached. Bacon himself attempted to systematize the process of discovering and proving them in a way which undoubtedly possesses value, and no less undoubtedly owes much to Aristotle : but as the Aristotelian ideas on which it is based do not occur in the Organos in connexion with suggests, he hardly realized how much he was borrowing. His analysis is offered in connexion with an unworkable theory of the nature of the problems which science should set itself to solve. To put it summarily, he thought that a list of the several sensible properties of bodies should be drawn up, and that men should then try to discover on what particular principle of corpuscular structure in the bodies that exhibited it each property depended. There was nothing in the conception of any particular principle of structure, which would lead you to anticipate that its presence would involve any one sensible property more than another; you could not tell. apart from experience, that a particular motion of the component particles of a body would exhibit itself to the senses as heat, or that a particular disposition of its surface particles would show as white and another disposition as black. Suppose we were to symbolize the sensible properties of bodies by Roman letters, and the principles

¹ It was also given to Induction by simple enumeration—i.e. to any attempt to prove a general proposition by merely citing a number of instances of its truth; but this is not a formally raild process.

of corpuscular structure in them on which these depend by Greek letters: how are you to prove whether a property a is connected with a or a or s? Bacon's answer is as follows. He called the principles of commenter structure Forms; whatever he the Form of a given property a it must be so related to a se to be present in every body in which a is present, to be sheent from every body whence a is absent, and to increase or decrease in any body as a increases or decreases. Our problem then is, as he says, at increnister nature alia (the Form) over cum nature data (the sensible property) perpetuo adeit, abeit, crescat atous decrescat. How are we to solve it? No mere enumeration of instances in which a sensible property a and a Form a are present together will prove that they are thus related, and that a is the Form of a: for your enumeration must be finite but your conclusion is to be universal. You may find a hundred bedies exhibiting both a and a: vet the presence of one may be quite unconnected with the presence of the other, and you may find a body to-morrow exhibiting one without the other. We must proceed then by exclusions. Where a hundred instances will not prope an universal connexion, one will dispress it. This is the corner-stone of his method: major set via instantiae negatione. If we had drawn up an exhaustive list of the different principles of corpuscular structure present in bodies in different combinations, all we should have to do would be to find instances in which any of these was present in a body that did not exhibit the property a. or absent in one that did exhibit it, or in which it increased or decreased without a corresponding variation in the degree of the property, or vice versa. We could then confidently reject that Form : and when we had thus rejected every other Form, then we could confidently affirm that principle of corpuscular structure which alone had not been rejected to be the Form (or cause of the presence) of a given sensible property a. Our assurance would rest not on the positive testimony of its presence along with a in a number of instances. but upon the fact that we had disproved all possible rival theories.

It will be seen that this procedure presupposes that we know all the possible Forms, among which that of any particular sensible property is to be sought; and Bacon, though he promised to do so,

¹ Nos. Org. II. 4.
1 Nos. Org. II. 4.
2 Aristotle, Anal. Pri. 2. XXVI. 48º 14 dua 8è 8\text{hor for and robbaneauditus iori rob aaraonauditus iori and more fully. Top. 7. v.

never showed, and could not have showed, how we were to discover that. The procedure is formulated too under the ides, that the immediate task of science is to draw up a complete list of all the distinct sensible properties found in nature, and then look for what we should perhaps now call their physical basis. This idea was mistaken. But the fundamental principle of the method by which Bacon proposed to 'interpret nature', 'the principle on account which he gave it the name by which he called it, Exclassis, is correct; it is that where you cannot (as in Mathematice) see that a proposition sust universally be true, but have to rely for the proof of it on the facts of your experience, there there is no other way of establishine it than by showing that facts disprove its ivals.\(^1\)

Bason called this method inductive; it may be as well to point out at once that formally the reasoning involved is just that of a disjunctive argument. The alternative hypotheses (with Bacon, the alternative hypotheses as to the Form or physical basis of a particular sensible property) are so and so: such and such of them are false; therefore the one remaining is true. How we are to discover what the alternative hypotheses are, he does not explain to us; we are to prove that the rest are false by appeal to the facts of our experience; these facts he would have men methodically collect and tabulate, and in making use of them he relies upon the guencal principle that nothing can be the Form sought for which is ever present in the absence of the property whose Form it is alleged to be, or absent in its presence, or variable when it is constant, or constant when it varies; when he has got his premises, his conclusion follows according to the ordinary principles of disinactive reasoning.

Bacon wrote in the dawn of modern science, and proclaimed with splendid confidence its future triumple. His predictions have been fulfilled, perhaps to the extent, though not on the lines, that be anticipated. Spec est sus, he wrote, in inductions even 2; and as men watched the continuous progress of the inductive sciences, they came to think that induction was really some new form of reasoning, ignorantly or perversely rejected by our forefathers in favour of

¹ There are many very valuable remarks in Bacon's account of his 'Exclusiva' about the kind of instances which are of most evidential value (and he therefore calls them Proposites Instances); but a discussion of them would hardly be relevant to the present argument.
² Nov. Ov., I. 14.

the deductive reasoning, which they associated with the name of Aristotle, and now held to be in comparison an idle thing. To praise induction became a sign of enlightenment; but the praise of it ran ahead of the undestanding.

Those who did the most to advance the sciences had not the need or inclination to pense and analyse the arguments which they were so successfully building up : nor would it imply any disrespect to add that many of them probably had not the nower of doing so. It is no more necessary that a great scientific genius should be able to give a correct arcount of the methods he uses than that a great artist should be able to expound the philosophy of art: those can often do things best who are quite unable to explain how they do them. The chief scientific name in the history of speculation upon the logic of the inductive sciences in this country is that of Sir John Herschell; four writers in all, if we exclude those still living, have made the principal contributions to the subject. David Hume, in a brief section of his Treatise concerning Human Nature (Of the Understanding, Part III, Sect. xv), gives 'Rules whereby to indoe of causes and effects' which contain the pith of much subsequent writing : but the work, as he said himself, 'fell stillborn from the press': this section was not incorporated in the later and more popular 'Enquiry': and it had no influence on the exposition of Induction. Sir John Herschell's Discourse concerning the Study of Natural Philosophy and the various works of Dr. Whewell did, on the other hand, much to stimulate interest in the subject; especially since Whewell propounded an explicit theory of it. The help which he had derived from both is acknowledged by J. S. Mill, whose System of Logic for many years held the field as an exposition of inductive reasoning. To that more than to any other work is to be traced the prevalence of the opinion, that inductive reasoning, or Inductive Logic as the theory of it, is a discovery of the moderns—an opinion which certainly contains less truth than falsehood. The name induction may be said with him to have stood for more than a particular form of inference; it was the battle-cry of a philosophical school, the school as it is called. of experience. But as a result of this, and of its previous history, it has become one of the most confusing terms in Logic. It stands firstly for that induction by complete enumeration which Mill denies to be properly induction at all, but from which his influence

was unable to withdraw the name after the prescription of so many centuries. It stands secondly for the logical processes employed in the inductive sciences, so far as these infer from particular facts the principles that explain them are to what the nature of these logical processes is Mill had a theory different from Whersell's and others have since had theories different from Mill's. Thirdly Mill who admits that there are certain general principles segumed as true in the resentings of the inductive enimose gives the name to what he conceives to be the logical process by which these principles themselves are reached : a process that starts in his view. barely from a great number of particular facts, and without the help of any general principles at all bases prop these facts the general principles whereon all other industive inference rests. Many of Mill's critics have thought and have thought rightlyfor it is better to state one's position explicitly at the outset—that if the process by which these principles are reached were as be describes it, it could only be called an illogical process.1

It would have been possible to omit the foregoing historical sketch, and to offer a purely dogmatic account of what Induction is. and what it is not. But against such a course there were two reasons. In the first place, a new writer has no right to do such a thing. It is indeed necessary for him to put forward that account of the nature of the reasoning of the inductive sciences, which he believes to be true; but not as if he was only delivering an accepted tradition. And in the second place, unless the reader knows something of the history, he can hardly fail to be confused by the diversity of senses in which he finds the word Induction used. Men have rightly felt that an antithesis could be drawn between the inductive and the deductive sciences; though they can be classed only according to their predominant character, since no sciences, except the mathematical, are exclusively the one or the other. On the strength of this they have most unfortunately erected an antithesis between Inductive and Deductive Logic:

"The second part of Jarona's Principle of Science cogbt perhaps to have been included along with the four works meatined above (cf. ake Letz's Lopic, Bt. II. c. 71. Among contributions on the part of living writers to the criticism of Mill's doctrines (for the great saceptance which his views obtained has made criticism of him a prominent feature of much subsequent writing on Induction) may be mentioned Bradley's Lopic, Bt. II. Part it. cc. 2 and 3, and an excellent discussion in Professor Welton's Manual of Lopic, vol. ii. § 1850. unfortunately, partly because Logic is one; the science which studies the nature of our thought embraces equally the processes and of the inductive; but unfortunately also, because it has led to much misunderstanding of the nature of inductive reasoning itself. Inductive Logic has not really laid bare any new forms of reasoning; we have already seen that Bacon's Induction is a disjunctive argument. The true antithesis is, as Aristotle saw, the antithesis between Dislectic and Demonstration; or in more modern phrase, between Induction and Explanation. Or if any one likes to keep the antithesis between Induction and Deduction, and to call inference deductive when it proceeds from conditions to their consequences, and inductive when it proceeds from conditions to their consequences, and inductive when it proceeds from facts to the conditions that account for them? he will find

- a. that the two processes cannot be kept rigidly apart. Whoever infers from the facts of experience the conditions which account for them must at the same time in thought deduce those facts from those conditions.
- 6. that what has been called Deductive Logic, what Inductive Logic has been contrasted with, analyses forms of inference which, if the antithesis between Induction and Deduction be thus understood, must be called inductive. This will appear more fully by and by; it will be admitted now that, if it is true, though we allow a difference between inductive and deductive reasoning, we had better give up opposing Inductive and Deductive Logic.

¹ The two antitheres are not quite identical, because some dislectical arguments are not inductive, and explanation is not demonstrative unless the premises from which it proceeds are known to be true. The reasoning from those premises is however the same, whether the premises are known or only believed to be true (cf. z. ziii, infre).

of induction is often registed anymorphing from particular facts to the restablishment of general principles, under which those facts are then brought by selvenpries, and so accounted for. And though we may also inductively establish from one particular fact the existence of another conditioning it, yet such a conclusion does imply a general principle of conditioning it, but such a conclusion does imply a general principle of another conditioning it, but there are universal connections (cf. next ch., and p. 502, infra). Moreover to have written general principles for conditions in the text would have narrowed unduly the scope of Deduction, which frequently, the condition of the conditions in the condition of th

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CHAPTER YIY

OF THE PRESUPPOSITIONS OF INDUCTIVE

'Way is a single instance in some cases, sufficient for a complete induction while in others myriads of concurring instances. without a single exception known or presumed on such a very little way towards establishing an universal proposition? Whoever can answer this question knows more of the philosophy of logic than the wisest of the ancients, and has solved the problem of Induction '1 However we may think of the knowledge possessed by the wisest of the ancients, the question which Mill asks is no doubt an important one. By what right do we ever generalize from our experience? and how can we tell when we have a right to do so? To these questions we must now attempt an answer. Afterwards we may note what other processes of thought besides oreneralization enter into the sciences; and then we shall be able to realize better the true nature of that antithesis between induction and deduction which was moken of at the end of the last chapter

The present chapter will address itself to the question, by what right do we ever generalize from experience. This is the primary question. Sylogism never generalizes. Unless it is provided with universal propositions for premisess, it cannot arrive at them in its conclusions, and even so, its conclusion is never more general han its premisess. It is in sut this fact which raised the difficulty,

¹ Mill's Logic, III. iii. 8, concluding paragraph. Strictly speaking, a single instance never is sufficient—if we had really to rely on it alone without help from conclusions already drawn from other parts of our experience. Cf. Jevons. Pure Logic and other Minor Works, pp. 295-299; and also Lotes. Logic, §§ 252, 253.

also Lotze, Logic, §§ 252, 253.

The third figure, when both premises are singular propositions, may seem to furnish an exception to this statement, and it would hardly be a sufficient answer to restall the fact that this is the inductive figure: for

how to get the universal propositions which syllogism needs to start with. If experience gives us only particular facts, how are we to get universal conclusions out of them? A mere enumeration of particulars will justify a conclusion about no more than the particulars will justify a conclusion about no more than the particulars will justify a conclusion about no more than the special particular will provide the conclusion of the claim in any generalization to go beyond the observed facts on which the generalization is based, and to draw a conclusion true in any possible instance whicheave. By what right do we do this?

The answer is that all induction sessues the existence of universal connexions in acture, and that its only object is to determine between what elements these connexions hold. The events of our experience are no doubt particular, but we believe the principles which they exemplify to be universal; our difficulty lies in discovering what principles they exemplify; in that, a close study of particular facts will help us; but were we to be in doubt whether there are any such principles or not, no amount of study of particular facts could resolve our doubt.

There are many ways in which this assumption may be expressed. It will be well to consider some of these, and to ask what precisely it is that we assume. We may then show that (as has just been said) it is hopeless to attempt to prove the assumption by any appeal to experience; and ask ourselves what justification we have for makine; it

The commonest expression for it is the Law of Universal Causation, or (more briefly) the Law of Causation; again, we say that we believe in the Uniformity of Nature; but the same idea is implied in the distinction between essential and accidental circumstances, or in asking what circumstances are relevant to the occurrence of an event, or what are the material circumstances in the case. For only those circumstances can be called material, or relevant, or essential, without which the event would not have occurred, or whose non-occurrence would have made some difference to it; and the occurrence or non-occurrence of any particular circumstances can make no difference to an event, unless there is some connaction.

the question is whether a syllogism can generalize, and it is hardly considerat with anying no, to add that it can only do so when its character is inductive. But the statement may stand, because all conclusions in this figure are particular or contingent. We may aim at generalizing—at finding as judgment which is true universally; but we have failed, with such premises, to do the state of th

between them and it. Were everything in nature loose and unconnected, it would be impossible to say that an event occurred because of any one thing rather than another. All these phrases therefore imply Causation, and imply Uniformity.

Both the Law of Covertion and the Uniformity of Nature and phrases open to missinderstanding. There is a sense in which it is the huginess of induction to discouse laws of causation : in the plural the term refers to the various particular principles of connerion exemplified (whether we detect them or not) in the course of nature : it is equivalent to Laws of Nature, or Natural Laws such laws for example as that matter gravitates or that organisms reproduce themselves after their kind. Used absolutely and in the singular, however, it means the principle that there are such particular principles, and hence we speak of the Law of Universal Causation, intending to assert that sperviling has a cause, and that no change occurs except under conditions with which its occurrence is connected universally. And it is because we believe its occurrence to be connected universally with such conditions, whatever they are, that we speak of the uniformity of nature. We do not mean to deny variety, but only to assert the unbroken reign of law. That which collectively we call nature is a vast assemblage of substances of divers kinds diversely intermingled; interacting with one another in wave that depend upon their abiding character and their shifting situation; what we call single things are highly complex, and their properties and behaviour depend upon their composition, and upon the circumstances in which they are placed . we may believe that whenever a thing of precisely the same kind is placed in precisely the same circumstances as another, it will behave in precisely the same way; nor is more required by the principle of the Uniformity of Nature; and yet we may doubt whether such precise repetition ever occurs. Watch the movements of a waterfall, how it breaks into a thousand parts which seem to shift and hang, and pause and hurry, first one, and then another, so that the whole never presents quite the same face twice; vet there is not a particle of water whose path is not absolutely determined by the forces acting on it in accordance with quite simple mechanical laws. No one would suppose that because these mechanical laws are unchanging, the waterfall must wear a monotonous and unchanging face; and so it is, on a larger scale, with the

course of nature. Nature is uniform in the sense that under like conditions like events occur; and in fragments, as it were, she is ever presenting us with the repetition of conditions that have been fulfilled before an that in fragments there is recovered of like events enough. But sooner or leter because the enventeding oircumstances are not quite the same as before, the course of like events is broken in upon: from the beginning the likeness was probably not complete. Were it indeed possible for the procession of events to bring back precisely the state of things which had existed at some moment in the nest then it must follow from the principle of the Uniformity of Nature, that the same procession would recur, and terminate again by reinstating the phase in which it had begun : so that the history of the world as a whole would really repeat itself indefinitely like a recurring decimal, and to a spectator who could watch it long enough, might seem as monotonous as the music of a musical box which, as it played, somehow wound itself up, to pass always from the conclusion to the recommencement of its stock of tunes. But nothing of this kind occurs : and the uniformity of nature is consistent, as Mill said, with her infinite variety.

But it may be said, the Law of Causation is one thing, and the Uniformity of Nature is another; every event may have a cause that the same cause need not always produce the same effect, nor the cause of the same effect be always the same. The human will, for-rample, is a cause; but it does not always ack in the same way under the same circumstances; to-day in a given situation I may act meanly; yet it is possible that in a situation of the same kind I may act better to-morrow.

The freedom of the human will is a peculiarly difficult problem, not to be argued here; doubtless there are some who so understand it (if understanding is then the proper word) as to make it an exception to the Uniformity of Nature. Some would say that, in this sense is to assert mere chance, the happening of events for no reason, the very negation of cause; for they hold that there is no causation which does not act uniformly. Others would make an exception to that principle in this one case; but even if we were to allow it, we should still have to say that, except so far as a cause is of the nature of the human will, there is no meaning in a cause which does not act uniformly.

Let us ask what is involved in the conception of a cause not acting uniformly: we shall see that it is the same as if we denied the existence of causal connexions altogether. For suppose that every event had a cause but that there was no resson why the same event should have the same cause or produce the same effect on different occasions. There need therefore he no annearance of order in nature at all but things might hannen just as if all changes were fortnitons. As it is we believe that plants produce seed after their kind: we do not expect to mather pranes of thorns, or fire of thistles; where we see garden fruit upon a wild stock, we look for a graft, convinced that the same stock will only bear different fruit in virtue of some material difference in the conditions. If any plant might produce any seed, or any seed any plant, and it was impossible to discover, in such circumstances as graft or soil-because no reason of the kind existed-why the same plant produced now one seed and now another, or the same seed now one and now another plant, then we should just deny that there was any cause for the things that happened. We should not say that there was always a cause, though the cause need not act uniformly. If two plants, whose nature is really the same, can determine the growth of totally different seeds, how can we call either the seed of that plant at all? Grant that a seed may sometimes be produced by a plant of its own kind, and sometimes by a plant of another kind, without any difference of circumstances, and merely because causes do not act uniformly, and you have really granted that anything may produce anything: flint and steel may produce seed instead of a spark, and oil raise the waves or quench a conflagration. But to say that anything may produce anything is to empty the verb 'produce' of all its meaning. For the causal relation is a necessary relation, such that if you have one thing you must have another. 'To add that it does not matter what the other is, destroys the force of the must. The distinction between essential and accidental, material and immaterial, relevant and irrelevant, will vanish. So long as causal connexions are universal, there is a meaning in it. That is essential to health, without which health is impossible and that is accidental to it which (though doubtless it has its effects) has no effect upon health. But if exercise, which is essential to my health to-day, should suddenly and without any change in my condition give me epilepsy tomorrow, while the loss of a letter in the post somewhere in the antipodes should on the following day cure my epilepsy, then it would
be impossible to say that anything was accidental, or anything
essential, to the same result for two minutes together. And the
discovery of the causal connexions that determine the succession of
events now would certainly be of no use in enabling any one to forecast the future; because the connexions themselves might have
altered in the meantime. It is difficult to see how all this differs
from denying that there are any connexions.

Causal connexions then are necessary and universal to assert causation is to assert uniformity of connexion. Were it otherwise. to discover them would mean only to discover the connexion subsisting at a particular moment; and we could not tell that such connexion would subsist the next moment. For this reseon, we could not generalize, even though we believed in the Law of Causation : nor indeed could we so much as discover what connexions did subsist at any moment. For since anything might produce anything, there would be nothing to make us connect a change with one rather than another of the events that were observed to occur immediately before it. No light would be thrown upon the problem by comparison with other instances, since, ex Appothesi, the cause might be different there. As it is, if the sun comes out when I hear the clock strike. I do not suppose that the striking of the clock causes the sun to shine, because it so often strikes without relieving the gloom, and is so often silent when the sun comes out. But when I reason thus I assume that if one event were really the cause of the other now, it would be so always. If it can be the cause now, and not another time, how am I even to tell whether it is the cause now or not? We spoke of the human will as an alleged exception to the rule that the same cause must always produce the same effect. We may notice here that just in so far as it is allowed to be an exception, human actions are allowed to be incalculable. And if everything were endowed with a will like man's, and all these wills were free in the sense in which some suppose that man's will is, then we should have no logical justification for any generalization whatsoever. But those who claim this freedom for the human will would attach no value to it unless the act to which a man was determined by his free choice produced effects that were necessary in accordance with universal laws.

There is no need then to distinguish the Law of Canastion from the Uniformity of Nature: for-bating the possible exception of the causality of the human will-a cause which does not act uniformly is no sense at all , and if we are looking for the presuppositions of inductive inference, it is plain that the only connexions whose evictorics would justify such inference are uniform connexions. But two cautions must be given here. First, it must not be imagined that uniformity is the fundamental element in the conception of causal connexion but accessity or law. Secondly we must be careful not to confuse a conditional with an unconditional necessity.

David Hume, whose enquiry into the meaning and origin of our ides of Causation was epoch-making in the history of modern philosophy 1 could find no other meaning for the statement that one event is the cause of another than that in our experience the one is always immediately followed by the other: and according to him the thought and expectation of this uniformity of sequence is all that is present to our minds when we assert causation. In agreement with this view. J. S. Mill (who differed from Hume on this matter chiefly in not drawing the logical consequences from the same premisees) defined a cause as the invariable and unconditional antecedent of an event. The word unconditional in this definition may seem to betray ideas inconsistent with the resolution of the causal relation into one of time: but Mill explains an unconditional sequence to be one that is subject only to negative conditions 2, and the negative conditions of any phenomenon 'may be all summed up under one head, namely, the absence of preventing or counteracting causes's: so that those circumstances are the cause of an event. upon which it follows whatever other circumstances may be present as well 4; and the relation remains one of invariable sequence after all. Now it is not denied that if any set of conditions a is the cause of an event x. x will be produced as often as the conditions a are fulfilled; and in this sense the sequence will be invariable; but we cannot intend to assert primarily that, when we say that a is

¹ Treatise, Of the Understanding, Part III; and Enquiry concerning Human Understanding, §§ iv-viii.

* Logic, III. v. 6.

³ Tb. III. v. 3.

More precisely, when there is nothing preventing it; and by the notion of preventing Mill presupposes the relation he is trying to explain; but if we are to avoid this petitie, we must interpret his statements as above.

the cause of s. For if a is the cause of s. the relation subsists between them in every case of their occurrence : it subsists between this a and this z: and it is clear that the relation between this a and this a cannot be the uniform secuence of all instances of a mon instances of a The action of light of certain wave-lengths &c upon a chemical surface prepared in a particular way may be the cause of the production of a photographic negative of a particular peak in the Himalayan mountains. I cannot mean by that that the production of all such negatives has been preceded by a similar assemblage of conditions on each occasion, since mine may be the only photograph ever taken of the neak in question. No event could have a cause until it had been repeated at least once, if the exerce of the causal relation lay in uniformity of sequence: nor could that relation ever be one subsisting between a and a in a determinate instance : and it is difficult to see how a causal relation which subsists between no determinete instances of a and a could enhaist at all So far then from the causal character of a sequence being derived from its uniformity, its uniformity is derived from its causal character. We avail ourselves of the uniformity which must characterize causal sequences so far as they are repeated, to determine which of the sequences that we observe are causal; and that is why the repetition of an event under diversity of conditions is of such assistance to us in determining what conditions are essential, or material, to its occurrence. But an event that was absolutely unique must just as surely have its cause, though we may be unable to discover what it is. For the causal relation has nothing to do with sumber of instances, so far as its existence—though not so far as its detection—is concerned; it is bound up altogether with the nature or character of things, and the nature of anything is not a question of the number of such things that may be or have been fashioned. We have seen indeed that a cause which does not act uniformly is no cause at all; but we may now see that were it otherwise, a thing would have no determinate nature. If a thing a under conditions c produces a change s in a subject s-if, for example, light of certain wave-lengths, passing through the lens of a camera, produces a certain chemical change (which we call the taking of a photograph of Mount Everest) upon a photographic film -the way in which it acts must be regarded as a partial expression of what it is. It could only act differently, if it were different.

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As long therefore as it is a and stands related under conditions a to a subject that is a no other effect than a can be produced; and to say that the same thing acting on the same thing under the same conditions may not produce a different effect, is to say that a thing need not be what it is Rut this is in flat conflict with the Law of Identity. A thing, to be at all, must be something, and can only be what it is To secont a causel connexion between a and a implies that a acts as it does because it is what it is . because, in fact, it is a So long therefore as it is a it must act thus: and to sesert that it may act otherwise on a subsequent occasion is to assert that it is something else than the a which it is declared to be. It may be replied that no two things ever are the same, and-what that renly must commit you to-that no one thing ever is the same for two successive moments. The fact of change is not disputed, nor the difficulty of finding two things that are qualitatively the same. But if the effect of the second is different, that must be because of its qualitative difference from the first, and not merely because it is a second : and so far as it is qualitatively the same, the effect must be the same also: it being understood of course that to sameness of effect qualitative sameness is equally necessary in all the material conditions. To deny this is to deny the possibility of reasoning altogether. If we cannot truly make the same assertion about a number of things, then, as Aristotle observes, there will be no universal, and so no middle term, and no demonstration.1 For an universal judgement connects a certain attribute with a certain subject in virtue of their content and without regard to the frequency of their existence. If we can do this, we can make the same assertion about all things of such and such a kind; if we cannot do it, we are left with nothing but particular things whose attributes must be ascertained from inspection or experience of themselves; and not by transference of what we have once found true of such a kind of thing to others of the kind. What holds for the relation of subject and attribute holds in this respect co ipeo for that of cause and effect. To suppose that the same cause-other things being equal-can have different effects on two occasions is as much as to suppose that two things can be the same, and yet so far their attributes different. To reply that two things cannot be the same, and that the same cause cannot be

1 Anal. Post. a. xi. 77* 5-9.

repeated, is either to miss the point, or to shandon reasoning. If it is meant that two complex things cannot be qualitatively the same. nor can conditions precisely the same in kind ever recur, such an objection misses the point. One need not maintain that such identity or such requirement in fact comire though it is not perhaps inconaciveble that it should all that is maintained is that so far as things are qualitatively the same they have the same attributes, and so for as conditions precisely the same in kind recur they must if there is such a relation as cause and effect at all have the same effect. If on the other hand it is meant that there is no qualitative sameness in what is numerically different we can only say that if so. there is no reasoning. But this denial of identity between different things is what is really at the bottom of the attempt to resolve the causal relation into uniformity of sequence. For the causal relation which connects a with a connects a cause of the nature a with an effect of the nature s. The connexion is between a and s as such. and therefore must hold between any a and any a, if they really are a and a respectively : in other words, it must be uniform. The denial of this is just the denial of universals; while if there are universals—the same content in numerically divers things—the relations between them must be universal. If, on the other hand, we are to substitute for a relation one and the same in all its instances a mere similarity between the relations that connect the respective terms of many different instances-if for the relation between a and s as such we are to substitute the uniformity between the relation of this a to this x, and of that a to that x, and of the other a to the other a then we are substituting for the common content of many things a bundle of things united by nothing in common. How then can we speak of them as things of a kind, or hold our sequences uniform except in the fact that they are sequences? 1 The cause of an event might then indeed be anvthing to which it stood in a relation of sequence at all, and need no more be the same on different occasions than its antecedent need be: since we should have agreed that it was impossible that the sequence of the same thing a upon the same thing a should ever be repeated.

We may pass now from this to the second of the two points mentioned on p. 376. If it is thus necessary that causal relations

¹ Strictly speaking, even sequence could not be a feature common to two successions.

should be uniform, it is all the more important that in speaking of the Uniformity of Nature we should not confuse conditional with unconditional necessity.

We saw shove that the Uniformity of Nature was consistent with any degree of variety in the course of events; but that it implied that the principles in accordance with which these events occur or what we often call the Laws of Nature are unchanging In other words, the uniformity which a particular law requires in events can admit of no exception : for an exception would mean. that events did not recessfully hannen in accordance with the law : and a law that changes is no statement of the way in which events ment hannen. Nevertheless we often use the term Law of principles which we should not be prepared to declare unchanging; which, as we might say do not hold good always. In the strictest sense of the word, no doubt, a law must hold good always and unconditionally 1; but we use it in a looser sense as well. It is important to realize this distinction, and also to consider how far, when we speak of the Uniformity of Nature, we mean to assert that what are commonly called 'natural laws' are unconditional.

The first law of motion is an example of a natural law which would perhaps be regarded as unconditionally true—that every body persists in its state of rest, or uniform rectilinear motion, until it is interfered with by some other body. The same might be said of the law of universal gravitation, that all bodies attract one another with a force that varies directly as the mass, and inversely as the square of the distance. Compare with these the principle that acquired characters in a plant or animal are not inherited. Supposing this to be true (for it is still sub sudice), yet it is not true unconditionally. We are not in a position to say that living things could not be so organized, in respect of their reproductive system, as to make acquired characters heritable, but only that, with the organization which we find, they are not heritable. That organization , therefore conditions the truth of our principle. Just as the prevailing necessity for sexual union in the reproduction of all multicellular organisms does not exclude arrangements in some species which make them parthenogenetic, so there might possibly be conditions

¹ Cf. J. S. Mill's definition of Laws of Nature in the strict sense as 'the fewest and simplest assumptions, which being granted, the whole existing order of nature would result' (Logic, III. iv. 1).

under which the non-heritability of acquired characters held good no longer. And as conditions may change, those realized at one time not being realized at another, so the conditional principles which prevail may change with them. It appears to be the case that living matter can only be produced from other living matter; there is no spontaneous generation of it from the inorganic; omservess es vice. But many scientific men have supposed that though this is true and necessary now, yet in an earlier period of the earth's history, under very different conditions of temperature and so forth, it was not no.

Conditional principles are necessarily derivative: i.e. their truth. so far as they are true, follows from some unconditional laws, which under given conditions involve them as their consequence. They therefore admit, theoretically if not as yet actually, of explanation, But derivative principles, or principles admitting of explanation. are not necessarily conditional. For when we call a principle conditional, we mean that the truth of our principle depends upon conditions which are not stated in it. If we bring the conditions into the statement, then, though it remains derivative, it is conditional no longer. Supposing that we knew precisely those conditions of organization in animals and plants which made acquired characters non-heritable; then the statement that in animals or plants of that organization acquired characters were not inherited would be unconditionally true, although no doubt it would admit of explanation. It would probably not be called a law of nature, because it would be derivative; but it would have all the necessity of a law of nature.1

The Uniformity of Nature then involves the truth, without exception or qualification, of all unconditional laws; but conditional principles admit of apparent exceptions, without derogation to its truth; and if we are ignorant of the conditions within which these conditional principles hold good, we cannot tell when the exceptions may not occur. To return to our previous illustration: if we do not know under what conditions of organization acquired characters are and are not heritable, we must be prepared to admit evidence that in some cases they have been inherited. Where, however, exceptions occur to some conditional principle, they constitute no exception occur to some conditional principle, they constitute no exception to the truth of the Uniformity of Nature; but only imply

^{&#}x27; Cf. c. xxii, infra; the non-reciprocating causal relations there discussed are all conditional.

that the conditions, under which that principle held good, are not fulfilled in the exceptional case. And the exception leads us, not to deep that 'Nature is uniform', but to revise or to determine more precisely the particular principle which we have found invalid. It is only unconditional laws that can have no exception.

It becomes therefore important to determine if possible when we have discovered an unconditional law. We may disregard here those derivative laws, which we may be capable of explaining from others more general than themselves for the question whether they are unconditional is the same as the question whether the more general laws from which they are derived are so. Now if wa have no better reason for accepting a law as unconditional than that hy assuming it to be true we can account for the facts of our experience, then though we might provisionally accent it, we can hardly be content with our warranty; for perhaps some other law might also account for the facts. But if (and this, as we shall see hereafter, is a distinction of the first importance in inductive theory) -if, without assuming it to be true, it is impossible to account for the facts of our experience, we should have to suppose it unconditional: though such impossibility may be hard to establish. Still, we should not be fully satisfied : for had the facts been otherwise, we need not have admitted the law; and we do not see, except on the hypothesis that the law is true, why the facts might not have been otherwise. Complete satisfaction would only come, if the law which the facts had forced us to recognize should, when considered, annear self-evident

Are there any unconditional laws known to us? There is nodoubt that the fundamental principles of physical science are often
so considered. It is held that we have discovered certain physical
laws prevailing throughout the material order takes place; that thee
laws are mechanical; and that nature is, in truth, and in the last
resort, a purely mechanical system. And this view is supposed to
so confirmed by the character of the principles with which physical
science works. A great deal is purely mathematical; and about
mathematical principles at any rate we can say that they are
unconditional because self-evident; no apparent exception would
make us doubt them or revise them; we should only doubt the fact
which was supposed to constitute the exception. And some of the

most general physical laws have often been held to possess the same self-evidence; the first law of motion, and the laws of the conservation of energy and the conservation of mass, are instances. That anything should occur in the material system unconformably with these principles would then present the same kind of contradiction as that two and two should make five. The explanations of physical science, at least so far as they rested on laws of this kind, would be complete and final.

On the other hand there are very serious difficulties in the way of admitting the finality of the explanations which physical science offers of events in the material system. These difficulties arise from the relation of some of these events to human and also to infra-human, consciousness. Experience reveals to us a correspondence between certain changes of a material kind in the nervous system, and changes in our consciousness. No satisfactory theory of this correspondence has yet been found: it cannot be said that what is involved in treating as unconditionally true the principles of physical science is satisfactory in theory. For if all physical changes are to be explained as determined altogether according to physical laws, then they are purely mechanical; the existence of consciousness has made no difference to anything which has occurred on the surface of the globe; we are, in Huxley's language, what Descartes thought the lower animals to be, conscious automata: and the laws of matter and motion would of themselves have sufficed (if we may borrow an illustration from Professor James 1) to produce the manuscript of Shakespeare's works-and indeed every edition of them-though Shakespeare had been no more than a lump of matter as devoid of thought and feeling as the pen he wrote with, or the automaton of Vaucanson.

Such a conclusion is undoubtedly paradoxical, but paradox does not by itself constitute a refutation. It is, however, impossible to account on physical principles for the facts of consciousness. They cannot be physical processes; and a mechanical theory demands not only that a physical event should depend only on physical conditions, but that physical conditions should determine only a physical result. Mass and energy are to remain constant in amount, but to undergo redistribution in accordance with certain kaw, which can be expressed

¹ Principles of Psychology, i. 182.

in a mathematical formula enabling us to calculate the precise degree of change in one direction that will be involved in a give degree of change in another direction. In these redistributions there is no room for knowledge or feeling among the 'forms of energy'; for mechanical conditions are to have their complete mechanical equivalent, in terms of matter and of motion, potential or setual. Thus to a physical theory of the world consciousness remains unaccountable: such a theory therefore cannot be complete or final.

Now philosophy suggests that in the last resort, instead of explaining consciounces in terms of physical law, we shall have to see in physical law a manifestation of intelligence. The whole material order is an object of apprehension; therein, however, it stands related to minds that apprehend it; it and they together form the complete reality, or res complete; and they cannot be understood except together. There is, however, another paradox here; for what understands is mind, and so one term in this relation has to understand both itself and the other term.

It is not our business to discuss here this central metaphysical problem. But we are concerned with the conception of an unconditional law; and a self-evident principle must be unconditional. With regard to the claims of physical science to have discovered principles really unconditional we must therefore either say that they are not self-evident, or admit that they are unconditional.

If we adopt the latter alternative, then we shall hold that whatever transformation our view of the material order may undergo, yet the interconnexions of events within it, the connexions of cause and effect there traced, will as it were be taken over es blee, unbroken and undistorted, by any interpretation of the universe which takes knowledge as well as its objects, mind as well as matter, into account. A moving body may be something else than a moving body; but its motion will for ever appear determined in accordance with physical laws. If, however, we adopt the former alternative, the principles of physical sincers may not be unconditions.

Now we are perhaps sometimes too hasty in supposing that we see the necessary truth of physical principles. The speculations of men of science themselves have lately called in question the doctrines

¹ Hance M. Poincaré has recently said that a physical law is a differential equation. Address on the Principles of Mathematical Physics, St. Louis, U.S.A., Sept., 1904: r. the Momia, Jan. 1905, p. 3.

of the conservation of energy and of mass: 1 though doubtless without questioning the possibility of cetting some physical formula that will be unconditionally true. It might be said that in the first law of motion it is salf-aridant indeed that a hody will named in its state of rest or uniform rectilinear motion until something interferes with it, but not that interference can only come from another body: that the mathematical reasoning in physical science is necessary, but not the physical principles which supply the data to which mathematical reasoning is applied; and that the doctrine that a body can only be interfered with by another body is one of these. If these physical principles are only conditionally true. the same will hold of their results; and changes may occur in the material order not accountable in terms of physical conditions, and not conformable to physical 'laws'. Nevertheless, because these physical 'laws' are not unconditional there is nothing even so that conflicts with the Uniformity of Nature.

We need not here determine which of these alternative positions to take. But it must be pointed out with regard to the latter. that if physical laws are conditional in the way suggested, there is an important difference between them, and the conditional principles with which we are already acquainted. For in the case of a conditional principle like the non-heritability of acquired characters, we conceive that the laws on which it depends might be found, and would be in codem genere with the principle itself : i. e. the principle stated with the conditions to its truth (and stated then in a form unconditionally true) would be derivative in an intelligible way from principles more general, but from principles that hold like itself of what is material. On the other hand, if the fundamental physical laws are only conditionally true, yet it is impossible to derive them from physical principles more general than themselves ; and so the kind of explanation which is possible of other conditional principles (when their conditions are taken into account) from principles of the same sort with themselves, whereof they are really but examples, is here precluded. Supposing that there are, if we may so put it, spiritual conditions upon which the movements of bodies in the last resort depend, and under some of these the first law of motion holds good, and not under others, then physical science at any rate cannot deal with those conditions.

1 Cf. Poincaré, op. cit.

For this reason, physical science will ignore this alternative. If the non-mechanical conditions upon which physical changes depend (supposing that such there are) cannot be ascertained and formulated in a way which enables physical science to take account of them it will treat them as non-evictent. It is of no use to recent a factor whose mode of entire is prescertainable. It must remain for science -what the will is mon one theory of human freedom-a source of murely inceleplable and to it irrational interference. But irrational interference is just what cannot be supposed to occur. No doubt an interference which admits of explanation according to law is not irrational. but, if the law is unsacertainable, it is as good as irrational. And this attitude of physical science has the practical justification, that if events are once admitted to occur in the material order whose conditions are unascertainable within that order, there is no point at which we can draw the line. Only by sesuming that it can explain everything is it possible to find out how much it can explain in physical terms.

What has been maintained then is this :- It is part of the conception of Cause to act uniformly : and so far, the Universality of Canastion and the Uniformity of Nature are the same thing. But it consists with the Uniformity of Nature that many principles which we use to explain events should be only conditionally true : these admit of exception; but no unconditional principle admits of exception. If a principle is self-evident, it must be unconditional: and the fundamental principles of physical science are commonly treated as unconditional. On the other hand, there is much in the world not explicable from principles of physical science. But if any of them are self-evident, what follows from them must be retained, and not contradicted, in any complete explanation which takes into account what physical science leaves on one side. And if the principles of physical science are only conditionally true, yet so far as the conditions under which they do and do not hold good are unascertainable, physical science may fairly treat these conditions as non-existent.

After those explanations and qualifications we may say indifferently that the industive sciences presuppose the Law of University cansation or the Uniformity of Nature. But as it has been held by some to be the task of induction to prove this principle¹, ¹ Cf. e.g., Mill. Loric, III, xxii. it may be worth while to show that that is impossible. It is alleged upon the view now to be considered that our experience of the great extent to which like antecedents have like consequents is the ground upon which we believe that this is universally the case. Against this we may point out in the first place, that such an inference assumes the course of events in one time and place to be a guide to their course in other times and places: which is really the very principle that is to be proved. As Lotze has urged, if a research can be given for the inference it retts on some previous assumption: and if no reason can be given for it, what is its force?1 Next, it is to be noted that two very different kinds of aroument. are confused. It is supposed that to infer the uniformity of nature from the observed succession of like consequents upon like antecedente is an argument of the same kind as to infer an universal connexion between two events a and a from the frequency with which one has been encoceded by the other. This, however, is not the case. We infer under such circumstances an universal connexion between a and a because upon the assumption that there is some set of conditions upon which every change follows uniformly, it seems the only thing consistent with the facts of our experience in the case of m to suppose the conditions to be a. Upon the assumption that there is some set of conditions upon which every change follows uniformly, the uniformity in general has not got to be inferred; while, if that assumption is to be made in neither case, an universal connexion between a and a could not have been inferred. There is therefore no parity between the two arguments. That may indeed be seen if we attempt to put them into symbolic form. In the one case we reason that because a has in many instances been followed by s. therefore the connexion a-x is universal. In the other we reason that because a has in many instances been followed by a. and b by s. and so forth, therefore there is something by which every other event, such as p. q. or r. will be uniformly followed. Again, the uniformities which are said to be the empirical basis of our generalization are not really matter of direct experience. We have said above, that the particular connexions which we believe to prevail in nature have been inferred with the help of the assumption that all changes occur in accordance with laws. But if any one likes to question this, he must at any rate agree that most of the

uniformities in which we believe have been inferred somehow . very little has come directly under our observation. We believe that winds are caused by differences of atmospheric pressure : these differanger of atmospheric pressure are themselves inferred rather than obcorred but weiving that for what proportion of winds have they been noted? We believe the sound of the notes of a nisne to be caused by the striking of strings . for what proportion of the notes which we have heard have we first seen the strings struck by the hammer? It is needless to multiply such examples . but when it is allowed that we are justified in inferring the uniformity of nature to hold good universally because we have direct experience of it over vastly the larger portion of the field, it is important to point out that our direct experience of it is singularly small, and that the vastly greater proportion of what we believe ourselves to have accertained is matter not of experience but of inference. Now we may offer the empiricist his choice. If this inference is made by the help of the assumption of the uniformity of nature. its results cannot be used to prove that assumption. If it is made without that help, by his own admission it falls to the ground, for the inference of any particular uniformity is supposed to need that assumption: and so he is not left with experience sufficient to justify his peneralization. We may present the argument against his position in vet one more light. The essence of his contention is, that we must come to the facts of experience without any preconceptions: we must have no antecedent view of what is conceivable or possible. For all that we can tell to the contrary until experience has instructed us, anything whatever is possible; and if it occurred with sufficient frequency, anything would be conceivable. Now, it will be admitted that if there are a number of independent alternatives all equally possible, an event that is inconsistent with only one of them leaves us quite unable to decide between the rest. But if, as the empiricist insists, all things are antecedently equally possible, then all proportions of regularity to irregularity in the world are equally possible antecedently. All events may occur in accordance with uniform principles; or there may be no event which ever has the same consequent twice: and between these two extremes an infinity of alternatives may be conceived, among which we cannot select except upon the evidence of experience. The extent to which regularity, or uniformity, prevails may therefore be limited in any

conceivable way, whether as regards place, or time, or subject, There is no reason why the succession of like consequents upon like antecedents, while exemplified at other times and places, should not fail in the hitherto unexplored parts of Central Asia or on all Fridays subsequent to the Friday in next week Nothing less than this is involved in the refusal to prejudge experience. But if that is so experience itself can never enable us to prejudge. For why should any degree of uniformity observed till now in the succession of events induce us to expect such uniformity to continue? It was antecedently as possible that such uniformity should continue till to-day, and then terminate, as that it should continue till to-day and still continue. The fact that it has continued till to-day has disproved what until to-day was a possible hypothesis, viz. that it might terminate sooner: but between its terminating to-day, and still continuing-two independent and antecedently equally probable alternatives with which that fact is equally consistent __it does not in the least enable us to decide. This argument will hold good, at whatever point in the series of time to-day may fall; so that we never get any nearer being able to infer a degree of uniformity which ones beyond what has been actually observed. It seems conclusive therefore against the view that the Uniformity of Nature can be an induction from experience, if by the term induction any legitimate process of inference is understood.1

- ¹ The last argument may be put in a way that will perhaps to some seem clearer as follows:
- An event which is equally consistent with two hypotheses affords no ground for deciding between them.
 g, g, if A and B keep a common stock of boots, and each uses every
 - e.g. if A and B keep a common stock of boots, and each uses every pair indifferently, footprints that fit one of these pairs afford no ground for deciding whether A or B has passed that way.
- It is admitted by those who regard uniformity in nature as empirical, that antecedently to experience all issues, so far as regularity and irregularity in the succession of events are concerned, are equally probable.
 By an issue is meant a certain course of events, however lone.
- 8. These alternative issues must be regarded as perfectly detached alternatives; i.e., antecedently to experience, the rejection of one issue would not give any ground for or against the rejection of any other. To samme that it would is to assume, antecedently to experience, the existence of such degree of uniformity as enables you to say that if one specific issue happens, another must or cannot.
- 4. That events should occur with any specified degree of regularity down to the end of the year 2000 A.D., and with less or no regularity, or in apparent conformity to different rules, thenceforward, is one such issue:

With what right then do we assume it? The answer to this has been given in discussing what we mean by it. To deny it is to resolve the universe into items that have no intelligible connexion. If the universe and the events in it form a eventematic whole then any change must be determined by comething in the nature of that whole, and for the same change to occur on different committee except under the same conditions is not consistent with its having a determinate nature. It is not of course denied that changes nertially the same may occur under conditions partially different . and the tack of disentangling the identities in what is nartially different is one of the tasks of the inductive sciences hut referie parities a proving about which it is very difficult for us to know in individual cases how far it is fulfilled—the same conditions must produce the same effect, and the same effect must have been due to the same conditions. The universe is otherwise unintelligible or irrational. If any one likes to accept that alternative, it may be impossible to reseon him out of it: for he has disallowed at the outset the appeal to reason. At least let him not maintain that, while the alternative is conceivable, experience proves that it is not the case 1

that they should occur with the same specified degree of regularity down to the end of the year 2001 a.D., and thence with less or none or other, is another such issue. And these issues are perfectly detached alternatives a priori. Let them be called X and Y.

- 5. The empirical observation of that specified degree of regularity down to the end of 2000 a.D. is equally consistent with the hypothesis that X, or that Y, expresses the truth. Therefore it affords no ground for deciding between them.
- 6. It would therefore be equally likely at the end of 2000 A.D. that the events abould thenceforward exhibit none or less of the regularity that they had hitherto exhibited, or conform to quite different rules, as that they should continue to exhibit the same regularity even for a year longer.
- 7. The dividing date might be taken anywhere; and one might take equally a dividing place or department of fact.
- 8. Hence the actual issue never affords any ground for preferring the hypothesis of a continuance of the observed regularities to any hypothesis of their discontinuance, complete or partial, with or without the substitution of other regularities, in any period, region, or department of fact, in which they have not been empirically verified.
- ¹ In speaking of causality in the present chapter, prominence has throughout been given to the conditions which determine successive sense. But so far as scientific explanation appeals to principles of interaction, it regards a thing as determined by what is contemporaneous with it and not by what is antecedent. Moreover, if the whole series of wents in time can be

Trix 1

regarded as an expression of the activity of that which is in some way exempt from subjection to succession, then what appears in time as future may have to be taken into account in giring a reason for the present and the second transplant of the second transplant in the

CHAPTER YY

OF THE BULES BY WHICH TO JUDGE OF CAUSES AND EFFECTS

WE saw in the last chapter that all inference from experience rested on our belief in universal connections in nature. If there are no givenmetances material to the occurrence of a landslip, it would he foolish to expect that any examination of the circumstances under which landsline have been found to occur would enable us to determine under what circumstances they will occur in the future. But if such universal connexions do exist, the examination may help us to detect them; and if we can detect them, we inso

tacto generalize.

Our problem then is how to detect them; and indeed the discovery of causes is the popular concention of the task of an inductive science. But cause is a relation 1: and how are we to determine -bet stands to what in that relation ? The relation itself connect be perceived. Events as they occur by no means display to observation the lines of causation that connect them. What we call the puerile fancies of the savage mind, which thinks that the incantations of a medicipe man will produce rain, or the plance of a witch wither the crops—or at a later stage of civilization that walking under a ladder, or overturning the salt, will bring disasterthese would never have arisen, if you could observe with what effect such incidents are connected, as you can observe that the medicine man is pesticulating, or the salt lying on the table. We may / observe the events, but never their connexions: these can be only indirectly ascertained by considering whether the events occur as they should if they were connected.

It is here comes in the working importance of the uniformity which is involved in the conception of a causal relation. All manner of events are occurring simultaneously at every moment;

^{&#}x27; i. e. one thing is called a cause on the ground of its relation to another.

and the events of one moment taken in the lump must be the causes of those at the next.1 But which is the cause of which the single experience of their succession will not determine. A man may run for an hour mund his garden on a frosty night, and when he wakes up next morning may notice that his less are stiff and the dahling in his parden blackened. If he had really no other experience of such events than in this succession, he might equally well conclude that the frost had made him stiff and his running blackened the dahlies, as vice versa. But it is involved in the causal relation that if two things are really cause and effect, the one never occurs without the other; and hence by comparison of that experience with others he might conclude that running round the garden did not blacken dahlias, because at another time they had not gone black after he had been running round it; and that frosty nights did not make his legs stiff in the morning, because he had waked up after another frosty night without any stiffness in them. So far he would only have disproved the connexions to which his mind at first had jumped. To prove that frost does blacken dahlies and that it was the running that made his less stiff is a more difficult matter; for the mere fact that one has been followed by the other many times constitutes no proof. Yet. the repetition of the same event under different circumstances is constantly parrowing the field of possibilities; for no two events can be precisely cause and effect, of which one in any case occurs without the other; so that if we can show that out of all the circumstances under which the blackening of dahlias has been observed to occur, a frost is the only one that has not also on another occasion either occurred without such an effect befalling the dahliss or failed to occur when it has befallen them, we may conclude that there is nothing except the frost to which their blackening can be attributed.

It may be said that an event of to-day may be due partly to some event that occurred a long time ago; for example, a man may inherit a fortune on his tweaty-first hirthday in virtue of a will made before he was born. We shall see later that it is by no means always practically convenient to call the immediately preceding conditions the cause: and the remoter cause may without offence usury the name. But the legisless becomes possessed of his fortune because he has just attained the age of twenty-one to-day; and the will may be regarded as having initiated a persistent legal position as regards the money; so that the statement in the text may be deemed sufficiently accurate in the context which it is intended to ducidate.

In this example we find the simple principle upon which the reasoning of induction rests: though the successful prosecution of inductive science requires very much besides such reasoning. The ceuse of any phenomenon !__in the strictest sense of that relation__ is so related to it, as to come whenever the phenomenon occurs. and never when it does not and to vary or he constant as the phenomenon varies or is constant, when enscentible of variations in quantity or degree. From this it does not follow that because in a limited number of instances some two particular phenomena a and a have been observed to be present and absent, to vary and be constant together, they are related as cause and effect: since there may be another phenomenon a which also satisfies the conditions, and it is impossible so far to tell whether a or b or the combination of them is the cause of a. But it does follow that nothing is the cause of a which fails to satisfy the conditions: and it is upon that consideration that all discovery of causes from experience rests. In saying this we do indeed but repeat what was said in reference to the 'New Induction' of Bacon.

Thus inductive reasoning rests upon the definition of Cause; for unless we know what causal relation is, we cannot know that certain phenomena do not stand to each other in that relation. And from the definition of Cause, or rules whereby to judge whether two phenomena are thus related to each other or not: just as from the definition of Property proceeded what Aristotle called Topics of Property, or rules whereby to judge whether a given predicate was or was not a proprise of a given subject. But you can only prove that they are use related as cause and effect by proving that there is nothing else with which either of them can be causally connected.

J. S. Mill formulated four 'Methods of Experimental Enquiry'.

I use the word phanomenon on account of its generality: an event, like the fall of a thunderboth, may be called a [natural] phanomenon: or fall or each account of the called a phanomenon: or fall or even a lose, like gravitation. The word certainly does not mean in its current usage, as in revertheless sometimes stated, anything that can be practived by the sames; it seems to be used to cover any particular thing, property, principle, or event which can be made matter of scientific investigation or med in replacing with a data the same of the control of t

or as he also called them, 'Inductive (or 'Experimental') Methods,' to which he attached considerable importance in his System of Logic. He called them the Method of Agreement, the Method of Difference, the Method of Residues, and the Method of Concomitant Variations. Among other defects of his expecition, there is one that darkens in a special degree the subject of induction.

We shall be able to appreciate the nature of this defect if we realize that the essence of inductive reasoning lies in the use of your facts to disprove erroneous theories of cansal connexion. It is, as Mill himself asserts, a process of climination.2 The facts will never show directly that a is the cause of a: you can only draw that conclusion, if they show that nothing clee is. In order to show that nothing else is, it is of course in the first place necessary that you should know what other circumstances there are among which the cause might be sought; you cannot 'single out from among the circumstances which precede or follow a phenomenon those with which it is really connected by an invariable law' (to horrow an excellent phrase of Mill's 3) unless you have secertained what circumstances do precede or follow it on divers occasions. But as to do that is no part of the inductive reasoning which we are now considering, we may for the present neglect it or assume it to have been done. The important thing to notice here is, that you do not discover what is the cause, except by eliminating the alternatives. Yet it is very often impossible to do this completely: nevertheless the nature of your reasoning is precisely the same, when you are left with the conclusion that the cause is either a or b or c. as if you had been able to eliminate b and a also, and so determine that the cause is a. Moreover, it makes no difference to the nature of your reasoning, as a process of advancing to the proof of the cause by the disproof of the alternatives, what the principle is to which you appeal in order to disprove them. You know that nothing is the cause of a which does not satisfy certain conditions-which is not present whenever x occurs and absent when it does not, which does not vary or remain constant as s does so. It is sufficient to be able to show that one of these conditions is not satisfied by a given circumstance p, in order to conclude that p is not the cause of x: and which condition it is does not matter in the least. It is unlikely that in any particular 1 Logic, III. viii. * e.g., ib. § 8 init. * Ib. § 1 init.

investigation every alternative hypothesis which we disprove as to the cause of the phenomenon that we are studying will be rejected because it fails to astify the same one of these conditions; the facts of our experience will probably show us one occurring where the phenomenon is absent, and the phenomenon occurring in the absence of another, a third unaffected in quantity or degree through all the variations of the phenomenon, and so on. All that seesential to the progress of our enquiry is that we should be able to show some fact inconsistent with supposing such and such an alternative to be the cause; then that alternative is eliminated, and the cause must lie among the rest.

The essence then of these inductive enquiries is the process of elimination. The reasoning is disjunctive. And the character of the reasoning is unaffected either by the completeness of the elimination (i.e. the fact that there are no alternatives left in the conclusion) or by the ground of elimination used. Yet Mill has so formulated his 'Methods' as to make it appear (a) that they are only used when the elimination is complete: (b) that they are different when the ground of elimination is different. From this it follows that very few inductive reasonings really conform to any of them; but the credit which this part of his work has obtained, and still more the currency given to the names of his 'Methods', in which his doctrine is enshrined, threaten us with a repetition of the same sort of mischief as arose from supposing that every argument could be put into the form of a syllogism. Just as arouments not syllogistic at all were forcibly tortured into the appearance of it, to the destruction of any proper understanding of what syllogism really is, and how it differs from other forms of reasoning, so inductive arguments are now often forced into a reseudo-conformity with the canon of one of these 'Methods', to the utter confusion of the mind. For in the process, we are made to allege that some circumstance is (say) the only one in which a number of instances of a particular phenomenon agree, in order to conclude in accordance with the canon of the 'Method of Agreement' that it is therefore the cause of the phenomenon. when we know perfectly well that it is not the only such circumstance: and as we know that it is not by such assumptions that we really conclude that circumstance to be the cause, we are only confused by a Logic which makes it appear that it is.

There are namenos in Mill's work (as is often the case with him) which implicitly correct his own error. In speaking of what he calls the 'Method of Agreement', he writes: 'The mode of discovering and proving laws of nature which we have now examined proceeds on the following axiom. Whatever circumstance can be excluded without prejudice to the phenomenon or can be absent notwithstanding its presence is not connected with it in the way of causation. The casual circumstances being thus eliminated, if only one remains, that one is the cause which we are in search of : if more than one, they either are, or contain amone them, the cause: and so mutatis mutandis of the effect.' It is plain from this that I am not the less reasoning in accordance with this method, because I am only able to say in the conclusion that the cause of the phenomenon is one or other of several alternatives. than if I were able to offer a definite solution. Yet this is quite ignored in what immediately follows: 'As this method proceeds by comparing different instances to ascertain in what they agree. I have termed it the Method of Agreement: and we may adopt as its regulating principle the following canon,' which Mill proceeds to enunciate thus :---

'If two or more instances of the phenomenon under investigation have only one circumstance in common, the circumstance in which alone all the instances agree is the cause (or effect) of the given phenomenon."

Every one who has tried known how difficult it is to find cases to which this canon can be applied: for it is seldom that your instances have only one circumstance in common. Where such instances are forthcoming, they are peculiarly instructive to the investigator; and therefore Bacon placed them first in his list of Prerogative Instances (i.e. instances to be consulted first), under the name of Instantiae Solitoriae.1 But what if your instances have several circumstances in common? Are they, therefore, useless to the investigator? Throughout the organic world it is observed that species present a number of adaptive structures—that is, structures fitting them for the conditions under which they have to live. To the question how this has come about several answers

Logic, III. viii. 1 ad fin.

Logic, 111. VIII. I ad fin.

'Now. Or, III. 22, where instances such as are required by Mill's Method of Agreement and by his Method of Difference are described under this name. And this is the proper way to treat them—not as instances the use of which constitutes a distinct method of inductive reasoning.

have been suggested: one, the oldest attributed them to special design on the part of the Creator: another to the inherited effects of use and disuse: another to the survival of those individuals who hannened to be born with a body more enited in any respect than their neighbours' to the conditions of their life combined with the elimination of the less fit. Now if it is pointed out that some adaptive structures like the horny back of a tortoise or the shell of a molluse cannot be improved by use as a muscle can one of these encreations is overthrown at least as a complete solution of the problem but it remains doubtful so far whether we are to refer the structures in question to design or to natural selection; yet we have certainly made some way in our enquiry, and this argument is part of our inductive reasoning. Mill's canon, however, is inapplicable to such a case as that, because the tortoise with his horny back, and the elephant with his powerful trunk for seizing branches though both possessing adaptive structures which may in both have been developed by natural selection, are not instances with only one circumstance in common. It is excellent advice to see in what the instances of your phenomenon agree: but the ground of the advice is that you may eliminate the circumstances in which they differ: and the principle at the foundation of the 'Method of Agreement' is not that 'the sole invariable antecedent of a phenomenon is probably its cause '.1 for the ' Method ' is often employed when there is no sole invariable antecedent: it is that nothing is the cause of the phenomenon in the absence of which it occurs. Again, so obvious is the difficulty of finding such instances as

the application of this 'First Canon' requires, or such as the second, that of the 'Method of Difference', requires, or such as the second, that of the 'Method of Difference', requires, that Milh, aving begun by mentioning four methods (of Agreement, of Difference, of Residues, and of Concomitant Variations), adds a fifth, which he calls the Joint Method of Difference', you are to find an instance in which the phenomenon under investigation occurs, and another in which it does not, agreeing in every circumstance except one, which last circumstance is to occur only in the former; and that will be the cause (or effect) or an indispensable part of the cause of the phenomenon. Such instances as these may also not be forthcoming; and therefore, under the name of the Joint Method, Mil describes the 'Jerons, Elementary Lessons. By 241 (1880).

case in which you look for a circumstance about which it can be said that it is the only one that is neither absent in any instance where the phenomenon occurs, nor present in any where it does not. Here then both grounds of elimination are employed; but there is no reason in the world, as a study of his account of his Methods would show, why he should not have had another Joint Method, of Difference and Concomitant Variations, or of Agreement and Residues, and so forth. An enquiry into the cause of one phenomenon mad not confine itself throughout to one ground of elimination.

For the above reasons it would be well to recognize that Mill has not formulated four (or five) but one ' Method of Experimental Enquiry '-as indeed Bacon might have shown him : of which the essence is that you establish a particular hypothesis about the cause of a phenomenon, by showing that, consistently with the nature of the relation of cause and effect, the facts do not permit you to regard it as the effect of anything else (and mutatis mutandis if you are enquiring into the effect of anything). It is this which makes the reasoning merely inductive. If you could show in accordance with known or accented scientific principles that the alleged cause was of a nature to produce the effect ascribed to it. your reasoning would be deductive: leaving saids the question how those scientific principles were ascertained, you would be applying them to produce a conclusion which you see to be involved in their truth . and if we suppose the principles to be of such a nature that we can see they must be true then the conclusion will annear necessary, and a thing that could not conceivably be otherwise.

Milly canon for the 'Joint Method' is by no means carefully worded (Logic, III. viil. A). It would be better if for 'the circumstance in which alone the two sets of instances differ 'we read 'the circumstance in which alone the second set of instances grees to differ from the first set.' Note that Mill represents it as necessary, under the terms of the Joint Method, to show of every other circumstance than that which is alleged us cause in the conclusion both that it is absent in some instances where the phenomenon cours and that it is present in some instances where the phenomenon cours and that it is present in some instances where it does not. This is because he develops it as an answer to the objection, that although a circumstance had not been called Plantility of Causes will be considered later. The point in the tact ther is, that it is quite possible, and very common, to above that one circumstance is not the cause on one ground—say that it is occurs without the phenomenon, and a third on a third ground—say that it is occurs without the phenomenon, and a third on a third ground—say that it is occurs wrinted the phenomenon is constant, all in the same investigation.

Take for example, the maxim that men hate those who have conferred a benefit on them. 1 We may repard that as, in the first place, an induction formed from the consideration of many instances of ill will, which are unaccountable otherwise than on that principle: vet so far it remains a thing obscure and unintelligible, a relation which the facts forbid us to dispute, but in which we see no necessity. Now if a man were to say that men hate to feel themselves in a position of inferiority, and that they do feel themselves in a position of inferiority to those from whom they have received a henefit. the maxim follows deductively and these principles are not only like the original maxim, capable of being inductively supported by an appeal to experience, but they are also intelligible to us in a way in which that was not: it is mercifully untrue to say that they appear necessary, but they do appear more or less natural. Where, however, we have to rely purely on induction, there is none of this 'naturalness'. I stand on my conclusion because 'I can no other'. and not because I see any intrinsic necessity for it. Necessity there is if I am right about my facts, and am to reason in this case consistently with what I know to be involved in the causal relation : but that necessity is not intrinsic; had the facts been otherwise. and for all I can see they might have been. I should have concluded otherwise: and then I should have been just as content to accept that as I now am to accept this conclusion.

There is an enormous number of general propositions, which we accept for no better reason than that the facts are inconsistent with our despring them, and not because in themselves they have anything which could have led us to suppose them true, antecedently to our experience. When it is said that we ought always to follow experience, it is meant that we ought not to trust our notions of what seems antecedently fit to be true, or mere guesses as to the connexions that rubsist in nature, but accept only thore connexions which our experience forces us to accept because it is inconsistent with any alternative. Such reasoning is called a posterior, because it starts from the facts, which are conceived as logically dependent on, or posterior to, their principles, and thence infers the principles on which they are dependent. Conversely, deductive reasoning is

Of course this, like most maxims with regard to human nature, is not an universal trath: sehal kind of men hate those who have conferred a benefit on them would be the next subject for enquiry.

often called a priori, because it starts from the principles or conditions. which are conceived as logically prior to the consequences that follow from them. When a priori reasoning is condemned it is not meant that we are never to resson deductively, but only that we are not to reason from principles that are not warranted by: experience: at any rate this is the only sense in which the condemnation can be justified. But it is an error to suppose that all general principles are arrived at a posteriori, or by process merely of showing that facts are not consistent with any other: the Law of the Uniformity of Nature itself, as we have seen, is not arrived at in that way since if we once doubt it, it is impossible to show that the facts are any more inconsistent with its falsity than with its truth : neither are mathematical principles so arrived at : we do not believe that three times three is nine, because we show successively that it is not five or ten or any other number except nine. Still it is true that in the inductive sciences the vast majority of our generalizations are reached either in this a posteriori manner, or by the help of deduction from other generalizations so reached. And it may be well to show by one or two examples how generalizations that rest merely on induction present as it were a blank wall to our intelligence, as comething at which we cannot help arriving, but which we can in no way see through or make intrinsically plausible. Facts show that the excision of the thyroid gland dulls the intelligence : could any one see that this must be so? Explanation may show that on a contribution which the gland, when properly functioning, makes to the circulating blood depends the health of the brain; but that comes later than the discovery of the effects of excision: and even so, can we understand the connexion, which facts establish, between the state of the mind and the health of the brain? Or take a thing more frequent and familiar. It sounds perhaps the most natural thing in the world, that we should see with our eyes, hear with our ears, taste with our palate, and so forth. Yet for all that we can see a priori, it might just as well have been the case that we should see with our ears and hear with our eyes, smell with our palate and taste with our

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Or, in another sense, illustrated in most mathematical reasoning because the premisees, without being more general than the conclusion, or giving the cause why it is true, are not based upon an appeal to facts which might conceivably have been otherwise: cf. p. 505, n. 2; infru.

fingers. Doubtless if we tested with our fingers, we should not have to eat in order to taste there might be some advantages in that and at any rate it is not antecedently inconceivable. It may he said that the mechanism of the eye by which light is forused from many points at once upon the extended surface of the retina and the eye is readily turned in any direction, makes it a priori a more suitable organ of sight than the ear could be; and it is true that upon the assumptions that light-sensations are produced by the stimulation of a nerve, that this stimulation is supplied by wave-motions in the ether, that distinguishable colours are produced by differences in the wave-length, and that the arrangement of these colours in the visual field corresponds to that of the nerve-fibres appropriately stimulated in the retina, we can find in the eve an excellent arrangement for securing clear vision. There is nothing, however, in those assumptions (which have only been proved inductively) that is any more intelligible to us than if the wave-motions of the ether stimulated the fibres of the ear: though doubtless our vision would be less serviceable in the latter case. There is in fact no nevcho-physical correspondence that is at present intelligible to us. although particular correspondences may be intelligible in the sense of conforming to more general principles which we have found to prevail. The same may be said with regard to the properties of chemical compounds which are not for the most part intelligible from a consideration of the properties of their elements; hence in saving that they depend upon the composition of the substance we rely merely upon this, that no other view consists with the facts which we have observed in our experiments. The largeness of these two classes of inductive generalizations may perhaps make it unnecessary to illustrate further what Bacon would call the 'surd and positive 1' character of conclusions resting only on induction : but, as showing how the mind desiderates something better, we may notice the attempt continuously made to conceive chemical as at bottom only physical processes. In the physical process, the successive stages do to some extent at least appear to follow necessarily one out of another; on their mathematical side, the principles that connect them are not mere matter of fact, but matter of necessity which we cannot conceive otherwise. Hence the attraction of

¹ De Principile atone Originibus, Ellis and Spedding's ed., III. p. 80.

reducing chemical processes to physical terms. It is true that the appearance of new sensible properties in hodies in virtue of their physico-chemical composition is not hereby explained hut it is supposed that they only possess these for us that the appearance is subjective, or in other words that while the processes in bodies themselves are nursly physical, see are determined to receive qualitatively different sensations by different physical stimuli. There is not much prospect at present of rendering psycho-physical correspondences really intelligible: thus there is a temptation to regard the emergence in a chemical compound of properties which cannot be seen to have any necessary connexion with the properties of its elements as only subjective, a fresh case of that psychophysical correspondence which we admit that we can only ascertain and not understand: in order that we may if possible find in the principles of chemistry itself something intelligible, and not merely necessary to be admitted. The gain is more apparent than real: but the procedure betrays a sense that though it may lead us far and win us much, induction turns out at last to be the blind alley of the resear

We must return, however, from those general considerations upon the nature of induction to the particular inductive reasoning which rest upon our knowledge of the requirements of the causal relation. By and by we shall find that reasoning which is really inductive enters into processes of a more complex and partially deductive kind. What we are at present considering is in principle quite simple. The cause of a phenomenon 1 is to be sought among those circumstances under which it occurs in the instances that we take. The causal circumstances are indicated by a process of exhaustive climination. Those which are not causal can be eliminated because the facts show that in regard to this phenomenon they do not satisfy the conditions of a cause. Now the grounds on which we may eliminate are these; and each points to some particular requirement of the causal relation, failure to satisfy which disproves that relation as between two given phenomena:

 Nothing is the cause of a phenomenon in the absence of which it nevertheless occurs.

Or mutatis mutandis the effect. I shall not complicate the exposition by always adding this.

- Nothing is the cause of a phenomenon in the presence of which
 it nevertheless fails to occur.
- Nothing is the cause of a phenomenon which varies when it is constant, or is constant when it varies, or varies in no proportionate manner with it.
- To these may be added a fourth ground .
- Nothing is the cause of one phenomenon which is known to be the cause of a different phenomenon.

This last principle is also, like the others, involved in the general conception of a reciprocal causal relation; but in applying it we appeal not merely to what we observe in the instances of the phenomenon under investigation, or in the instances where under more or less similar circumstances the phenomenon does not occur; we appeal also to previous generalizations regarding the connexion of phenomena. These generalizations regarding the connexion of phenomena. These generalizations, however, are used not to account for the connexion which we are now establishing—it is not deduced from them; but merely to exclude alternative explanations of the present phenomenon, and so force us upon the one which we finally accept; and so far the reasoning which appeals to under a ground of elimination is still inductive. But it belongs especially

On these grounds of elimination Mill's 'Inductive Methods asversally repose. The irru is the foundation of his 'Method of Agreement', the second of his 'Method of Difference,' the first and second jointly of his second of his 'Method of Difference,' the first and second jointly of his second of his 'Method of Difference,' the first has a which of the control of the production of the phenomenon in the control above in a way which only holds if in the cases we include everything necessary and nothing superflows to the production of the phenomenon in question. The illustrations in the present chapter are not confined to that, the strictest, sense of sause; but he important point involved will be considered later in Chapter xiii, on reciprocating cases, other principles call to be applied: e.g. we may any that 'where the removal of one of a number of conditions is found to involve the cossistion of a phenomenon, though the other conditions may remain, in the absence of those other conditions; it may be called the cause of the becamenon: Cases there is clearly only a size question, but for various phenomenon. Cases there is clearly only a sixe question, but for various with the saccration. Lothe, in Bl. III. c. vii. of his Legic, headed Universal Inductions from Purreylien, has paid some attention in § 261 to the formulation of principles of this kind, stating what degree of connexion between two elements C and Z can be inferred from what kind of observious with regard to the circumstances of their occurrence. The section is eminently principle in question might all be called Topics of Lank though some of them are doubtful; just as Aristotte recognised Topics which hold true in

to the later stages of a science, because it presupposes the discovery of other causal connexions, as a means of prosecuting some present enaniry.

It is plain that we cannot get to work in the application of these principles, until we have clearly conceived the phenomenon we are studying, and sacertained and distinguished the circumstances under which it occurs (or fails to occur) from one another. And if all this were done, their application would be an easy matter, as Bacon imagined he could make it. All symbolic representation of such inductive arguments by letters of the alphabet, where one letter stands for the phenomenon investigated, and others for the circumstances among which its cause is sought, presume these tasks to have been achieved; and thus they are apt to convey a totally false impression of the decree of difficulty attaching to inductive enoniries 1. The truth is that inductive reasoning is in form very

Treatise, Of the Understanding (already, like this chapter in Lotar, referred to), gives a number of Rules by which to judge of Causes and Effects which are derivative, but highly important, as for example that "where several different objects produce this same effect, it must be by means of some quality, which be really the ultimate principles, if a reciprocating cause is meant.

On the artificial simplification which letters of the alphabet tale imply, of Venn's Empirical Logic, or will, pp. 408, 407. If they are to be used at all, to which I see no objections to long at their limitations are understood, all, it is a superior of the superior of superior of the superior of superior of the superior of superior of superior of the superior of superior of superior of the superior of superior of superior of superior of superior of the superior of always an equal number of big and small retters; but when we are looking for the cases of some phenomenon, and each it among a number of alterna-tive the case of the case of this phenomenon is sought. Only alternatives among which the cases of this phenomenon is sought. Only in symbolizing him 'Method of Rendues' is this feature appropriate; there certain circumstances collectively are supposed to be known to be the cases of a sumber of effects (or of an effect of a certain quantity or degree), and out of these we reject, as not the cause of one among the effects, those which we know to produce the others (or if the question is one of quantity or degree, we reject those whose total effect we know to differ from what we have to account for, as not accounting for the remaining component). Hence separate symbols for the effects (or components of the effect) of the Hence separate symbols for the effects (or components of the effect) of the minons circumstances among which the cause of one effect (or component) is rought, as well as expante symbols for the causes, are required. The followed by or a, & & .). Now, as Mr. F. H. Braidley points cut (Principles of Loyic, p. 839, note *), the letters are intended to symbolise the phenomena separated to the before we apply our inductive canons; and therefore they ought not to imply, as by this correspondence they do, that the phanomena themselves, as datined from the fact of their joint or separate occurrence,

simple; but the discovery of the proper premises is very hard. As Hume well observes of the rules he gives 'by which to judge of causes and effects ', 'All the rules of this nature are very easy in their invention, but extremely difficult in their application.' I the sary enough to see that if out of so many alternatives $a b \in d \dots s$, the cause of a is not $b \circ d \dots o s$, it must be a; and it is easy enough to see that if c occurs without s, it is not its cause. But to show that c occurs without s, and to show some reason for rejecting $b \circ d \dots s$, saw well, and to discover $b \circ d \dots s$, and allow that no other alternatives are possible—all these things are extremely difficult. Something will be said of these operations in the next chapter. Here we are concerned with the form of the reasoning, which is of a disjunctive kind, and may be symbolized thus:—

The cause of z is either a or b or c or d ... or z

It is not hor cord or c

· It is a

In this argument the minor premise is proved piecemeal by hypothetical arguments that rest upon one or other of the above grounds of elimination, or 'rules by which to judge of causes and affects'.

If δ were the cause of x, it would be present whenever x is present

But (in this instance) it is not.

If c were the cause of c, it would be absent whenever s is absent.

But (in that instance) it is not :

and so forth. Or if any one prefers it, he may represent this part of the argument as a syllogism:

Nothing is the cause of x, in the absence of which x occurs b is a thing in the absence of which x occurs

Nothing is the cause of z. which varies without relation to it

Nothing is the cause of s, which varies without relation to it d varies without relation to s.

It is of course possible that bcd...z may all be eliminated, or shown not to be the cause of x, by the application of the same principle or major premise; in this case the minor of the above disjunctive argument might be proved m bloc, and not piecemeal;

have anything about them that proclaims which is the cause of which. Cf. also Professor Bosanquet's Logic, II. iv. vol. ii. p. 128.

1 Treaties, Of the Understanding, loc. cit.

but this is by no means necessary, and in fact unusual, and does not affect the nature of the argument. It is, however, the only case contemplated in Mill's formulation of inductive reasoning. It is also possible (and this Mill's formulation does not recognize at all) that we may not be able to prove the whole of the above minor premise: and then our argument will take the form

The cause of a is either a or b or c or d ... or z

- It is not c or d ... or z
- . It is a or b
- It is not d or z
 - ... It is a or b or c ...

where the degree of uncertainty symbolized as remaining at the end of our enquiry is greater.

It appears plainly enough in this analysis how all induction rests on the Uniformity of Nature: for in proving the minor of the disjunctive argument a principle is always appealed to, that would fall to the ground if the Uniformity of Nature were denied. It is not indeed necessary in a particular investigation to assume this uniformity to extend beyond the department of facts with which we are dealing: if I am looking for the cause of cancer, it is enough that cancer should be subject to uniform conditions in its occurrence; and I should not be impeded in my research by the fact, that thunderstorms occurred quite capricionaly. There is, however, no ground for assuming cancer to be subject to uniform conditions in its occurrence which does not apply equally to thunderstorms, or to anything else that could be mentioned: if I assume the principle of Uniformity at all. I must logically assume it altogether; and so, though I may be said to appeal to it in any particular inductive argument only so far as concerns the department of nature to which my investigation belongs, I really assume it universally.1 Nevertheless it is not correct to say that it is the ultimate major premise of all inductions : for that implies that an inductive argument is, formally considered, a syllorism, and we have seen that it is not. It is indeed impossible to see how this principle can be made the major premiss of any inductive argument as a whole, though its particular applications

¹ Cf. what Aristotle says of the assumption of the Law of Contradiction implied in all syllogisms, An. Post. a. zi. 77° 22-24.
Mill, Lopic, III. iii. 5 1 med.

may afford the major premise of an argument by which we prove any part of the minor in our disjunctive argument. Let us may that 'Nature is uniform', or (since we can hardly make a middle term of 'Nature', which in the sense of nature as a whole is not predicable of any particular subject) that 'All events in nature take place in accordance with uniform laws': we may then proceed to arous that ' Cancer is an event in nature', and therefore that it takes place in accordance with uniform laws; but we are thus no further advanced than we were at the heginning, since so much is assumed in looking for a cause of it at all. Or if we put our major premies in the form 'Every relation of cause and effect that is observed in any instance between one phenomenon and another holds good universally, and then used as our minor 'The relation between a and a is a relation of cause and effect between one phenomenon and another observed in certain instances, we might indeed take the formal step of concluding that it holds good universally (though that is already implied in calling it a relation of cause and effect), but the whole question at issue is beyond in the minor premise: for what we want to prove is just that a is related to g as a cause, and not in time only and accidentally. For the formulation of the reasoning by which that is proved-which is the inductive reasoning-nothing therefore has been done. And any other attempt to reduce inductive reasoning to syllogism with the principle of the Uniformity of Nature as ultimate major premise will be found equally unsuccessful.

It remains to illustrate by a few examples the truth of the contention that inductive conclusions are established disjunctively by the disproof of alternatives.

1. The power of the chameleon to change colour in accordance with the colour of its surroundings is well known. But this power is not confined to the chameleon; it occurs, for example, also in certain frogs. The question raised is as to the cause of this coange. We have first indeed to show that the change is due in some way to the colour of the surroundings; that implies a previous inductive argument; for so long as it was only noticed that the frog change colour from time to time, it would be quite uncertain with what that change was connected. Of the suggestions of the control of the control of the suggestions.

¹ This example is taken from Dr. Vernon's Variation in Animals and Plants (Internat. Scient. Series), pp. 255 seq.

that might occur to a biologist (for we may disregard such as might occur to a collector of portenta: Livy gravely records as portents of disaster some facts quite on a par with the statement that 'a froe changed its colour in broad daylight ', but it would be easy to show that the phenomenon had occurred at a time of no disester)-of the suggestions then that might occur to a biologist we may conceive the nature of the animal's food to be one; time of day or season of year to be another: intensity of sunlight to be a third. and so on that when it was shown that the from might variously change its diet and he of the same colour and that the change of colour might take place at any time of the day or year, and in various degrees of sunlight, these suggestions would be discarded. and so on until the only reasonable suggestion left was that which connected the change of colour with the colour of the surroundings Of course this conclusion would acquire great strength so soon as any one noticed the frog in the process of changing colour upon removal from one ground to another; for thus the alternatives would be confined to those matters in which a change of conditions had been just then effected. The preliminary induction implied in saving that it changes colour according to the colour of the ground on which it rests need not, however, he further considered : we wish to know more precisely what produces the change. Now differently coloured grounds may vary in temperature as well as in colour: but it can be shown experimentally that the colour-reaction is independent of temperature. Granting then, in the absence of any other alternative, that it depends on the colour as such, we may ask in what way the differently coloured rays 1 affect the animal. Lord Lister showed that they affected it through the eyes: for a specimen of Rana temporaria whose eves had been removed was no longer affected by any change in the colour of the surroundings in which it was placed: thus the alternative, otherwise not unreasonable, is excluded, that the reaction is somehow determined through the skin, the principle applied being that no circumstance in the presence of which the phenomenon fails to occur is its cause. This conclusion is further confirmed by the fact that in other species that normally exhibit a similar colour-reaction individuals have been found, in whom the power of adjustment to the colour

¹ To speak strictly, rays are not differently coloured, but of different wave-lengths.

of their surroundings is sheent, and that these individuals on examination have been accertained to be blind : but it may still be asked how the stimulation of the eve by different kinds of light effects the colour-change. Perhans there are two alternatives have it might be necessary for the frog to be aware of the colour of its surroundings, or there might be a reflex mechanism. The latter is supported by the fact that a blinded from after a violent struggle to escape, changed from dark to light, but in half an hour. though placed in a bright light, became almost coal-black again. Here it is shown that a colour-reaction can take place without awareness of colour: so that awareness of colour is eliminated from among the conditions necessary to the production of the reaction. on the principle that a circumstance in the absence of which the phenomenon nevertheless occurs is not its cause. We must look then for some circumstance common to the case of a blind from changing colour after a violent struggle, and of a normal frog changing colour with a change of surroundings; and we may find this in nervous excitation, for that may be produced by the action of light upon the eye, and also by the struggle. Until some other feature common to the two cases was successful, we should accent this on the principle just cited : but it is also supported by the known physiological function of the nervous system in the building up of reflexes: it consists too with the fact that when the excitement subsided the free returned to a colour not adapted to its environment. Yet how can the animal's colour be affected by different kinds of nerve-stimulation? There have been found in the skin of the frog pigment granules of divers colours, so arranged that different surface effects can be produced by different degrees of concentration in the granules. The final connexion of the phenomenon of colour-reaction in the frog with these pigment granules is indeed rather deductive than inductive; for the part which efferent currents from the nerves play in provoking muscular contractions and relaxations is already known, and so is the fact that an afferent nerve-current discharges into an efferent nerve : and we have just shown that the colons-reaction is connected with afferent nerve-stimulations.

2. Let us take next a simpler example, and one in which there is little or no generalization: for inductive reasoning may be applied to discover the cause of a single event, as well as of an event of a certain kind: and it is not necessary to carry the analysis (of which more in the next chapter) so far as to make a general conclusion possible. Let a novice notice that his bicycle makes an unpleasant noise in empring and try to assertain the cause. We are to suppose a novice because any one of any experience may be presumed already to have arrived by induction at the knowledge that one kind of noise is made in the chain, and another kind in the bearings and the application of this previously acquired knowledge to a particular case would be deductive. In this problem the determination of the alternatives among which the cause is to be sought is tolerably simple: for the noise must originate in one or other for it may be several) of the non-rigid parts. Say that these are, on the machine in question, the axle-bearings of either wheel and of the cranks, the hearings of the head the nedal-hearings the clutch the backpedalling break, and the saddle-springs. All that the rider has to do is to ascertain which of these parts may be at rest while the noise occurs, and which may be in motion without the noise. If the noise ceases in free-wheeling, it is not produced in the axlebearings of either wheel, for they are still running, and that is not the cause, in the presence of which the phenomenon fails to occur: for the same reason it is not in the bearings of the clutch, which is now running. If it is not produced in 'wobbling' the head, or turning sharp corners, he may acquit the bearings of the head on the same principle. If it occurs in driving with each nedal singly. it does not arise in either pedal-bearings, because it occurs with each nedal in turn undriven, and that is not the cause in the absence of which the phenomenon occurs. Similarly if it occurs without putting on the back-pedalling break, or when he removes his weight from the saddle, it does not originate in either of those quarters. Two alternatives remain: it may be in the crank axle-bearings, or in some looseness of the clutch when that is caught and driving. As between these alternatives a decision might be made if he dismounted, and listened while he whirled the hind wheel round by the pedals: here however he would be reasoning deductively from the principle that sounds are more distinct when you are nearer to their point of origin. The difficulty of generalising in such a case arises from the difficulty of distinguishing the phenomenon investigated from others that may be like it but have different causes. If the noise which each part of his bicycle could make were of a distinctive

kind easily recognized, a man might very soon determine that such and such a noise (at least in his bicycle) only originated in such and such a part : or if he could note the differences between noises otherwise similar coming from before or behind him from right or left. he might then (without having originally known although he distinguished their quality from which quarter each kind of noise came) establish inductively in the way described a oreneralization that such and such a noise was produced by something in the front axle-bearing, and such another by something in the left pedal: again, further experience, argued from on similar lines, might show him that a particular character in a noise was due to want of oil in a bearing and another character to a broken ball. But so long as the phenomenon studied is submitted to no such analysis, it is liable to be confused with others that are not really the same, and error would obviously arise if we generalized about it under these circumstances. Hence one may have to be content with a conclusion that assigns the cause of it in the particular case. It is however. instructive to observe that the same process of elimination among the members of a disjunction is employed here, as if one were establishing a general conclusion. For ex Appothes the novice recognizes in the noise no intrinsic character which he knows to be connected according to any principle with a particular origin : he has therefore to fall back upon ascertaining its origin by the indirect method of showing that among the possible origins to which it can be ascribed there is none but one to which the facts permit him to ascribe it consistently with the principles of causation.

8. Professor Weismann's theory of the 'Continuity of the Germ. Plasm' is well known. The reproductive cells, whether of a plant or animal, are different in certain important respects from those composing other parts and tissues, and called somatic or body-cells; and in particular of course, whereas the latter, in the process of increase and division, produce only cells of one kind, such as compose the part or tissue to which they belong, the former produce cells of every kind that occurs in the organism, and, in fact, are capable of reproducing the whole organism and not merely a special part of it. In so doing they must, of course, reproduce the reproductive cells also, in order to provide for the following generation. Now Weismann holds that the reproductive cell, or germ-plasm, as it develops, sets saids from the outset a part of itself to serve

the nurpose of reproduction once more, and that this which is still perm-plasm, remains as it were isolated in the developing organism. and unaffected by the other and heterogeneous parts, or somstoplasm. which the reproductive cell develops into and as this hannens in each generation, there is an absolute continuity of the germ-plasm: from which it follows in his view that no characters acquired by the individual in the course of its lifetime and not concenital can be transmitted to its offspring: for a character which is purely an acquired character arises in the somatoplesm, and the perm-plasm is from the first secluded from the possibility of being affected by the sometoplasm. Influences which reach the perm-plasm can alone modify subsequent generations; of which the most important is the fusion of two reproductive cells that takes place in sexual propagation (for the theory applies only to the metazoa. which increase by copulation); for the germ-plasm of the ovum blends with another germ-plasm conveying more or less different heritable tendencies, and a sort of shuffling takes place as a result of which there arises a new individual resembling precisely neither parent, but exhibiting those 'spontaneous variations', as Darwin called them, which form the material for Natural Selection to work upon. Darwin himself, on the other hand, believed that 'acquired characters' might in certain cases be inherited, and that it was very difficult to account entirely for the progressive modification of species in adaptation to their environment, without allowing the influence of this so-called 'Lamarckian' factor. 1 The question has formed a subject of protracted controversy among biologists, and it is not an easy one to settle conclusively on inductive principles by appeal to evidence, because most facts admit of being interpreted in either way. One of the most important investigations into the subject is a series of experiments on guines-nigs, conducted during thirty years by Brown-Sequard and extended by two or three other naturalists; and it is claimed that in the course of these experiments certain modifications appeared in some of the guinea-pigs, the cause of which lay in injuries done to the nervous system of their parents.

¹ Because Lamarck (1744-1829) had propounded a theory which ascribed ACCOUNT. ASSESSED ASSESSED AS PROPOUNDED & theory which ascribed the gradual modification of pecies largely to the inherited and accumulated effects of use and discuss of organs.

"The following argument is taken from G. J. Romanes' Dervoin and ofter Dervoin, vol. II. ch. iv.

It was found that enilency sometimes appeared in animals born of parents which had been rendered enilentic by an injury to the spinal cord or a section of the sciatic nerve. Here was a fact to be accounted for, and the cause must be sought among the circumstances to which the enileptic offenring were exposed. Brown-Sequent attributed it to the injury done to the parent : but nobody professes to see Acre that could produce the effect, so that one can only be forced to accept that explanation by default of anything else to which to attribute it. It might be said that the enilepsy was due to some concenital defect that had no relation to the experiment performed on the parents; but epilepsy is not otherwise known to occur apontaneously in guinea-pies, and apart from any improbability in the concidence, we should expect that if some concenital modification of the germ-plasm produced epilensy in these cases, it would have occurred and produced it in others. Weismann suggested that it was due not to the injury to the parent, but to 'some unknown microbe' which, entering at the incision whereby the injury was made, both produced the epileney in the parent, and by invading the ova or spermatozon. produced it also in the offspring. But against this suggestion we may urge that, though there may be microbes enough unknown to us, yet if this microbe of epilepsy in guines-pigs exist, it would he likely to seize other opportunities of entering: the disease. however as already mentioned is not otherwise known to attack them. And it was also found that the enilency might be produced (and annarently transmitted) without incision, by a blow on the head with a hammer in circumstances that preclude the entry of microbes. To this Weismann rejoined that the shock of the blow might have 'caused morphological and functional changes in the centre of the pons and medulla oblongata, identical with those produced by microbes in other cases', and so set up the epilepsy; but these changes would not penetrate, as microbes may be conceived to do, to the ove or spermatozos, and so the disease in the offspring occurs without the presence of the cause alleged. Moreover, there are cases (though the facts of them are not so clear or well confirmed) in which other diseases produced by other traumatic injuries to the parent have reappeared in the offspring; these diseases were not such as could have been produced by microbes; and to suppose, with Weismann, that the shock of the injury caused

a ceneral weakness of the nervous system, in consequence of which the animals would be likely to hear 'weak descendants and such as are readily affected by disease', does not account for the diseases in the offenring being of the same port as those respectively produced in the parents. So far therefore the alternative hypotheses to that which attributes the disease in the offenring to the injury done the parent seem to be excluded hut Weismann has a final aronment to uros against the 'Lamarckian' hypothesis. If the enilency was produced in the parent by the injury inflicted, it anght not to occur in the offening in the absence of that injury in the offenring and it would therefore he necessary to show that the nervous lesion which is the alleged cause of the epileney and not merely the epilepsy itself, is transmitted. To this Romanes renlies, that it very well may be transmitted; since even if adequate examination had been made (which is not the case), there may be structural injuries in a nerve which are not discernible. Nevertheless, he admits that the result of the whole debate is to leave 'the Lamarckian interpretation of Brown-Séquard's results' rather unassailed than proved. The facts alleged are 'highly peculiar' and hardly sufficient by themselves to furnish 'positive proof of the transmission of acquired characters'.

This example has been chosen because it illustrates very well how the inductive proof of a conclusion rests on excluding alternative explanations. The whole chapter in Romanes' work, from which it is taken, may be profitably studied from that point of view.¹ A further knowledge of facts might enable a biologist to suggest a cause for the appearance of epilepsy in the second (or later) generations of guine-pigs, consistent at once with the facts and with Weismann's theory of the continuity of the germ-plasm, But this does not detract from the value of the example as an illustration of the method of inductive reasoning; indeed, it must be remembered that such reasoning; if the premises are false, will probably involve us in false conclusions. But it must be pointed out, that in the process of excluding alternative suggestions as to the cause, it was sometimes necessary to do more than merely

¹ Cf. Romanes own words with reference to another experiment on guinespiece. "Naturally, therefore, the hypothesis of heredity seems less probable than that of mere coincidence on the one hand, or of transmitted microbe on the other. But I hope to have foirly excluded both face alternative explanations," Deroin and ofter Deroin, p. 119. (The italias are missessed in the probability of the

appeal to one of the grounds of elimination set down earlier in this chapter: some deduction of the consequences of accepting such alternative was needed, more elaborate than is involved in saving that if such were the cause the criteria would annear where it did not or not appear where it did. Thus it was around that the enilance was not to be attributed to a microbe because other discusses consily appeared to be transmitted, which a microbe could not have originated we cannot be said to be here applying the simple principle that that is not the cause of a phenomenon in the absence of which it occurs for these other diseases are not the same phenomenon as the enilency. To make the evidence of these other diseases serviceable it had to be shown that there was no tenable alternative to the Lamarckian interpretation put forward (in lies of microhes) in their case: and the principle involved in the use of their evidence was this, that if it is necessary to attribute the reannegrance of one kind of disease in offenring to its artificial production in the parents, it is more reasonable to attribute the reanneagence of another kind of disease (epilensy) in offenring to its artificial production in the parents than to a different sort of cause of whose presence and operation there is no evidence. This principle may in turn be said to rest upon the principle that like effects have causes correspondingly like; and all rests ultimately on our understanding of the causal relation; but in order to see that facts are inconsistent with the ascription of a given phenomenon to some particular cause, a more or less extensive hypothetical deduction of the consequences that ought to follow if that were the cause is often necessary. It may be noted, too, in this example, that some of the steps of the argument are only probable; if the entry of a microbe at the incision were the cause of the epilensy, it would probably occur in cases of natural injury where, so far as we can see, the microbe might equally well enter: according to the principle that that is not likely to be the cause of the phenomenon, which is probably present on some occasion when the phenomenon fails to occur.1 And lastly, Romanes cautionaly

In the Prior Analytics Aristotle discusses at great length modal syllogizms, i.e., yllogizms where one or both premises are problematic or apodeticis, showing under what conditions the conclusion will be problematic or apodeticis. We have here an example of what might be called a modal induction; the parallelism may be commended to the notice of any who think, with Mil, that an inductive argument which can be represented in symbols (like hir 'Inductive Methods') is the less formal because it is inductive,

concludes that the attribution of spilepsy in the offspring to its artificial production in the parent is not proved, because the cause may lie in something hitherto undetected; and this illustrates what was maintained earlier in the chapter, that the getting of a positive conclusion, but not the inductive character of the argument, depends on the completeness of the elimination.

4. Adam Smith, in the Wealth of Nations 1, discussing the inferences which can be drawn from the low money prices of goods in ancient times, and wishing to show that from the low prices of goods in general nothing can be inferred as to the wealth of a country, though much can be inferred from the comparative prices of different kinds of goods, such as corn and meat, mentions that it was commonly supposed that the said low money prices of goods in ancient times were a proof of the poverty and barbarism of the countries where they prevailed. He uses the following argument to show that this is not the case, but that they prove only the barrenness of the mines which then supplied the commercial world. First, he save that China is a richer country than any part of Europe, yet the value of the precious metals is higher there than anywhere in Europe: now on the principle that that is not the cause of a phenomenon which does not vary proportionately with it, we cannot attribute low money prices to poverty in the face of lower prices where poverty is less. Next, he admits that since the discovery of America the wealth of Europe had increased, and the value of gold and silver diminished; but he urges that the two events have scarcely any connexion; the first being due to the fall of the feudal system and the growth of public security, the second to the discovery of more fertile mines. In support of this way of connecting the facts he points to the case of Poland. Poland was the most beggarly country in Europe, as beggarly as before the discovery of America; yet the money price of corn (the most important single commodity) had risen equally there: if poverty were the cause of low money prices, it ought not to be found where prices were high. On the other hand, Poland was still feudal, so that her beggarly state was consistent with the connexion of facts alleged by Adam Smith. Again, Spain and Portugal were the next most beggarly countries in Europe to Poland, and prices ought therefore to be low there, if there were the connexion between low money prices and poverty that was supposed: but it was not the case: prices were high; as might be expected if they depend on the facility with which the precious metals are obtained for owing to their control of the American mines could and cilver were brought more cheenly to Spain and Portugal than to any other country in Europe. The cause of low money prices in general, therefore, is not poverty and barbarism. and may be the harrenness of the mines supplying the commercial world with gold and silver; and this has been shown by inductive resconing. Adam Smith also offers deductive arguments to show that it is the latter, and is not the former. It is not the former. because a moor could not afford to nav as much as a rich country, in labour and means of subsistence, for such comparative superfluities as cold and silver: it is the latter, because the purchasing power of gold and silver, or the amount of goods for which they will exchange, depends on what has to be given in order to get them : and where the mines are fertile, a less amount of labour and means of subsistence needs to be supplied in the work of getting them, then where they are more barren. The logician may distinguish an inductive from a deductive argument; but investigators will gladly use arguments of both kinds to support the same conclusion

5. We may conclude with an example drawn from the Poor Law Commissioners' Report of 1834, with regard to the cause of the appalling increase of pauperism in England during the early part of the last century 1. The Commissioners who were appointed to find the cause and to suggest a remedy, attributed the evil to one principal fact in the situation, viz. that the condition of those receiving parochial relief had been allowed to become not less eligible than the lowest condition of men maintaining themselves by independent labour. In proof of this finding, they pointed out in the first place that the cause alleged was present in all instances of the phenomenon to be accounted for. The great increase of nauperism had dated from 1796. In that year, an Act of 1723. providing that no one should be entitled to relief who would not enter the workhouse, had been repealed; and it had become customary for the parish to assure to all labourers, in their own homes, a certain weekly sum, varying with the numbers in the 1 e. the Blue-book, esp. pp. 186-216.

family and the price of bread. This sum was made up in various ways; sometimes grants were given in supplementation of wages (which naturally tended to make farmers and other employers give a lesser wage, and so interested them in the support of a system from which they saw more clearly the immediately resulting benefit than the remoter but far greater evils); sometimes the parish found work, generally lighter than what was exacted for the same price by private employers (and this led men to prefer to work for the parish); sometimes a money-grant without any return of labour was made to men out of work (who were not, therefore, the more likely to look for work); but in any case, it was made possible for a man to count upon parish pay, efficient to maintain him as well as many independent labourers were maintained, whether or not he endeavoured to support himself.

The cause alleged, then, was present where the pauperism was present. but that was not enough to show that it was the cause It might indeed be plausibly argued, from familiar principles of human nature that such a method of administering mor-relief would be likely to increase pauperism faster than it relieved it: but this deductive reasoning was not and still is not sufficiently convincing to men who from one motive or another, are attached to such methods—whether from compassion for the immediate suffering of those applying for relief, or from desire to get relief on the easiest terms, or from fear, if relief is less readily given. that it will become necessary to give higher wages to the labourer. To bring conviction, it was necessary to show that there was nothing else to account for the phenomenon. Now several other causes had been suggested to account for this growth of pauperism. One was the great rise in the price of corn, which had occurred during, and partly in consequence of, the French war: another was the increase of population; and another was the introduction of machinery-a highly unpopular thing at the time, because its first and most obvious effect was to displace labour; and there had been agricultural riots directed against the use of machinery in 1880.

It would not be possible to show that none of these causes had ever made a man a pauper. But it was possible to show that in the main the pauperism so widely prevailing (which was so great a national eril because it prevailed so widely) could not be due to them. The Commissioners were able to point to numerous instances of three kinds, in which the pasperirm so prevalence cleswhere was absent; in all of them, the cause they alleged was absent too; but the alternatives which they wished to disprove were nevent.

The first class of instances consisted of certain parishes where what was called a Select Vestry had adopted the plan (till then lawful, though not since 1796 compulsory) of refusing relief to any able-bodied labourer except in a workhouse where a full task of work was exacted. It was their experience that pauperism immediately and greatly diminished. And naturally; for when men who had hitherto been content to take parish pay found they had to work as hard all the same, they preferred to work for themselves; with a motive for independent industry and thrift, they became more industrious and thrifty; becoming more industrious, they were better worth employing; and the farmer besides, knowing that the parish would no longer supplement the inadequate wages by which be had obtained labourers upon his farm, was compelled, if he would still have labourers, to give a better ware.

The second class of instances was furnished not by parishes which, in removing the cause alleged, had removed the pauperism which it was alleged to be the cause of : but in the parishes themselves where the pauperism existed. It was furnished by what are called the non-settled labourers, who in all parishes were found to be more industrious, thrifty, and prosperous, and less pauperized. than the settled labourers. As the circumstances of two sets of labourers in one parish are likely to be more nearly alike than those of labourers in distinct parishes, these constituted what Bacon calls a prerogative instance; for all the conditions equally affecting settled and non-settled labourers may be excluded, in looking for the cause of this difference between them, on the principle of rejecting the circumstances present when the phenomenon is absent. By a non-settled labourer is meant a labourer living in another parish than that which is legally bound to support him. If he becomes a nauper, such a person can be removed to the parish to which he is legally chargeable; and to save their own rates, overseers were always anxious to remove any one they could. To the labourer, on the other hand, removal was as a rule by no means welcome: such labourers, therefore, found that they had to choose

between removal, which they did not want, and an effort to maintain themselves by their own labour; for if the parish relieved them at all, they would only get—unlike their settled neighbours —little relief on hard terms where they were.

The third class of instances was afforded by parishes which had never adopted the practice, so common since the Act of 1796, of relieving able-bodied men out of the workhouse; i. e. they had never consented to make the condition of the pauper as eligible as that of independent labourers; and in them the same extensive pauperization and increase in the rates, which had occurred elsewhere had never hanoand.

Now in all these three classes of case, the Commissioners' theory held good: for when the effect was absent, so was the cause to which they attributed it. But the same could not be said for the alternative theories put forward. If it were alleged that nonsattled labourers had smaller families which is doubtful wat the increase of population was not confined to parishes which had adopted, or banished from those which had abandoned, the practice rendered permissive by the Act of 1796. The price of corn had risen, and the introduction of machinery must have had its effects -whatever they were in the parishes which had abandoned or never adopted that practice as much as in the rest, and among the non-settled as much as among the settled labourers of any parish. In short, looking to the mass of pauperism, there was no other circumstance which might be suggested as its cause, that could not, upon one or other of the plain grounds of elimination so often referred to, he rejected; and the Commissioners' cause was left in possession of the field: with the additional support derived from the deductive reasoning that might not have been thought ofeven if it would have carried conviction-by itself. For it often happens that we can subsequently show that a cause, to which an effect has been attributed on the grounds that there is nothing else to which the facts permit us to ascribe it, must, in according with some accepted principles prevailing in the subject-matter to which the enquiry belongs 1, produce that effect; although, but for the help which the inductive argument had given us in finding the cause, the deductive argument would never have occurred to us.

i.e. special principles, or ideas doyal. Cf. supra, p. 359.

CHAPTER YYI

OF OPERATIONS PRELIMINARY TO THE APPLICA-TION OF THE FOREGOING RULES

Ir was allowed in the last chapter that it is impossible to apply the kind of reasoning there analysed until a good dead of work has already been performed upon the material which experience offers us. That work is really much harder than the reasoning that succeeds it; indeed so simple does the reasoning look when thrown into symbolic form, that it would not be surprising if any one mistrusted the foregoing account on the mere ground that induction must be a harder business. A consideration of the present chanter may reasure him on this point.

The operations that have to be performed in order that the foregoing rules, or any other more special rules of the same kind, may be applied, are difficult to classify in a perfectly estisfactory manner. Different writers have called attention, and have given different names, to processes which are sometimes more or less the same essentially. Moreover, we should make our list shorter or longer according to the extent to which we considered what may be called the Methodology of the several sciences. By this is meant an attempt to give special directions, based partly on general logical considerations and partly on the nature of the facts with which it deals, for mastering the special difficulties which a particular science presents; for example, a mythologist might be enjoined to adopt the comparative method, and collect, with all the precautions which the experience of those who know the difficulty of rightly interpreting the savage mind can suggest,

¹ Mill deals with the subject of this chapter for the nost part in his Fourth Book, Of Operations subsidiary to Induction. In the sense that the reasoning described in the Third Book cannot be profitably performed till they have taken place, they may be called subsidiary; but Induction is parkapa rather taken place, they may be called subsidiary; but Induction is parkapa rather than the profit of the

the muthe and material of many different lands in hislogy again we should probably be told of the importance of obtaining statistics of a terestworthy kind regarding the mode in which divergences were distributed on either side of the average or normal in respect of divers measurable characters in animals and plants: and so forth. The particular preliminaries without which inductive reasoning in each science may have little prospect of success could of course only be determined by some one well acquainted with that ecience: though it is quite possible that a man of logical training, coming fresh to the study of what others have done, may he the better able for that training to make contributions to the work of scientific investigation : still, here as elsewhere. Logic learns by reflection on the immediate operations of thought about things. A methodology of the several sciences lies bowever beyond the scope of this volume, and would require far greater knowledge than it has at its command. The list of operations therefore which follows makes no pretence to go as far as it might, or to embody the only possible division.

First of all may be placed what has been called the Analysis of the Given 1: and this is requisite in two ways,

- 1. in determining precisely the phenomenon to be studied;
- 2. in distinguishing and detecting the various circumstances under which it occurs, or under which it fails to occur when perhaps it might have been expected.

Long before we consciously seek 'rerum cognoscere causas', a beginning has been made in the performance of this analysis and the results are embodied in the general names by which men group and distinguish different objects, attributes, or events. But there are many distinctions which ordinary language ignores, and it often gives different names to things which are in some important respect identical. For ordinary purposes the identity may be of no secount, and yet in a scientific enquiry it may prove fundamental. For example, to the lawyer hares and rabbits are vermin, to the sportaman they are game, and to the zoologist they are rodents; each of these men for his own purposes is interested in characters that unite them respectively with quite a different group of other animals; but there is nothing in their specific

¹ Professor Welton's Inductive Logic, c. v.

names to indicate their affinities with any one of these groups. Or again breathing, burning, and rusting are three processes for all practical murnoses so very different, occurring in such different connexions and of importance to us in such very different ways. that they naturally have obtained distinct names: yet one of the createst stems in the history of chemistry was connected with the discovery that they are, chemically speaking, all processes of the same kind, viz. the combination in the first two cases of carbon and in the third of iron with the oxygen of the air.1 These cases illustrate the way in which it may be necessary to ignore our customary classification of things, and bring together, upon the strength of some identity which an analysis may have discovered in them, things that we have habitually kept quite apart in thought. It is consily necessary at times to distinguish things which we have habitually classed together, if we are to make any progress in the investigation of them. The case of rent furnishes a good instance. The name is given equally to the sum which a man neve for the occupation of land, and to that which he neve for the compation of a building; as these are very commonly raid to the same person, as a lump sum is then charged for the two. and as the ordinary tenant in search of a dwelling is prepared to pay so much for accommodation, but indifferent to the question whether the owner considers his charge to be based on the value of the house or of the site it stands on, it follows that most of us find no inconvenience in this double use of the word. The farmer who has to consider separately what the land he farms is worth to him per acre, and what the value of the homestead is to him, is more or less aware of the ambiguity: but the political economist. when he comes to consider the causes that determine rents, is bound to distinguish house-rent and ground-rent by name. Indeed until that is done, his investigation will make no progress; for the two depend upon quite different conditions. The rent of a house. apart from any special history or sentiment, depends chiefly on the cost of building another like it, and the current rate of interest on money in the country at the time; but land cannot be produced as it is wanted, and this natural limitation of supply may give to a particular piece of land, in virtue of its fertility or its situation. a rentable value that depends mainly on its superiority in those ¹ Cf. pp. 486, 437, infru. Of course the oxygen need not be atmospheric oxygen. respects over other land which cannot be dispensed with for cultivation or for building, and only very slightly and remotely, if at all, upon the circumstances which regulate house-rent.

The process of discovering identities between things in which we commonly ignore them and that of discovering differences between things which we commonly take for the same very generally involve one enother. We perform as it were a mental re-ornuping and in the set of bringing together what we had hitherto only distinemished we most probably break up or find distinctions in the eronne from which members are brought together. But in a given case one aspect may be much more prominent than the other; and Bacon has observed I that some men have a prester canacity for the one kind of work than for the other, insisting (like Plato before him) on the necessity of noting in the investigation of nature, both the resemblances and the differences that are ordinarily overlooked. Analysis is at the bottom of each process for until we have distinguished the various characters of things, we have not discovered the bases on which to compare them. It must be added however that analysis may be of great importance, yet without leading to any act of fresh classification, when we want primarily to know the circumstances under which a phenomenon occurs.

We have now to some extent considered the nature of the work involved in the performance of the two tasks above mentioned: namely, in determining precisely the phenomenon we have to study, and in distinguishing and detecting the various circumstances under which it occurs, or under which it fails to occur when perhaps we should have expected it. It is sufficiently obvious that without performing them we should hope in vain to discover causal connexions by way of induction. If we have no precise or exact conception of the phenomenon to be studied, or have not (as one might say) duly determined it, we may examine instances that we ought to ignore, and ignore instances that we ought to examine. The result of the former error will be that we shall try to make our theory as to the cause of a consistent with the facts of the occurrence of a different phenomenon y: and the result of the latter, that we may be ignorant of facts which might throw great light upon the cause of g. The necessity of making a correct enumeration of the circumstances under which a phenomenon occurs, before asking with which of them it is causally connected, needs no comment; nor is it less plain that, if the question is to be answered, we need equally to recognize the circumstances, where they occur also in the absence of the phenomenon.

But though this work is so necessary, it is impossible to give any rules for the efficient dispatch of it. Familiarity with a science may help a man to perform it in the investigations of that science, teaching him the sort of thing to look for, and the sort of way in which to look for it. Yet the seganity upon which the discovery of new truth depends does not come to most men even by such familiarity. The logician's business at any rate, since he cannot teach them to do it, is to make men realize the part which it plays; and one or two further examples may be given with that object.

A research which has been so frequently cited in works on Induction as to become almost a stock instance will serve this purpose-Welle's Theory of Dew. Dow, as is now pretty generally known, does not rise but falls : the atmosphere can hold in suspension a certain proportion of water in the form of vapour, but the amount depends upon the temperature of the atmosphere, and increases with it. If anything suddenly chills the atmosphere, it precipitates such a portion of the moisture which it holds as exceeds the maximum it can hold at the temperature to which it is reduced. It may be chilled in various ways. One is the contact of a colder surface, on which the moisture is thereupon precipitated : and the rapidity with which the surface of a body gets chilled depends on various circumstances-partly on its substance, partly on its texture (rough surfaces, or those with many points, like grass, radiating heat more rapidly than smooth ones); another way is by the inrush of a heavier and colder current; another is by radiation to the sky, and the degree to which that takes place depends on the amount of cloud about; a sheet or other covering stretched over the ground acting in the same sort of way over a small area, though with more effect over that area, as the clouds spread out over the earth. This precipitation of moisture held in suspension in the air is seen not only when dew falls; when warmer weather comes after a frost, particularly if accomnamied by rain, the cold surface of a stone wall, if painted or otherwise not porous, drips with the water it has extracted from the air which its contact chills. In the same way cold spring water poured

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into a clear in summer will shill the outside of the clear so that water is denosited on it from the air without and when hot water is nouved into a class without filling it and sends its vanour into the air shove some of this vanour belows the interior surface of the class shove the water-level until this portion of the class has acquired by conduction the temperature of that below it. Now our present business is not with the reasoning by which Wells showed the denosition of dew to depend upon a relation between the temperature of the atmosphere and of the body on which the dew fell.

• * taken in conjunction with the degree of saturation of the atmodia. sphere at the time. But it is plain that he could never have done w. this, if he had not taken note of all the above points, the material and texture of hodies, as affecting their surface-temperature. .. the clearness or cloudiness of the nights on which he looked for 'n. dew, the conditions of air and wall when the latter drips with ω, moisture, and so forth. It would have been in vain to observe that one body collected more dew and another less, unless their roughness and smoothness were noted, as well as their substance : A** * or that on some nights there was heavy dew and none on

others, unless the saturation of the atmosphere were ascertained as

well as its temperature. And similarly, it was necessary that he should get a right conception of the thing called dew that he proposed investigating. There are clammy days when everything grows damp from a moist fog hanging in the air. It would not have been unnatural to look in this for a phenomenon of the same nature as dew, and to overlook such things as dripping walls and moisture-frosted tumblers. Yet the mistake would have nut the enquirer altogether off the scent. Curative effects of different kinds are exhibited by certain

waters. To the eye many of the waters are indistinguishable; and if the palate detects a difference, yet it would not be found possible to connect efficacy in particular complaints with particular flavours according to any explicit and invariable rule. It is plain that no progress can be made unless the various diseases are described not merely by their more obvious symptoms but by reference to the physiological character involved; and the water chemically analysed, so that one may know each separate ingredient, and the different proportions in which they are present in different cases. Again, the

bacteriological theory of disease would never have been formulated,

until the heaterie themselves were found_hodies so small that before the construction of powerful microscopes their presence was of necessity overlooked; and when one hears of pathologists endeavouring to isolate the microbe of some particular disease one realizes how impossible it is without the preliminary work of distinguishing the circumstances, to apply the 'canons of induction' to any effect. Or suppose that an enquiry is undertaken not into the physiological cause of a disease, but into the causes of its dissemination, either generally or on some particular occasion; let the disease, for example he meleria. Malaria was long supposed to be contracted from the exhalations of the ground; and it was true that many malarious districts were marshy, and that persons who avoided the swamps at dusk and dawn seemed less liable to be infected : but it was not until it was noticed that such districts were infested with mosquitoes of a particular species, and it occurred to some one to connect this circumstance with the communication of the disease. that false ideas were exposed and the true law of the matter established.

The last remark suggests a transition to the next preliminary

operation that we may notice—the formation of hypotheses. Much has been written upon the question whether Logic can lav down any rules by which the formation of hypotheses should be controlled; but beyond the somewhat obvious and quite general consideration that an hypothesis must contain nothing inconsistent with principles which thought finds necessary, it does not seem that Logic can be of any more service here than in the performance of the work of analysis. It would be an illegitimate hypothesis on the part of a bank clerk confronted with a small discrepancy in his books. to suppose that on this occasion two and two made three; but a petty theft on the part of the Principal Manager, though very likely a foolish hypothesis, would not be logically illegitimate. It might indeed be urged, that the hypothesis of angelic intervention, though there is nothing inconceivable in the existence of angels, would not be a legitimate way of proposing to account for an event; and this may be admitted; for there is no use in attributing phenomena to causes whose presence we have no means of ascertaining: since such hypotheses can never be brought to the test of facts. It is obviously more reasonable to go on trying to account for them by ascertainable natural causes in the hope of being able to connect

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them by general principles with other observable phenomena then to abandon that hope at the outset and invoke the agency of beings whose existence cannot be empirically verified; so that although we can hardly pronounce it logically inconceivable (however it may be scientifically inadmissible) for the physical order so to depend on something beyond itself as to make it impossible to account for a particular natural event by reference solely to other natural events preceding it, yet we may on logical grounds pronounce it unscientific: i.e. it is seen to be unscientific not in virtue of any special knowledge of the particular science to which such hypothesis belongs but in virtue of our general appreciation of the aim of science as such, and of the logical conditions under which that aim can be realized. And this is perhaps what Mill really had in his mind when he said I that 'It appears then to be a condition of the most genuinely scientific hypothesis, that it be not destined always to remain an hypothesis, but be of such a nature as to be either proved or disproved by comparison with observed facts'. It should he of such a nature that observable facts if see could find them might prove or disprove it 2: i.e. it should not appeal to the agency of causes (like the intervention of an angel 3, or the influence of the organic type as a whole upon the growth of the individual organ. ism) of whose presence we can have no independent evidence. and whose nature we are not able so to ascertain as to determine deductively how they must act if they are present: for with the accency of such causes as these any facts are equally compatible: and thus they furnish no explanation why the facts are so and not otherwise. For this reason, as Bacon said, in looking for the causes of things in nature Deum semper excipinus 4: and Laplace. when Napoleon observed to him that there was no mention of God in his Mécanique Céleste, replied that he had no need of that hypothesis. But that an hypothesis should be of such a nature that observed facts will ultimately either prove or disprove it, and not merely might ultimately do so, seems a condition quite impossible to

Logic, III. ziv. 4.
Facts, as we have seen, cannot prove an hypothesis by their agreement with it, except so far as at the same time they disprove its rivals by their disgreement.

2 Cf. Newman's Parochial and Plain Sermons, vol. ii, Sermon xxix, on The

Feast of S. Michael and all Anoels.

De Principiis atque Originibus, Ellis and Spedding, III. p. 80.

lay down. We cannot tell the future in these matters : how long may an hypothesis be destined to remain an hypothesis without prejudice to its genuinely scientific character? The ultimate destruction of life on the certh is commed by ecience : for human minde an hypothesis which is not proved or disproved before that date will always remain an hypothesis. We cannot enprose that its ecientific character, when it is made is to be estimated by the proenect of its truth being definitely secentained a few years or even a few myriads of years earlier or later. Darwin in the Origin of Species 1 writes as follows . As the embryo often shows more or less plainly the structure of the less modified and ancient procenitor. of the group, we can see why ancient and extinct forms so often resemble in their adult state the embryos of existing species of the same class. Acassiz believes this to be a universal law of nature. and we may hope hereafter to see the law proved true. It can however, he proved true only in those cases in which the ancient state of the progenitor of the group has not been wholly obliterated. either by successive variations having supervened at a very early period of growth, or by such variations having been inherited at an earlier stage than that at which they first appeared. It should also be borne in mind, that the law may be true, but yet, owing to the geological record not extending far enough back in time. may remain for a long time, or for ever, incapable of demonstration.' But that the rule in question is an universal law is a scientific hypothesis.

An hypothesis then must be thinkable 2, consistently with the fundamental assumptions of the science which makes it : but we cannot restrict, within these limits, the freedom of scientific hypothesis. What is important is that men should be cautious not in

¹ Origin of Species, c. xiv. 6th ed. p. 396. The italics are mine.

¹ Origin of Species, c. xiv, 6th ed. p. 386. The italies are mise. ¹¹ Dotie would explain this by saying that our hypotheses must conform to our postulates. He draws a distinction (Lepic, § 273) between a postulate as ¹an absolutely necessary semmytion, without which the content of the observation with which we are dealing would contradict the laws of our postulate than abstractly stated by precifying the concrete causes, forces, or processes, out of which the given phenomenon really arose in this particular case, while in other cases maybe the same postulate is to be satisfied by utterly different though equivalent combinations of forces or active elements. ¹I takend be added, that in saying that hypothese must be thinkable consistently such the fractionantal commytions of the accesse subject and and a continue of the cases which is the content of the content of the cases when the case of the case of the cases when the case of the cases when the case of the case of the cases when the case of the case of the cases when the case of the case of the cases when the case of the case of the case of the cases of the case

framing but in testing hypotheses. The publication of every wild conjecture is undesirable; but it would be consily undesirable that a man should never entertain an hypothesis which contemporery opinion could propounce wild. Derwin said that he had framed and abandoned many an hypothesis which he would be ashamed to avow . he does not imply that he was ashamed to have framed them. The best control over the licence of the imagination is exercised by special knowledge. The man who knows most about any department of nature will see most readily what hypotheses are foolish in that department, just as in such practical matters as legislation the best critics of a bill are those who have experience of the affairs with which it deals.

It is clear that every causal connexion presents itself at the outset in the light of an hypothesis, to the mind to which it first occurs. The framing of the hypothesis may sometimes be very simple. though the proof of it may be very difficult. If we know exactly what persons were cognizant of a secret which has been betraved. it is easy to say that one of them must have betraved it: and so far there is no hypothesis; hypothesis begins so soon as we secribe the offence tentatively to any one of them, and in this there is not the least difficulty; but a proper test of it may be impossible. Whereas Here, however, all the alternatives are before us, and in the abstract any one of them would equally fit the facts, because it is simply a question of connecting an event s with one of a number of conditions s b c. about which we do not know enough to say that it might not be connected with any one of them: yet commonly it happens that the facts which an hypothesis has to fit are more or less elaborate: and then the framing of it is not such a simple matter as the pairing off of two terms a and x. Take for example the question of the authorship of the Acts of the Apostles; if that book must have been written as it stands by one of the recorded companions of St. Paul's journeys, it is a simple thing to say that the author may be Luke, or may be Silas: although it need be by no means a simple thing to decide between them. But if that is not necessary, facts in terms of them.

framing them. We restrict it to something which the facts of experience might test: but the fundamental assumptions of a science may be meta-physically untenable, and we enlarge it to extend to all which these assumptions cover, however it may be ultimately impossible to think the

if the book may be of late date, and contain the work of several hands, it becomes very difficult to frame an hypothesis which shall do instice to all the features of it. We have a large number of facts to co-ordinate: and the semmptions by which we connect them must all be mutually coherent. Historical criticism presents many problems, where no hypothesis is free from difficulty; and though doubtless a problem must have a solution, yet an isporance of some details, and very likely the erroneous accounts that we have received of others, may leave us permanently unable to find it. And the penetration and incremity of the historian are shown in such cases in devising as well as in testing hypotheses : indeed the two operations cannot be kept altogether distinct : for when our knowledge of the concrete detail of events is considerable, the process of framing an hypothesis to fit them all is itself a process of testing. Now what is true in history, where upon the whole 1 our business is rather to determine events in conformity with acknowledged principles than to determine principles in accordance with empirically accortained events is true also in science of whose business the letter would be the more accurate description. Scientific hypotheses consist for the most part not in the mere coupling in the mind, as cause and effect, of two insulated phenomena (if the epithet may be allowed): but in the weaving of a large number of phenomena into a coherent system by means of principles that fit the facts. In the framing of hypotheses therefore we are called upon to conceive facts in new ways: and to conceive not simply that certain facts are connected, but how, or in accordance with what principle, they are connected. And this often involves a radical transformation in our way of looking at the facts themselves: for a fact is not such an easily accertainable thing as the language we sometimes use might seem to imply. In a sense facts are stubborn: in another sense they are pliant to our thought. They are stubborn so far as we have rightly apprehended them; but what we call fact is largely matter of inference and interpretation, performed often unconsciously, and often erroneously: there is room

¹ Upon the whole, because the historian has often to rediscover principles—constitutional, legal, social, or economic; and history advances by changes in mon's way of conceiving the relations of past facts to one another as well as by changes in their ries of what the facts were. We no longer bolisve in William Tell; but the Patriarchal Theory has also changed our views as the relations between the individual and the State in ancient society.

***1 PRELIMINARIES OF INDUCTIVE REASONING 488

here for re-interpretation, in accordance with the requirements of the rest of our knowledge, and so far as facts lend themselves to this they may fairly be called pliant. It would have been called a fact, for example, in the days before Copernicus (though some of the Greeks had questioned it) that the sun went round the earth; but this was only an interpretation of appearances which we have now been taught to see to be equally compatible with the fact that the earth goes round the sun. It would have been called a fact that peoies are fixed and immutable; and it is the case that they breed so true upon the whole in any non generation as to make that a fairly accurate statement for practical purposes. Yet we have learnt to see that this comparative stability is consistent with any degree of modification over long enough periods of time. These instances will be enough to show how the familiar facts take on a new appearance in the light of new theories.

Now some new theories or hypotheses are, as we all know. more far-reaching in their effects than others: for some are much more general, and apply to a much larger number and variety of facts. Their introduction marks an epoch in the progress of science : and Whewell attached more importance to the framing of such hypotheses than to any other of the operations connected with inductive reasoning. Indeed he held that this step was the induction; and that the history of the inductive sciences could be represented as the preparation, elaboration, and diffusion of successive hypotheses each more adequate to all the facts of a science than its predecessors. He did not use the word hypothesis very prominently in this connexion : he preferred to speak of conceptions : and what he called the colligation of facts by means of appropriate conceptions 1 was in his view the essence of induction. The new conception, however, is always an hypothesis as first entertained, and only converted into a part of the accepted body of knowledge by its superior success in co-ordinating facts. This work of 'colligation' therefore must not be regarded as something distinct in its nature from the framing of hypotheses: it is rather a special and important case of it, where the hypothesis, instead of merely connecting facts in a more or less familiar way that leaves our view of them very much what it was before, involves a profound and far-reaching

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¹ v. Novum Organum Renovatum, Bk. II. c. iv: Philosophy of Discovery, c. xxii. 55 1-37.

change in our view of the facts themselves. Thus the succession that malaria is communicated by the bits of the Anopheles mosunito neither altered seriously our notion of the nature of that insect (though it altered our practical attitude towards it in a way by no means favourable to the numbers of Anopheles) nor introduced any new way of conceiving disease; for the bacteriological conception of disease had already been applied to many other fevera. But the first suggestion that a disease depended on or consisted in the presence and multiplication of some specific notions becillus. in the blood altered profoundly men's view both of what it was. and of how it was communicable, and of how it might be cured. In the relation of this 'colligation' to the more general notion of framing hypotheses we have an instance of the difficulty of distinenishing sharply the different operations of thought which logicians have enumerated as preliminary (though by no means subordinate) to such application of the rules on which inductive reasoning rests as we examined in the last chapter.

A somewhat unprofitable controversy arose between Whewell and Mill as to the part which the 'colligation of facts' should be regarded as playing in induction. While Whewell said it was the induction. Mill said that it was improperly so called. Mill seems to have been influenced in part by the idea that an induction must end in establishing a general proposition, whereas it is possible to bind facts together by a new conception and so place them in a different light and reinterpret them, without apparently generalizing; he seems too to have considered that nothing in the whole process of thought, by which general conclusions were reached from the examination of particular facts, ought to be called induction, except what could be reduced to the form of inference or reasoning : the rest was all subsidiary to induction. But the operations of thought preliminary to the application of such rules as inductive reasoning rests on are not subsidiary in the sense of being of secondary importance; and it would perhaps also be better to distinguish induction as the whole process from the reasoning employed in it. We might then agree with Whewell that in induction, i.e. the whole process of the 'interpretation of nature', what he called the 'colligation of facts' is an operation of the very first importance, demanding higher and more uncommon powers of mind than inductive reasoning; while we agree with Mill that it is not the

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inferential eneration. But if hy induction we meen the inferential operation, then we shall have to say that this 'colligation of facts' is more momentous in the history of science than induction : for most of us as Becon rightly said 1 would light upon the use of the methods of inference to which Mill would restrict the name of induction by our ordinary intelligence, without their being formulated for us but few can originate the new concentions that bring order and intelligibility into a mass of facts.

The instance which served to illustrate the dispute will help to show what this 'colligation' is. The ancients at first supposed the planets to move in circles round the earth. When further observation showed that this was not so, they conceived the centre of the circle in which a planet moved to travel on the circumference of another circle: these circles were conceived not as mere imaginary paths, but as physical entities actually revolving: and it was possible to assign such a radius and rate of revolution to them as would account for the planet fixed upon the outer circle describing the path it does. This hypothesis had grown more and more complicated, as the mass of observations upon the movements of the planets had increased; and though it was capable of application to the heliocentric no less than the geocentric theory. Kepler sought for one more satisfactory. After trying a large number of other curves, and rejecting them on the ground that they did not agree with the observations, he at last discovered that the planet Marsthe primary subject of his investigations-moved in an elliptical orbit round the sun, which stood in one of the foci. Now the ellipse is here the appropriate conception which binds together into an unity the successive observed positions of the planet Mars. Each position taken singly must of course necessarily be on the circumference of that or any other curve; for any curve can pass through any point. But he sought for a curve which would pass through all the positions; and he found that in an ellipse. There was indeed nothing disjunctive in his argument. Other curves were rejected because disproved by the observations; but the ellipse was accented because the observations agreed with it, and not because no other curve would satisfy them. If it had suggested itself cooper, the others would not all have been tried. There are curves, of higher degree, that will equally satisfy the observations, and had 1 Nov. Org. I. 180.

they occurred to Kenler, he could perhaps have given no other reason. for preferring to accept the ellipse than an a priori preference for the simplest curve that would do so. It is to be noted however. that even here the critical matter was the thinking of an ellipse and not the testing its agreement with the facts: any one with the necessary methematical training could have done that whenever the ellines had been thought of. And so it often is though not always. when the appropriate conception is a conception of causal relation; not always because sometimes there may be as much difficulty or more in testing the concention than in thinking of it. To test it we may have to deduce its consequences by some intricate mathematical calculus as in the case of the Newtonian theory of pravitation; or to devise an experiment in which we may see whether the theoretical consequences of our concention occur. Great mathematical power or great ingenuity may be wanted here; but the reasoning will be deductive. Yet even so, to introduce the appropriate conception is much; new ideas are scarce; inductive reasoning, if the material were given all ready prepared, is easy, An excellent example of the part which a new hypothesis may

play in inductive enquiry is furnished by the Ozwacz theory. It is horrowed from Whewell 1, whose works afford many more. It was for a time supposed that combustible bodies were combustible because of the presence in them of a peculiar substance. that escaped in the process of burning. This hypothetical substance was called phloriston; and it was very natural to think that one could see it escaping into the air wherever a fire was burning. When it was found that there was one air (or, as we should now say, gas) in which bodies burnt readily, and another in which they would not burn at all, it was conceived that air could only absorb a limited quantity of phlogiston in proportion to its volume; in the former it was supposed that there was no phlogiston, and it was called dephlogisticated air: the latter was supposed to be already saturated with all that it could hold, and was called phlogisticated air accordingly. The phlogiston theory received a shock when it was discovered that if a body were calcined or reduced to ashes, in a closed vessel, the weight of the ashes was greater than that of the body before it was burnt. This, however, was explained by supposing phlogiston to be a substance naturally 1 Whewell, Hist. Ind. Sci., vol. iii. Bk. XIV. 11, 4-7.

really presenting great difficulties in relation to the theory of gravi-

conception to the facts: he conceived that when a body harned what happened was not that a substance naturally light escaped from it into the air, and so left it heavier: but a substance naturally heavy was withdrawn from the air and combined with the burning body: burning in fact was a process of what we should call chemical combination; and Lavoisier supported his theory by showing that after the calcination of a body in a close vessel the air in the vessel was lighter by the same amount by which the ashes were heavier: this observation perhaps was not conclusive if the phlogiston had carried its natural levity into the air . but the new way of conceiving the facts accorded far better with the general theory of gravitation. The substance thus withdrawn from the air in burning he called oxygen; and oxygen now took the place of dephlogisticated air while phlogisticated air, instead of being conceived as esturated with phloriston, was conceived to be a different substance from oxygen, incapable of entering into those chemical combinations which constituted burning. This substance was rechristened azote, and afterwards nitrogen. Lavoisier further showed that oxygen was withdrawn from the air and chemically combined with other substances not only in burning but also in the familiar process of breathing, and in the rusting or oxidation of iron, which could rust in water also because oxygen was present there as well: and thus his new conception, that burning was really a process of chemical combination between a substance in the atmosphere, which he called oxygen, and the substance of the body burnt, served to throw light equally on processes at first sight quite remote from burning. In this example, therefore, we have as it were a 'colligation' of two kinds: primarily, in so far as a large number of facts about burning were all rendered consistent with one another and bound together by the help of this new conception of what goes on when a body burns; secondarily, in so far as that conception was shown to be applicable to other phenomena as well as burning, and they are therefore brought under the same explanstion with it. It may be worth while to give one more example of the transforming and connecting power exercised by a new and appropriate concention upon a multitude of facts, in the biological theory of Evolution, or the modification of species through natural descent. We are not for the moment concerned with the question whether the only agency in determining such modification is Natural Selection. The theory of Natural Selection, as a theory of the way in which modifications have, not indeed originated, but been established when they had once arisen, teaches that in each generation individuals vary more or less in colour, size, structure, &c., from their parents: that some of these variations are useful to their possessors under the circumstances in which they live; and that their possessors will, in the constant struggle for existence going on in the world. have an advantage over their competitors; so that those individuals who happen to possess 'adaptive' variations will survive and propagate, while their less fortunate and worse-adapted rivals will perish; and thus species are brought into and kept in conformity with the conditions under which they have to live. Now there is not complete agreement among biologists either as to the extent to which the neculiarities of different species of plant or animal are adaptive, or as to the extent to which those that are adaptive can be accounted for by the theory of Natural Selection alone: though there is no doubt that the doctrine of Evolution won its way on the strength of the success of the principle of Natural Selection in accounting for at any rate a vast number of adaptive structures, instincts, and colourings. But the doctrine of the Evolution of Species, or their modification by descent, as opposed to their special creation in immutable form, does not stand or fall with the view that Natural Selection is its exclusive modus operands. This doctrine has brought into intelligible connexion with one another whole departments of fact. It explains the various and intricate relations of likeness and unlikeness between different species of the same genus, different genera of the same family, different families of the same order, &c. : it explains why the same structural plan is observed in many cases where the function of some part of the structure has been lost or altogether altered; and why it is that where their life requires the performance of the same function in groups otherwise very remote morphologically from one another, we find the function fulfilled by such very different means as are, for example, the wing of an insect, of a bird, of a bat, and of a fivingfish. Again, it explains the divers series of fossil forms; and

accords with the facts of embryology, such as that the embryo of a given vertebrate only gradually develops the more distinctive specific features, and at an earlier stage is very little distinguishable from the embryo belonging to a different genue on family : for the characters which appeared later in the course of evolution and supervened as it were more simpler structure enness leter in the growth of each subsequent individual of the same more complex type. and supervene upon the simpler structure there. Again, it explains the facts of geographical distribution such as that the degree of affinity between species is much greater when they inhabit a continuous area, than on either side of a geographical barrier; and that the barriers on either side of which the difference is most marked are not the same for every kind of organism, but are for each kind those which would offer the most effective obsteole to the migration of that kind-high mountain ranges in the case of land animals or fresh-water fish, deep sea in the case of salt-water fish. and so forth : or such facts again as this, that 'wherever there is evidence of land areas having been for a long time separated from other land areas, there we meet with a more or less extraordinary profusion of unique species, often running up into unique genera. All these facts, and many others, for which upon the old hypothesis of the special creation of immutable species it is impossible to suppost a reason or a motive, fall into line upon the hypothesis of modification by descent, and are bound together by that conception as common consequences.

We have now considered some of the most important operations. without which inductive reasoning would be powerless to advance inductive science. One or two others may be noticed. It may seem unnecessary to mention the observation and registration of facts: vet that is no small part of the work that has to be performed before we are in a position to tell what phenomena may be supposed to stand related to one another as cause and effect. Along with this goes often what was incidentally referred to on p. 4862-the devising of experiments by which to test whether a phenomenon is

¹ Romanes, Derwin and ofter Denwin, i. 235 st al.
² The other process, of mathematical calculation, there referred to, falls rather to be considered later: as belonging to a stage of science in which deductive reasoning plays a larger part than in the application of the rules discussed in the last chapter.

present or absent, varies or is constant, as should be the case if its cause is what we take it to be. If it be supposed, for example, that spirit-rapping is really produced by 'cracking' the joints, it will be necessary not only to show that a man can produce unch noises that way, but to devise conditions under which one may be certain that the joints cannot be 'cracked' without its being detected, and see whether the 'spirits' still continue to rap.\text{The collecting and sifting of statisties, and their reduction to tabular form or curves, is also in many enquiries a necessary preliminary to the application of the rule that nothing can be the cause of a varying phenomenon which does not vary proportionately with it.

This is perhaps enough to say upon the present subject. There are other tasks set to our thought in science, which are of great importance to its development: but we have been concerned especially with those that are presupposed in inductive reasoning. The help afforded to the 'interpretation of nature' by a well-choses armours of technical terms, great as it is, is not confined to the use of inductive researing. And the work of abstraction has had account taken of it in what was said of analysis and hypothesis and the formation of conceptions. By abstraction we mean considering some special feature of the concrete fact, in mental separation from all with which it is combined in its existence. It is between feature and feature that we strive to trace connexion. The concrete mass of events changes from moment to moment. Not until we pick it to pieces are we able to see what it is in one state of the mass that determines what in another. Every common term involves some degree of abstraction; but in science we have to break up what in daily life we treat as a single matter, and to consider by itself, or in abstraction, that which had hitherto not been specially noted and distinguished in the total nature of some comparatively concrete notion.

¹ r. Podmore's History of Modern Spiritualism, i. 184, 185.

CHAPTER TYII

OF NON-RECIPROCATING CAUSAL RELATIONS.

In all that has been so far said with regard to the process of inductively determining the cause of a phenomenon, it has been searmed that the cause, whatever it is, reciprocates with the phenomenon: i.e. that not only does the phenomenon occur whenever the cause is present, but that the cause must be present whenever the phenomenon occur; so that you may selfly argue from either to the other, as in geometry you may equally infer that a triangle is equilateral from the fact that it is equilateral, and that it is equilateral.

But we often speak of one thing as being the cause of another, where this reciprocal relation by no means obtains. We say that drunkenness causes crime, although many people get drunk without committing crime, and many people commit crime without getting drunk. And in some of the examples of inductive reasoning given in previous chapters, the cause found was not a reciprocating cause. The appearance of congenital epilepy in guines-pige was shown to be possibly due to a traumatic injury producing epilepsy in the parent; yet it was not alleged that the production of epilepsy by these means in the parent was always followed by the appearance of suilersy in the offscoine.

If was said that the inductive proof of the cause of a phenomenon rested on the definition of cause; for nothing that does not stand to the phenomenon in relations that estaify the definition can be the cause of it; and it is by eliminating all alternatives that its cause is inductively established. Our definition of cause assumed that it reciprocated with its effect. But if it does not, we clearly have no right to eliminate whatever fails to reciprocate. The admission that there are non-reciprocating causal relations may seem therefore to invalidate reasoning that starts with the assumption that cause and effect reciprocate.

This difficulty has been postponed till now, partly that the exposition of the subject might not be unduly complicated: but

also because the causal relation is really, and in its strict sense. reciprocal and without understanding that first, we could never render non-reciprocating causal relations intelligible to ourselves. Properly speaking to give the cause of anything is to give every. thing necessary and nothing superfluous to its existence. Nevertheless we should often defeat our ends if we gave precisely this . if our object in seeking the cause of a thing is that we may be able to produce or prevent it and if something is necessary to its existence which is a property of an object otherwise superfluous. it would be of no use specifying the property necessary unless we also specified the otherwise superfluors object in which it was found.1 Even though we have no such practical purpose, so long as we do not know what object contributes, in the property which it possesses, the factor necessary to the effect, we can hardly be said to understand completely the production of the effect. Hearing at a distance, for example, depends on the transmission of certain vibrations through an elastic medium: the necessary elasticity is a property of the air: and therefore we can hear at a distance in the air, while if there is a vacuum interposed between the sounding (i. e. the vibrating) body and the ear, the transmission of the sound is prevented. It is true that, except in respect of its elasticity, air is quite superfluous so far as hearing at a distance is concerned : not air in the concrete, but that property in abstraction, is one of the conditions that make up the reciprocating cause of hearing at a distance. But an elastic medium cannot be just elastic and nothing else besides.2 We want to know what possessed of the necessary elasticity is present when we hear at a distance : nor could any one. without knowing that, prevent the transmission of sound by removing the elastic medium : for he would not know what to remove.

We may pursue this illustration a little further. It might be shown inductively that the intervening air was the cause of the trans-

^{1.6.} g., it may be the texture of pumice-stone that fits it to remove intertains from the skin; but it would be of more use to tall a man with lawly fingers to get a piece of pumice-stone, than to give him a description of the finences of texture which would render a body capable of making his fingers clean.

ingers clean.

It is just the fact that we know no more about the ether than its form
of elasticity which makes it a somewhat unsatisfactory conception; and led
the late Lord Salisbury, in his Presidential Address to the British Association
at Oxford in 1894, to say of it that it merely 'furnished a nominative case
to the web to acadisate.'

mission of sound: indeed it was shown inductively. by the help of a well-known experiment. And speaking loosely, it is true that from the presence of air it can be inferred that sound will be transmitted and reciprocally from the transmission of sound that air intervenes. Yet neither inference is quite safe. The first is only true with qualifications . the distance must not be too great in proportion to the londness of the sound, and so forth. The second may be altogether false. for sound can be transmitted through water, or (with the help of a telephone 1) through a vacuum. And in this case the reason is that the elasticity is provided in some other way than by means of a continuum of air. We saw that, except in respect of its elasticity, air was superfluous : but we could not get the elasticity alone. Now we find that there are other elastic media which will serve, and the elasticity may be provided by them. An elastic medium is what is wanted : but divers things will supply the want. They are alternatives, and none of them exclusively reciprocates with the effect; for the effect may be produced by the help of any one of them, so that the occurrence of the effect does not prove that any one more than another is producing it. But their common property of providing an elastic medium does reciprocate . sound cannot be transmitted without that

There is, then, always a reciprocating cause : but it is not always most instructive to state only that. And very often that is not what we want to know. There are several reasons for this.

In the first place, though the object of a science is to discover strictly universal propositions and though in most sciences these involve relations of cause and effect, yet as a science advances, its problems often take a different form than that of an enquiry after the cause of a given phenomenon. We may start with some phenomenon that seems comparatively simple: and, as we proceed, may find that it depends upon a number of conditions being combined together. each of which can be fulfilled in a number of ways, but none of them without much that is superfluous or irrelevant to the production of the phenomenon in question; each is an incident of some concrete event, or implies the operation of a property of some concrete object.

¹ The elasticity of the air is employed also in the telephone: but not continuously. It is hardly necessary for the present purpose to go into the detail of the apparatus.

Not in any branch of purely mathematical study; nor again in Logic.

like the elasticity of air in the case of the transmission of sound. To state in abstract form the conditions that must be satisfied. without indicating the kind of object or event in which such conditions can be realized is uninstructive : for it fails to explain by what the phenomenon is produced - yet to mention every object or event in which the conditions might be realised would be an andless and unprofitable task. Hence we alter the form of our noblem. Looking upon the phenomenon as the complex result. of many conditions, we attempt to determine not what assemblaces of chiects or events will produce the result, nor on what properties or incidents therein it depends : but what is the principle of action in different objects or events, in virtue of which some one particular condition necessary to the production of the phenomenon is realized in them. For the reciprocating cause of a complex phenomenon we substitute as the object of our search the principle in accordance with which a certain kind of object or event acts. Our problem is better expressed as that of discovering laws of nature, than causes. For example, we may ask what is the cause of the monacons-that is, of the regular and periodic winds that blow steadily in certain regions for one part of the year in one and for another in the opposite direction? If we said that they were due to periodic alternations in the distribution of atmospheric pressure, it would not be very instructive; for we really want to know what events. happening in those regions, produce these differences. Yet the events which contribute to determine the deviation and direction of the monacons are numerous and variable : the exact combination of them differs from year to year and from place to place, and produces corresponding differences in the result. It is better therefore to take these events, by their kinds, singly: to point out the difference in power of the sun at any place produced by the varying directness of its rays; how the sea gives off vapour; how vapour absorbs part of the heat of the sun's rays; how the heated water circulates with the colder; how the earth absorbs and retains the heat of the sun : how air is expanded by heat ; how the principle of atmospheric pressure acts under conditions of different expansion : and so forth. Then we can see that if a certain combination of events occurs. a particular complex result must arise; if the sun travels from over the sea to over the interior of a continent, we shall find monsoons; for the difference between summer and winter temperature will in the interior be very great, but on the sea, owing to the way in which the moisture of the air absorbs part of the heat, and the currents in the water carry away part, it is not so great; hence as summer is ending, the air inland will be hotter and have expanded more than out at sea, as winter is ending it will be colder and have contracted more; so that to ne time the current of air sets inland in accordance with the laws of atmospheric pressure, and at another time it sets shorward. The principles, or ways of acting, on the part of the sun according to its altitude, of the earth and eas

respectively under the influence of heat of air when unequally expanded &c. are not exhibited solely in the phenomena of monecons: while the details of those phenomena display the influence of other principles of action on the part of other objects (e.g. the action of a mountain-wall on a moisture-laden wind). To give the cause of monecons, without deficiency or superfluity, would mean that we must not mention the sun (because only the heat of its rays is material) nor the sea (because only its fluidity and its power of giving off vapour concern us, and a lake, if it was big enough, would do as well) nor any other of the concrete things which act in the way required, but only their requisite actions. If we do not go to this length of abstraction, we shall have to include in our statement of the cause elements at least theoretically superfluous : and even so, we shall have to choose some particular monsoon, supposing we are to state everything that goes to produce it. It is clearly simpler to break up the problem, and look for the principles in accordance with which objects of a certain kind act under certain circumstances; then we can show that the monsoon is only the complex result of the action of a number of objects under the

principles of action which our 'laws' express.

This then is one reason why what we want to know is not by any means always the reciprocating cause of a determinate phenomenon: the phenomenon under investigation is often highly complex, and subject to all sorts of variation on the different occasions of its occurrence, through variation in the objects or events contributing to its production; not the whole nature of the objects or events under whose influence it occurs is relevant to its occurrence, but only certain particular properties or modes of action; and it is possible to formulate severally the principles of action involved.

particular circumstances of the case, and in accordance with the

from which the joint result may be seen to follow, where it would not be possible to assign to the phenomenon any group of concrete objects or events as cause, about which we could say not only that, given them, the phenomenon, they must have been given too. These laws or principles of action may of course be proved inductively in just the same way as may a causal connexion between two particular phenomena a and a. Just as we may argue that a cannot be the cause of a, if it occurs in the absence of a, or is absent when a course, so we may argue that a cannot be the cause of a, if it occurs in the absence of a, or is absent when a course, so we may argue that a law or principle of action cannot be rightly stated, if consequences should follow from it as thus stated which do not actually arise, or should not follow, which do arise. Here, as there, we may have no other reason for accepting a theory than that the facts are inconsistent with any other that we can devise; and then our accument is inductive.

Another reason for the same fact is that for practical purposes it is generally more important to know what means will produce a certain result than by what it has been produced. We cannot alter the root . we may control the future. The means prescribed for the production of a certain result may contain much that is not relevant precisely to the production of that result : and as this irrelevant matter may be different on different occasions, there may he a choice of means. To have a choice of means is undoubtedly useful: but if any of these means is called the cause of the result in question, the term cause is clearly not used in the strict sense: for we may be able to argue forward from the means as cause to the result as effect: but we cannot argue backward from the result as effect to this particular means as cause. Yet this may be of comparatively little consequence, if our interest lies less in being able to determine by which means the result in question was produced on a past occasion, than that it will be produced if such and such means are employed. About a variety of advertised rat-poisons. all that we should care to know would be that they would rid us of rate; and we might endeavour to determine inductively whether a particular poison was efficacious. But we should be indifferent to the fact that other poisons might be equally efficacious, and that rate who died off need not have been killed by this particular poison; in other words, we shall not want to learn the reciprocating cause of the dying off of rats. Indeed as long as the effect is stated in such a general way, a reciprocating cause cannot be given. There are, as Mill observed, many causes of death : and though he was referring to men, it is also true of rats. But death is not altograther the same thing whenever it occurs - and the doctor or the coroner knows this. The many different causes of death do not have altogether the same effects: if you shoot a man and if you behead him the difference in the result is visible : if you role. are an or and if you poison him he is not soundly edible. As soon as we begin to be interested in the particular variety of death now. duced we find the number of causes that produce the result in which we are interested diminish rapidly; if we carried our interest far enough into detail, we might say that for death of a nerticular kind there was only one cause possible. But since much of this detail is quite unimportant, we treat as instances of the same event events which in some respects are different, and then say that the same event has divers causes: forgetting that the differences between these several causes consist partly in irrelevant circumstances, included in our statement because indissolubly bound up with what is relevant, but otherwise superfluous to the production of this event; and partly in circumstances that are represented by differences in the resulting event, only by differences which we ignore. Here then, in the fact that our search is often for means to the production of a phenomenon of a certain general character, to the precise form of which we may be indifferent, is a second reason why the causal relations which we seek to establish are often nonreciprocating. On the other hand, thirdly, there are cases where it concerns us

more to be able to argue from one phenomenon to another as its cause, than from the latter to the presence of the former as effect. For example, there may be alternative symptoms of the same disease: for the effects of the disease may differ to some extent in patients of different age, or east, or race. Here it may be important to show, that if a certain symptom cours, that disease must be present to produce it; while the fact that the disease may exist without giving rise to that symptom is a minor matter, and one which, if we could be certain that some other equally conspicuous and unambiguous symptom would occur instead, might be called altogether unimportant. In such a case we shall be anxious to show a cassal connection between the disease and the symptom in ques-

tion, though again the relation will be non-reciprocating; but it will fail to reciprocate this time, because the so-called cause may exist without the so-called effect, although the so-called effect cannot exist without the so-called cause; whereas in such cases as were considered in the last paragraph, the so-called cause always produced the so-called effect, but the so-called effect might exist without the so-called cause.

Fourthly, our enquiries are often directed to the discovery of the cause or effect of some singular event-singular, not in the sense of unusual but of a single and definite instance : we ask, for example, what has been the effect of the repeal of the corn laws, or what was the cause of a particular railway accident, or epidemic. It is plain that the relation we wish to establish in such cases as these is a non-reciprocating relation. The repeal of the corn laws was a measure introduced into a highly complex social and economic state, and whatever results we can point to depend on much else besides that measure: no one would pretend that the same measure would have produced the same results in other circumstances. It might be possible here to substitute for the question, what effect reneal has produced in the United Kingdom, the more scientific question, in what way corn laws act: the answer to the latter question might be given in the form of one or more universal propositions: but the answer to the former will be a singular indeement. For it is practically impossible to specify all the conditions which have combined with repeal to produce the results in which the influence of repeal is exhibited; so that we cannot hope to establish an universal proposition of the form that repeal of corn laws produces always under such and such conditions the result which we ascribe to it in the case of the United Kingdom since 1846. If a man save therefore that the repeal of the corn laws has increased the population, or depopulated the country, or crippled the ancient Universities, or made inevitable a celibate clergy, he is not to be understood to mean either that it would always produce any one of these effects, or that they must always be due to a repeal of corn laws: but only that in the history of the United Kingdom, had the corn laws remained in force, other things being equal, these effects would not have occurred in the same degree. So also when we enquire the cause of a singular effect: it may be known that the reciprocating cause of small-pox is the presence of a certain

microhe in sufficient strength in the blood but if we sak for the cause of a definite outbreak something else than that is wanted. We want to know what particular precaution has been omitted, by taking which this outhreak might have been prevented; or in what particular way the infection was conveyed to the neighbourhood. Thus we might say that the outbreak was due to a tramp sleeping in a common lodging-house or to insufficient vaccination : but it is not imagined that a tramp suffering from small-nox cannot sleep in any common lode inc-house without an outbreak of small-nox following in the place : or that no such outbreak ever occurs unless from that reason: while insufficient vaccination even if no serious outbreak ever occurred where it could not be alleged may prevail without an outbreak following so long as nothing brings the infection. Similarly in the case of a railway accident, the question is, what particular act or omission that some one is responsible for, or what other unforeseen event, can be alleged, without which on this occasion there would have been no accident : did a signalman give the wrong signal, or pull the wrong points? did an engine-driver disregard a signal? had a flood washed out the ballast of the line, or a fire destroyed a wooden bridge? These and many more are the 'causes' of railway accidents, though railway accidents occur without them. and they may occur without accidents following.

In previous chapters we have represented the phenomena between which it is sought to establish cannal relations by letters of the alphabet. Each of these letters is quite distinct from the rest, insulated as it were, and discontinuous both with those grouped with it to indicate contemporaneous phenomena, and with those placed apart to indicate phenomena preceding or succeeding it; and the use of them as symbols tends to suggest that the course of events is a succession of discontinuous phenomena, which produce each the next in a number of parallel or contemporaneous series. Nothing could be further from the truth: it is impossible to conceive the matter thus. 'We have already noted the ambiguity

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Let nobody object that in such a matter we must ask what experience teaches, and not what it is possible to conceive. Experience can teach nothing inconceivable. All thinking is an attempt to make experience more inchingible, and so far as it is not intelligible, we seeme our account thought the appearances which experience presents. The very search for causal connexious is an example of this operation. It rests on the principle

-the convenient ambiguity-of the term phenomenon : some 'phenomens, which we isolate and individualize by a name do succeed one another: but others do not precede or succeed at all, but and the or persist. Kent said that 'only the permanent can change'. we look on events as occurring to things; permanent things change their states and the permanent thing enters into the earlier and the later state alike or persists through them. What that is which remains unchanged how we are to conceive it, and how we are to conceive the junction between its shiding nature and its changing states-these are very difficult questions. And such deep questions do not belong to the Logic of Inductive Science. But it is clear that our alphabetic symbols fail in the first place to represent the persistence of anything through change; they are discontinuous in their series where they symbolize a change which is continuous. And secondly they are discontinuous within the group that represents contemporaneous phenomena: whereas the contemporaneous phenomena they represent are not similarly insulated from one another. What we commonly speak of as single phenomena are bound together not in independent series unit to successive unit, but by all sorts of cross ramifications, so that each is what it is in consequence of conditions which are at the same time conditioning many others in the most complicated way. To this complication the letters of the alphabet do no justice. Doubtless if we carry our analysis far enough, we may find the a which is the reciprocating cause of a: but a will not in that case as a rule be anything for which we have any single name : a long and carefully guarded statement of conditions will be what it must signify.

The fact is that in most cases the reciprocating cause of anything, if we push our enquiries far enough, emerges as the conditions that constitute it, and not those that precede it and bring it about. The reciprocating cause of small-pox is that activity of a specific

that change is only intelligible if it embodies universal principles of change; to these principles are not presented to our observation. Therefore we believe that events occurred, which have not falles within our experience: as Robisson Orsos, seeing footprints, concluded that men must have been to the island whom he had not seen. And if we deep that the events experienced "we sell that occur, on the ground that their succession would then be without principle and unintelligible, we may equally deep that history can consist of streams of discontinuous erents, even though these succeeded one another according to the most constant rules, on the ground that such a succession would be unintelligible. becilles in the blood in which small-nov consists: the reciproceeting cause of malarial fever is the corresponding activity of another bacillus. But in the procession of events by which that state is brought about there may be one which for one reason or another-it concerns us to single out, and call the cause and that will often be a non-reciprocating cause. It need not be so it is nomible to find an event whose hannening in a given set of conditions or to a given subject always gives rise to some definite new event or state of that subject, and without whose hannening such new event or state of that subject never arises. It is supposed for example that malaria is always communicated to man by the hite of the Anonheles mosquito: there are persons immune to the bacillus, and therefore the bits of Anopheles is still a nonreciprocating cause: but if we knew what state of a subject precluded immunity, then we could say that the bite of Apopheles caused malarial fever in any man in that state, and we should have stated a reciprocating relation; for no man in that state could be bitten without cetting malaria, nor get malaria without being bitten. If with Aristotle we call the conditions which constitute anything the formal cause, and the event whose occurrence brings those conditions into being when they had previously not all of them existed, the efficient cause 1, we may say that the formal cause reciprocates or is commensurate with the phenomenon (as indeed anything must which can in any sense be called the definition of it: and the conditions into which it can be analysed may be called its definition); while the efficient cause seldom reciprocates. The event which provides the conditions, or part of the conditions, constituting the phenomenon, may also be called, in a metaphor of Bacon's using the rehicle of the formal cause; the bite of the Anopheles mosquito is the vehicle of, or conveys, the bacillus in whose activity malarial fever consists; the headsman's axe, or the bullets of the firing party, convey, or are the vehicle of, that bodily state which we call death.

There are indeed many cases where our ignorance of the conditions constitutive of a certain phenomenon compels us to seek

Besides the formal and the efficient, Aristotle distinguished the material cause, or matter of which a thing is made, and the final cause, or purpose of its being. These were all causes in the sense of being necessary to the existence of what they are the cause of. Cf. e.g. Phys. B. ii. 1949 16-195° 3.

instead for some event indignoneshle to its compresses even though our scientific interest would be better satisfied by discovering the constitutive conditions. And there is one most extensive and important class of cases where the reciprocating conditions cannot really be called constitutive of the phenomenon: it is this class of cases which made it necessary at the heginning of the last nameranh to write 'most' and not 'all'. The former sort may be readily exemplified in the biological sciences. That form of barrenness ' writes an authority quoted by Romanes I, 'yery common in some districts, which makes heifers become what are called "bullers"-i.e. irregularly in season, wild, and failing to conceive -is certainly produced by excess of iron in their drinking water. and I suspect also by a deficiency of potash in the soil.' Here we have one and perhans two causes alleged for an effect, whose nature we do not understand sufficiently to see how the causes bring it about, though the facts may prove the connexion. Such a relation may be called discontinuous—i.e. we do not see how the alleged cause, by any intelligible procession of events, passes into the affect. or helps to set up the conditions constitutive of it. We connect one phenomenon as cause with another as effect, where from our ignorance of the intimate nature of the effect, and of the subject in which it is produced, and from the fact that the intervening process of change is withdrawn from view, the two seem quite heterogeneous. In Chicago, one is told, there are machines into which you place a pig at one end, and receive sausages at the other. The pig and the sausages, to any one who has no conception of the nature of the machine and what befalls the pig in it, appear in a relation of sequence without continuity: first the pig exists, and then instead of it, the sausages; but we do not see how the one becomes the other. This somewhat mythical machine may serve to illustrate how our ignorance of the nature of the process of change connecting one event with another may produce apparently discontinuous causal relations; and such relations are often all that we can at present hope to discover; and they are generally, as may easily be understood, non-reciprocating relations. This case is different from that mentioned previously on p. 446; for there it was our practical ends which interested us in causes that were non-reciprocating:

¹ J. W. Crompton: v. Darsoin and after Darsoin, iii. 170.

here it is due to the limitation of our scientific knowledge that we have to acquiesce in them.

But in the extensive and important class of cases to which attention must be called next we find discontinuity even where the causal relation recipercetor viv when the cause is physical and the effect revehical or vice verse. It has already been stated that such connexions furnish one of the best kinds of example of purely industive reasoning because there is nothing in the nature of a particular physical process which would lead us to anticipate the particular nevelical state that we find ourselves led by the facts to connect with it. What may be the true interpretation of this apparent dependence of psychical states on physical processes and physical movements on psychical states, is the hardest question in metaphysics. Meanwhile, at the standpoint at which many sciences and all of us in our ordinary thought are content to stop, we attribute many psychical events to physical causes, and vice versa. In science indeed the attribution of physical effects to psychical causes is less common than that of psychical effects to physical causes; just because between the successive events in the physical order there are prospects of establishing that continuity, which there seems less hope of establishing in any completeness in the psychical series. and none of establishing between members of one series and members of the other, between a motion of matter in the brain and a sensation or thought or feeling or emotion. The series therefore whose members do appear capable of continuous and coherent connexion is often treated as independent, and psychical states regarded as by-products of particular terms in the physical series; although further reflection can easily show that such a statement of the case, when thought out into its consequences, involves us in hopeless contradiction. We are however at present only concerned with the interdependence of physical and psychical states as it appears to exist, and is for many practical purposes rightly treated as existing. It is supposed that to every distinct state of consciousness there

corresponds some distinct state of the body; and this bodily state is not separated from the state of consciousness by any intervening process, the discovery of which might help us to see how one gives rise to the other (as drinking water with an excess of iron in it is separated from the supervening larrenness in a heifer). There is perhaps no interval of time between them, but the completion of the conditions in which the bodily state consists is ∞ isso the production of the corresponding state of consciousness; so that some writers have been led to speak as if the state of consciousness could be analysed into these bodily conditions, and they really constituted it. That because when semaning proves to be propensed.

Yet though in this field we may hope to find relations that reciprocate in spite of the discontinuity between the so-called cause and its effect, there are instances here too where the causal relations are non-reciprocating; and of this perhaps the most notable instance is death. It was explained above, how the many alternative causes of death are not all of them causes of the same effect; because they do not not the body into the same state, although the differences may not concern us. But if we look not to what befalls the hody, but to the result on consciousness-whether we suppose it to be that the soul is separated from the body or that it is destroyed-we can see no difference in that main result corresponding to the difference of the means by which it is produced. If the soul or individual consciousness, be destroyed at death, there is of course nothing any longer in which a corresponding difference can be displayed; if it be not, we may conceive that as the manner of a man's death, if it he not absolutely sudden affects him while he yet lives-one death being more painful, for example, than another -so the differences between one death and another are represented by some difference that persists in the experience of the soul after death, and therefore the effect is not really the same upon the soul when the physical 'cause' is different. But such a suggestion is quite unverifiable; and however that may be, it is well to realize the peculiarity of the relations which we try to establish between physical causes and psychical effects; owing to the heterogeneity of the two terms, we cannot hope to find an intelligible cause of the nevchical state in the conditions constitutive of the physical state with which it is connected: at this point there is discontinuity; and so there may arise an appearance of different causes producing the same effect which we cannot explain as we explained it in a purely physical sequence. There we saw that different series of events might, in their course and as a part of their result. agree in establishing the same complex of conditions constitutive of some particular phenomenon, although the difference in the events occasioned differences in the rest of their result which we ignored. Here, inazmuch as we cannot see that the different causes cetablish conditions that are constitutive of the effect at all, the appearance of the same effect when the causes are different cannot be exhibited as a case where effects different as a whole (in a way corresponding to the difference of the causes) agree so far as concerns the conditions constitutive of the phenomenon we are investigating.

The sum Plavaility of Carees 1 has been used to indicate the fact that the same phenomenon may have different causes on different occasions. We have seen that the fact is more apparent than real: that the alternative 'causes' of a phenomenon, which make up the plurality, are none of them causes in the strictest sense, but rather events which agree so far as the production of the phenomenon requires, though taken as a whole they are very different. It would perhaps be well if there was a term to indicate the corresponding fact, that the same phenomenon may produce different effects on different cocasions: a fact also more apparent than real, for such phenomenon cannot be the cause, in the strictest sense, of any of the alternative effects which it produces. We might speak in this sense of the Diversity of Effects. In neither case do cause and effect reciprocate

Where the cause or effect sought is non-reciprocating, it is obvious that the rules on which the elimination involved in inductive reasoning rests are no longer to be safely trusted. If the same effect may have divers causes, we cannot say that nothing in the absence of which a phenomeno occur can be the cause of it; it cannot be its cause in the particular instance in which it is absent; but it may be on another occasion. If a small group of plants be geographically isolated from the main stock, it will diverge, and in course of time probably give rise to a new species; but there are other ways in which a particular group may be prevented from interbreeding with the main stock (a.g. by flowering at a different season), so that new species may arise in the absence of

¹ The term was introduced by Mill, who sometimes speaks as if he thought the Pirmity of Canses more than an appearance: as if he thought that, in the stricket sense of the term cause, the same phenomenon may have distinguished from the Composition of Canses: which means that a complete phenomenon, which we call now, may be due to a number of cases esting together on one occasion. Clearly none of these is the cause in the full sense, but only part of the cause.

geographical isolation; it would clearly be unsafe to conclude, from the fact that new species had arisen without geographical isolation, that geographical isolation was not a cause of new species arising.

No doubt such an aroument would betray insufficient analysis it would overlook the fact that geographical implation was not a simple factor, but highly complex; and that one feature shout it wiz, that it prevented interpreeding with the rest of the stock-characterized also such very different phenomena as difference of flowering-season, or selective starility. However, our analysis is very commonly incomplete; and then it is possible, that by applying the above rule of eliminating whatever fails to occur in any instance of the effect, we have eliminated the cause altogether : and that if some circumstance is left uneliminated, because it fails to occur in none of the instances of the phenomena, we take it to be the cause of what it has really nothing to do with. If a child were given the same medicine in a variety of issue, and always had a particular biscuit afterwards, it might very likely attribute the effects of the medicine to the hismit. Summer my apple-crop fails four years in succession, and that each year it was 'overlooked' by a woman reputed to have the evil eve : were I to arone that the failure was not due to insufficient rain, since in the first year there was plenty-nor to late frosts, for in the last year there were none-nor to blight, which only occurred once-nor to high winds since the third year was singularly quiet. I might at last attribute the failure of the crop to the 'witch-woman' overlooking it.

In such a situation it is well to test one's results by the second rule, that nothing is the cause of a phenomenon, in the presence of which the phenomenon fails to occur. If the child were frequently given the same biscuit when it had not been doced, it would learn to disconnect the biscuit from the effects of the medicine; and if the witch-woman were observed to overlook my orchard in several years when I subsequently obtained an excellent crop, I might be cured of my superstition. It is however possible that I might still hold her responsible for the bad crops, and apply the doctrine of

^{&#}x27;Or 'physiological isolation'—i.e. that certain members of a species x which happen to exhibit some modification m are more fertile with one another than with the rest of the species in which this modification has not appeared. This would prevent swamping by intercrossing, and so, for breeding purpose, isolate the new variety.

the Diversity of Effects to explain why her action had failed of its previous result on other occasions. Perhaps I might have had the crop blessed by a priest, and attribute to that an effect counteracting the influence of the evil eye; or merely say, that the evil eye cannot be expected always to produce the same results, when there must be many contributory conditions that are varying.

There is no remedy against such arrors except a wider acquaintance with facts and a closer analysis of them, and a better way of conceiving them and their connexions. To this and however very special help is given by emeriment. The results of an experiment are of the same kind with the data of observation-facts namely. with which we have to make our theories consistent: and the inductive reasoning to which the facts contribute premises is not altered in character because the facts are obtained experimentally. But where we can experiment, we can commonly discover facts which observation would never reveal to us. We can introduce a factor into conditions carefully prepared, so that we know more or less accurately what change we make, and in what we make it: and then when we watch the effect, the work of elimination has more grounds to proceed on. If we are in doubt whether to refer some phenomenon to a plurality of causes, or to a single circumstance which, as present in all our instances, they have not so far enabled us to eliminate, we might resolve the doubt by producing this circumstance experimentally: should the phenomenon not follow, we have then shown that, at least in the conditions into which we introduced it, the factor in question will not produce it. We may then try one and another out of the plurality of alleged alternative causes: and if we find each of them producing the phenomenon, we shall conclude that they are causes of it. We shall still probably be far from having discovered its precise cause. without deficiency or superfluity; but we shall have advanced our enquiry. The child who attributed to the biscuit the effects of the medicine could correct its error by experimenting with the biscuit separately, and the medicated jams separately. And if I could bring myself to experiment with the evil eye, I might convince myself that it was innocuous to orchards.

It should be noted that though the Plurality of Causes and the Diversity of Effects render precarious, when our analysis is imperfect,

the application of both the grounds of elimination just cited-viz that nothing is the cause of a phenomenon in the absence of which it occurs, and nothing also, in the presence of which it fails to occurvet the amount of error in which we may be involved is not the same in each case. Should we reject in turn everything, without which the phenomenon is found to occur, we might reject all its several causes, and fall back on something whose presence in the instances we have examined is quite accidental; something altogether immaterial to the phenomenon. On the other hand, should we reject everything, with which the phenomenon is yet found not to occur, though we might be wrong in concluding that what is left is the whole cause of the phenomenon, or that the phenomenon may not have other causes, yet we should be right in concluding that it was not altogether irrelevant to the production of the phenomenon. I give a dog evanide of potassium, and it dies; assuming this to be the only fresh circumstance in the case, I cannot conclude that dogs do not die without taking cyanide of potassium; but I can conclude that taking evanide of potassium contributed something to the death of this dog, and that the conjunction of the two events was not merely accidental, as eating the biscuit was accidental to the child's subsequent experience, or as being 'overlooked by a witch-woman was accidental to the failure of my apple-crop. In the former case, where I reject everything in whose absence the phenomenon occurs. I reject too much: the essential factor lurks undetected each time in a different 'vehicle': each of these 'vehicles' is rejected in turn, and the essential facts rejected with them. In the latter case, where I reject everything in whose presence the phenomenon fails to occur. I may reject both too much and too little-perhaps too much, for what I reject, though insufficient of itself to produce the phenomenon, may contain conditions without which it cannot be produced; perhaps too little. for what is left, while I take it to be essential to the phenomenon. may still contain more than the essential factor that lurks within it : so that other things, in which the same essential factor is contained, may equally serve to produce the phenomenon; vet still I retain something essential, and do not reject everything which I need to retain.

This also is to be considered: that in the loose sense of the term canee which we are now employing, we may either mean

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of the phenomenon (as when we say that atmospheric pressure is the cause of water rising in the common pump, though the production of a vectory by numbing is necessary tool or (ii) something sufficient but superfluors in part to its production (as when we say that the explosion of a powder magazine under the place where he is standing is the cause of a man's death) or (iii) something at once superfluors in part and insufficient but containing an element that is essential (as when we say that the Company Acts are the cause of a new class of fraudulent actions); or where our phenomenon is the failure or destruction of an effect that depends on the fulfilment of a number of conditions, in the absence of any one of which the effect cannot occur. (iv) something sufficient but not essential to such failure or destruction (as when we say that a late and severe frost causes the failure of the fruit crop). Now when by 'cause' we mean (i) something essential but insufficient, it is only part of the real cause: and there must be other factors, also essential but singly insufficient: and it is false to say (1) that nothing in the presence of which the phenomenon fails to occur is its cause in this sense : though it is true to say (2) that nothing in the absence of which it occurs is its cause. Nevertheless when we use the former rule to show that certain circumstances are not the cause, and therefore that what remains is

so, we use it really to show that such circumstances are not sufficient. and that what remains is cesestial: which if we thereupon call the cause of the phenomenon, we mean to emphasize the fact that it is essential, but not necessarily to assert that it is sufficient; and hence, though what we reject or eliminate may have as much right to be called the cause as what we retain and call so (as being also essential though not sufficient), we fall into no error in inferring that what we retain is (or contains) something essential, nor need we fall into the error of supposing that there is nothing essential in what we reject. But when by 'cause' we mean (ii) something sufficient, but in part superfluous, to the production of the phenomenon, then on the contrary it is true to say (1) that nothing is the cause, in the presence of which it fails to occur: but false to sav (2) that nothing is the cause of it, in the absence of which it occurs : if a man could be blown to pieces by the explosion of a powder-magazine without dying, that would not be, in this sense, the cause of his death; but if he may die without being blown to pieces, being blown to pieces may still in this sense be a cause of it. In this sense (ii) of came therefore the second of the above rules or erounds of elimination is false and the first true: while conversely in sense (i), the first is true, and the second false. But when we are enesking of cause in sense (i) the application of what is then the false rule is less misleading than, in sense (ii), is the application of the rule which is false for it. We really argue from the principle that nothing is sufficient in the presence of which the phenomenon fails to occur, to the conclusion that something else is secretial. This principle is true. If the something else is thereupon called the cause, in the sense of being essential though insufficient, yet what is eliminated is denied to be cause, in the sense merely of being insufficient. By means of this discrepancy in the meaning attached to the term 'cause' as applied respectively to what we reject and what we accept, in the case where we wish to establish that one thing is essential to the production of another, though not necessarily sufficient, the rule, that nothing in the presence of which the phenomenon fails to occur is its cause, comes to seem a safer ground of elimination, than the rule, that nothing in the absence of which it occurs is its cause, appears to be. But if the term 'came' is interpreted in both with the same strictness and consistency, there is no justification for discriminating between them.

[J. S. Mill, who make of what he called the Plurality of Caness as the characteristic imperfection of the Method of Agreement. said that the Method of Difference was unaffected by it. Clearly he was wrong. The above argument endeavours to bring out the truth underlying the exaggeration of his statement. That he was wrong may be seen further by help of the following considerations. If a occurs under the circumstances abc, and not under the circumstances bc. I can infer that bc is not sufficient to produce z, and that a contributed to its production on this occasion; but I cannot infer that a could not have been produced without a: plc might equally produce it. That a and p can equally produce a (or equally produce it in bc) is an instance of the Plurality of Causes; and it is the Plurality of Causes therefore which prevents my inferring universally that x is produced by a, or requires a for its production, and limits me to the inference that a produces x, at least in bc. It will be said that a and p must have some common property r, which is the really essential factor. No doubt; but, as we have seen, this is equally the case in any instance of Plurality of Causes; if I

The distinction which Mill draws between the two ' Methode' then is not altogether sound; for the appearance of Plurality of Causes affects the inference which can be drawn in each. But there is this much truth in it, as was pointed out in the text : that in the ' Method of Agreement', where I am eliminating that in the absence of which the phenomenon occurs. I may unwittingly eliminate the essential factor . I throw away the bahy with the bath and am left enprocinc that a is the cause of a when a may really have nothing to do with it, and its presence in each of my instances be a mere accident; in the 'Method of Difference', where I eliminate that in the presence of which the phenomenon fails to occur, though a large part of a may be superfluous to the occurrence of x, yet it is not altogether superfluous; I do not this time connect s with something that has nothing to do with it. But I am unable to infer a reciprocating relation between a and a for the same reason that in the former case I was unable to infer any relation at all-viz. the Plurality of Causes. And let it not be said that this difficulty would not arise. if the conditions of the 'Method' were fulfilled, and a were the only circumstance of difference where a occurred and where it did not. For (i) I should still be unable to infer a reciprocating relation : I could only conclude that a was necessary to the production of a in &: how much of & was also essential I should not yet have discovered. And (ii)—what belongs more particularly to the present contrast-it is equally the case that if a were the only circumstance of agreement in the instances where & does occur, the difficulty would not arise. In both cases, if the analysis of the circumstances were more complete, the Plurality of Causes would Mill seems unconsciously to assume that this analysis is more

complete when we employ his 'Method of Difference' than when we employ his 'Method of Agreement'. The reason of his doing is probably that experiment uses the 'Method of Difference' (or the principle of elimination which it involves), and a completer analysis is generally obtainable when we can experiment than when we are confined to the observation of events as they occur in nature: experiment uses the 'Method of Difference', because in experimenting we introduce or remove some particular factor—and that

funder circumstances which we have endeavoured to ascertain as precisely as possible—and watch the result; and if we are right in assuming these circumstances to remain otherwise unchanged, we do approximate to having only the 'one circumstance of difference' which Mill's canon requires; in other words, we are really eliminating at once and by appeal to a single principle all except this factor removed or introduced by us : though it must not be foreotten that what we eliminate is only shown to be insufficient to the production of the phenomenon, and may still contain conditions that are essential though not sufficient. We may note here the reason why Mill thought the 'Method of Difference' to be of superior corency. The reasoning is clearly no better in it: but it is easier. in the case of this 'Method', to obtain facts of the kind on which corency depends, because it is easier to obtain them by experiment. and this 'Method' is practically a formulation of one of the commonest wave in which we reason from the results of experiment. We may indeed say that the error into which reasoning from an incomplete analysis of the facts may lead us is greater when our ground of elimination is that underlying the 'Method of Agreement' than when it is that underlying the 'Method of Difference' because in the former case we may reject what is essential, and end by attributing the phenomenon under investigation to something whose presence is quite accidental : while in the latter case, we may rather end by supposing that more is essential to it than really is so. Yet there is error in both cases, and for the same reason, viz. our incomplete acquaintance with the facts. What Mill however saw was. that where you can experiment with precision, your acquaintance with the facts is most complete, and hence the conclusions to be drawn most cogent. It is just in these cases that the 'Method of Difference ' as he formulates it is specially applicable; for it requires instances where the phenomenon occurs and where it does not occur with 'only one circumstance of difference'. He overlooked the fact that the reasoning is just the same, where this condition is not fulfilled, so long as your ground of elimination is the same-viz, that nothing in the presence of which the phenomenon fails to occur is its cause; and so he attributed to the 'Method' a superior cogency which really belongs to the 'prerogative' nature of the instances in connexion with which chiefly he considered its use.]

It has been the object of the present chapter in the first place to acknowledge that the 'Rules by which to judge of causes and effects', whereon inductive reasoning depends, are not infallible where we are dealing with non-reciprocating causal relations; for they rest on the assumption that one effect has only one cause, and conversely that the same cause has never any but the same effect; and so they furnish no safe onide to the discovery of ' causes' which are not the only causes of the effect assigned to them, or of effects which are not the only effects that the alleged cance may have Its second object has been to show that such non-reciprocating causal relations arise from the fact of our including in the cause more than is necessary and perhaps also less than is necessary, to the production of the effect; or including in the effect less or more than the cause assigned produces: i.e. our analysis is not perfect: we combine with the matters strictly relevant to one another others irrelevant, but closely bound up with what is relevant : so that there annears to be a Plurality of Causes for the same effect, or a Diversity of Effects for the same cause, while really, if we could 'purify' our statement of the cause and the effect sufficiently, we should see this not to be the case. But we admitted that for many purposes, practical and even scientific, it is causes in the looser sense that we need to discover the sense in which the cause includes more than is material to the production of the effect, in question, but a more from which what is material cannot be dissevered, and so forth. And we saw that science when pushing its investigation beyond such a level as that, tends to substitute for the search, for the determinate cause of some concrete effect, the search for laws or principles in accordance with which things of a certain kind act on one another under specified conditions

In illustrating these points, the rules whose guidance we showed to become unsafe when non-reciprocating relations were in question were the first two of the rules laid down in the Twentieth Chapter. But the last two are also liable to mislead us in such cases. These are, that nothing which is constant when the phenomenon varies, or varies when it is constant, or varies independently of it, is its cause; and that nothing which produces a different effect is its cause. In particular I cannot, because elimination based upon these rules reveals that w is not independent of a in the instances before me, infer that s never occurs without s: for p might do as well. If I find that the faster I run, the hotter I get, and if I know that the temperature of the atmosphere has not altered, and so forth, I may infer that running makes me hot : but not that no one gets hot without running. If I experiment over a series of years with a particular manure, and take care to ascertain by 'controlling' experiments the average crop that I might have expected without its use. I may be led to attribute the excess to the use of the manure: but I cannot conclude that a similarly large crop is always due to the use of it. Errors of that sort would be similar to those which I might commit in applying the mile that nothing is the cause of a phenomenon, in the presence of which it fails to occur. then too I have no right to assume that what I fail to eliminate is altogether necessary, and that nothing else would serve equally instead of it. But the denoer of eliminating too much which besets the amplication of the rule that nothing is the cause of a phenomenon in the sheepes of which it occurs does not equally heret the application of the two rules we are now considering. It is true that in investigating the cause of a phenomenon that may vary in quantity or degree, and is due as a whole to a number of contributory factors, this danger is theoretically possible. The quantity or degree of the phenomenon might remain constant. owing to divers complementary variations in the factors some increasing as others decreased; and because the variations masked one another. I might reject each varying factor in turn, until I had rejected all the contributory factors, as canable of varying with no corresponding variation in the phenomenon. But this is not a probable error. And the fact that the phenomena, to which these rules are applicable are chiefly measurable phenomena is of great importance in the use of them. Peculiar difficulties no doubt often beset us in tracing the influence of some particular factor upon a phenomenon, which varies in magnitude dependently upon the joint action of a large number of conditions independently variable: it is for example exceedingly hard to determine inductively whether the corn-duty of 1902 influenced the price of bread in Great Britain. But these difficulties would obviously be altogether insurmountable if no measurement of the conditions and of their result were possible. The introduction of the element of quantity enables us to determine laws which connect a definite amount of change in one phenomenon with some corresponding amount in another. Where we can do this, we are already getting clear of the errors lurking in non-reciprocating causal relations. It still remains true that we cannot, in virtue of a law which connects with a change in the condition a a corresponding change in the result z, argue backwards from the presence of x to that of a. But that point has been sufficiently exemplified already; and inasmuch as

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some special attention will have to be paid in another connexion 1, when we are dealing with the importance of quantitative methods in induction, to the two rules or principles of elimination last mentioned, it is perhaps unnecessary to say anything further here upon the care that must be used in arguing from them when the causal relations which we have it in mind to establish are non-reciprocatine.

1 Cf. infra, a. xxiv. pp. 516-521.

CHAPTER XXIII

OF EXPLANATION

To explain anything is to show that it follows from something at ready known, or taken as known, or shown by our explanation to be true. Explanation is deductive, for it goes from conditions to their consequences, from principles to that which they involve. We may explain either a particular fact or a general principle. There is no fundamental difference between the two undertakings; but in the explanation of particular facts, particular facts necessarily figure among the conditions to which we appeal. In all explanations, our premises are 'special' or 'proper' or scientific principles. General logical considerations, such as direct us in the inductive search for causal relations, account for nothing in particular; every explanation must be consistent with them, but they will not themselves explain anything. The explanation of the facts or derivative laws of any science rests therefore on a scientific knowledge of the subject-matter of that sciences.

In an earlier chapter it was pointed out that the first or fundamental principles of science are themselves insusceptible of scientific explanation. It does not follow from this that the principles which at any given time are the most ultimate to which a science appeals should be insusceptible of explanation; the Law of Gravitation, for example, is and has long been a fundamental physical principle, but various mathematicians have attempted to show that the behaviour of matter expressed in that law follows necessarily from some more general principles exhibited also in activities whose principles we commonly regard as different, like electricity and light. But the process of explaining must come somewhere to an end, with principles deductible from nothing prior to themselves.

These principles, as was also pointed out, may possibly appear

We may point to facts from which it follows that we must believe a proposition; but we do not thereby explain the proposition. It is the thing believed, and not our believing, which must be shown to follow, if we are to say that we are finding an explanation.

self-evident when we have reached them; the First Law of Motion has often been thought to be a self-evident or necessary truth. But in most cases, they do not; and then all that we can say about them is that nothing so well explains those facts, the study of which has led us to their enunciation. This however is a rise dis-

It has not infrequently been aid that acientific certainty is unattainable. Jevons urges that the conclusions of Induction are only probable at the best. The reason is that the principles which we arrive at as those which explain things are not—at least as a rule—seen to be necessary; and that we cannot absolutely prove that so other principles will explain the facts: just as in simpler inductive enquiries our confidence in the cause which we assign to a phenomenon is qualified by the difficulty of being sure that we have overlooked nothing which might equally, upon the facts examined, be allowed to be the cause.

Jevons indeed suggests 1 that the true though impracticable road to certainty would lie in Complete Enumeration. 'Perfect Induction ' rests on complete enumeration, the 'Imperfect Induction' of actual scientific procedure does not; and in this he sees the source of the 'imperfection' which conclusions only approximately certain possess. But though we may agree with him that many of the conclusions accepted in science fall short of certainty, we cannot agree that they would rank higher if they were reached by complete enumeration : for in that case they would not be universal truths at all, in the proper sense, but only truths about the whole of a limited number of particular facts. Indeed the antithesis of Perfect and Imperfect Induction is an unfortunate one. It belongs to a different sense of the term Induction from that which, in the phrase Imperfect Induction, the term now bears. It is drawn from the completeness and incompleteness of the enumeration of the particulars on which the Induction rests and to which its conclusion refers : we have seen that if a generalization rests merely on citation of particular facts, without any attempt to establish connexions of a causal character by analysis and elimination, the citation should be complete: though in such cases, the conclusion has not the true character of an universal proposition. But the reasoning which infers general truths from the analysis of a limited number of

¹ Elementary Lessons, XXV, 'New Edition,' p. 213: Principles of Science, 2nd ed. pp. 148-152.

particulars does not rely on enumeration and is not an operation of the same kind as that which proceeds by complete enumeration. Though the one therefore may cite every instance, and the other not, yet they are not to be contracted as if they were operations of the same kind differing only in that feature. They are operations of different kinds - and their other differences are more fundamental than the difference in the completeness or incompleteness of the enumeration they involve. If the one is called perfect because its enumeration is complete, it must be remembered that it requires a complete enumeration : but since the other does not require it, it is misleading to call it imperfect for not employing it. The imperfection attaching to the conclusions of inductive science—conclusions which are said to be reached by 'Imperfect Induction'springs from the defective analysis of the instances cited, not from failure to cite every instance; and it is a mistake to suppose that 'Perfect Induction', if it could be employed—as it is acknowledged it cannot-would remove the defect of certainty attaching to scientific generalizations. For science seeks after the necessary and the Iniversal not after the excentionless

However, our present concern is less with the reason for the want of absolute certainty in the principles of scientific explanation, than with the fact itself. It cannot be demied that the first principles of science rest for the most part on no better foundation than this, that no others have been suggested which explain the facts equally well; and this is not the same as saying that no others can be suggested which will do so. And even if we were satisfied that no others could be suggested, i.e. if we could be certain that solding so well explains the facts as the principles to which we appeal in our explanation, yet if we cannot see why these principles need have been what we find them to be, we are still left with something that at once demands to be and cannot be secounted for.

We shall be wise therefore to recognize these two things about scientific explanation at the outset, viz. (i) that it often starts with principles, or truths, or laws, which are neither accounted for nor in themselves self-evident, but only warranted by the success with which they account for the facts of our experience: and (ii) that these principles are not absolutely and irrefragably proved, so long as any others which might equally well account for the facts remain conceivable. But it would be foolish to let these considerations engage us in a general and indiscriminate distruct of scientific principles. Such principles may lack that demonstrable character which we should like them to have; and Logic would abandon its function, if it hesisted, out of respect for the greatness of scientific achievement, to point this out. But they hold the field; we are not entitled to treat them as dogma, which cannot be questioned; but we are entitled to say that so long as they remain unshaken, they should be treated as true.

It may be objected that they are not unabaken; for the fundamental concepts of science are unable to resist metaphysical criticism: the independent existence of matter, the action of one independent thing on another, the production of a conscious state by a process in a physical organism, are all unintelligible. And it must be allowed that the representation of reality which the physical sciences offer cannot be the ultimate truth. But if the provisional nature of its metaphysical assumptions be borne in mind (for science does not really discard, though it sometimes professes contempt for, metaphysics), we may then admit the explanations which it offers within that limits

If however we are to accept those principles which best explain the facts of our experience, we must have some antecedent notion of what a good explanation is. Now it can certainly be required of an explanation that it should be self-consistent. But we are not content with this. There are a number of maxims, which do actually guide us in theorizing about the laws of nature, pointing to some more positive ideal than self-consistency. The influence of these maxims shows that there operates upon scientific minds some notion of what a rational universe should be, as well as a belief that the universe is rational, not derived from experience, but controlling the interpretation of experience. We saw that the principle of the Uniformity of Nature was an 'anticipation' of this kind; but it does not stand alone in that regard. 'The common notion that he who would search out the secrets of nature must humbly wait carperience, botcheint to its slightest hint, is,' it has been said',

¹ Presidential Address at the British Association, Cambridge, 1904, by the Rt. Hon. A. J. Balfour (Times of Aug. 18). He illustrates his stakement by reference to two cases, the permittant belief that the chemical elements will be found to have a common origin, and the permittant refusal to believe in

that partly true. This may be his ordinary attitude: but now and again it hannens that observation and experience are not treated as onides to be meekly followed, but as witnesses to be broken down in cross-examination. Their plain message is dishelieved. and the investigating judge does not pause until a confession in harmony with his preconceived idea has, if possible been wrone from their reluctant evidence.' What these preconceived ideas are. it would be difficult to say precisely: nor is the question of their instification an easy one. They have formed the subject of considerable discussion on the part of philosophical writers since the time at least of Leibniz, who perhaps did most to call attention to them. But one of the most famous has a much higher antiquity. Occam's razor '1-entia non sunt multiplicanda praeter necessitatemis a maxim to which science constantly appeals. It is felt that there is a presumption in favour of theories which require the smallest number of ultimate principles: that there is a presumption in Sevens of the derivation of the chemical elements from some common source or of the reduction of the laws of gravitation. electricity light, and heat to a common basis. Again, we are inclined to believe that the ultimate laws of nature are not only few but simple. The law of gravitation states that the attraction between any two bodies varies inversely as the square of the distance. But it is conceivable that the true relation of the force of attraction to the distance of the bodies between which it acts is not so simple: provided it diverged from the ratio of the inverse square so slightly that the difference would be less than our observation, with the margin of error to which it is liable, could detect. such less simple relation would have as much to be said for it, so far as the facts go, as the simple relation that Newton established. Yet few would seriously consider its claims. It may be said, and truly, that there are sound practical reasons for accepting the simple relation, in preference to any other that has no better claims. because it renders our calculations much easier : yet it may be doubted whether we really repard it as only a more convenient hypothesis. We should regard it as more likely to be true, and this because such a simple relation satisfies better our ideal of explanation. .

action at a distance. It may however be doubted whether this refusal is as well justified as that belief by the maxims in question.
William of Occam, ob. 1847.

J. S. Mill's definition of Laws of Nature has been already quoted— 'the fewest and simplest assumptions, which being granted, the whole existing order of nature would result'.\(^1\) In the words fewest and simplest' are contained perhaps the most important of the preconceived ideas which we have about the explanation of the facts of nature.

It is impossible to reduce explanation to any definite formulae. When nothing but a middle term is wanted, to connect with a subject a predicate empirically found to characterize it, there it will fall into the form of syllogism. But comparatively few explanations can be expressed in a single syllogism. Where, as is commonly the case, they trace the complex result of several principles in some particular combination of circumstances, the building up of this result in thought can never be expressed syllogistically.

As has been said above, there is no fundamental difference between explanation of a particular fact and of a general principle. In the latter case, more abstraction has been performed; we are explaining something exemplified in facts that constantly occur, that has been extricated in thought from varying and irrelevant detail. In the former also, some amount of abstraction must have taken place: but the fact we have thus isolated still retains details that make it unique. An oculist may explain the common fact that shortsighted persons grow longer-sighted as they grow older, by showing how clear vision depends on focusing all the rays proceeding to the eve from each several point precisely upon the surface of the retina : in short-sighted persons, the curvature of the lens of the eve is excessive, and therefore objects have to be nearer than would normally be necessary, in order that the rays proceeding from any point in them may be focused on the retina and not in front of it; but the curvature of the lens is maintained by certain muscles. which relax with age, and therefore as years advance, clear vision of objects is possible at a greater distance. If he were called unon to explain some unique peculiarity of vision in a particular nationt. the task would still be of the same kind; but the facts to be taken into account would partly be facts peculiar to this case, and though their consequences would be traced according to general principles, their special combination would make the complex result unique:

Logic, III. iv. 1. But cf. infra, p. 487, n. 2.

unique however not necessarily, for the same combination might

Historical explanation is largely concerned with events in this sense unique. History has generalizations that admit of evaluation also: but human affairs are so complex, and our interest in them vertends into so much detail, that the unique occupies a onite neculiar share of attention in its investigations. And its task consists largely in making facts intelligible by tracing their development. For an institution or event when we come mon it as it were abruntly may emprise us whereas if we know the nest we may see that its existence or commence connects itself with other facts about the same folk or period in accordance with accepted principles. The institution of primogeniture for example, according to which land descends mon the eldest son, is a neculiar institution. unknown, according to Sir Henry Maine, to the Hellenia, to the Roman, and apparently to the whole Semitic world: neither did the Tentonic races when they spread over Western Europe bring it with them as their ordinary rule of succession. Whence then did it originate? for such institutions do not occur at haphazard. Maine accounts for it as 'a product of tribal leadership in its decay'. Chieftainey is not the same thing as being a landowner: but some of the tribal lands were generally the apparage of chieftaincy. So long as times were warlike, the chieftaincy seems not necessarily to have gone to the eldest son of the deceased chief; but 'wherever some degree of internal peace was maintained during tolerably long periods of time, wherever an approach was made to the formation of societies of the distinctive modern type, wherever military and civil institutions began to group themselves round the central authority of a king, the value of strategical capacity in the humbler chiefs would diminish, and in the smaller brotherhoods the respect for purity of blood would have unchecked play. The most natural object of this respect is he who most directly derives his blood from the last ruler, and thus the eldest son, even though a minor, comes to be preferred in the succession to his uncle; and, in default of sons, the succession may even devolve on a woman. There are not a few indications that the transformation of ideas was gradual'. The custom. Maine thinks, was greatly fixed by Edward I's decision in the controversy between Bruce and Baliol; where the celebrity of the dispute gave force to the precedent. The rule of primogeniture was extended from succession to the lord's demesne to succession to all the setates of the holder of the signory, however acquired, and ultimately applied to all the privileged classes throughout feudalized Europa. In a case like this, a knowledge of past facts enables us to see how a new custom might emerge conformably to known principles of human nature. There are motives for allowing the chieftaincy to devolve upon the eldert son, and motives for conferring it upon the strongest of the near kindred; when the latter are weakened by change of circumstance, the former are likely to prevail. The influence of precedent upon the human mind is also a familiar principle; and though it is impossible to show that in such cases nothing else could have happened (Edward I for example might have decided differently), yet what did happen is shown to follow according to accepted principles from the previous circumstance.

Sciences like Geology or Biology set themselves for the most to solve more generalized problems of development: though to them too some particular fact, apparently in conflict with a theory, may offer occasion for a detailed historical enquiry. But the explanation of the occurrence of crystallized rock, common as it is, is not logically different from what it would be if there were only one place where it occurred; and if we set about accounting for that local and temporal affinity of species which is expressed in Mr. A. B. Wallace's principle that 'Every species has come into existence coincident both in space and time with a pre-existing and closely allied species', we shall not proceed otherwise than if the affinities of one particular historical group of species were to be accounted for.

There are other sciences (e.g. Political Economy or Kinematics) which do not concern themselves with tracing any particular historical development, yet have to explain the laws manifested in a succession of events. Here too it may be of the essence of the explanation to show how one change determines another, and the new fact thus introduced determines a third, and so forth. The laws to which we necessarily appeal may be different laws, and the sequence is explained by resolution into stages, each of which

¹ s. Maine's Early Institutions, pp. 197-205, from which the above example is abridged.

³ Onoted Romanes. Derwin and after Derwin, i. 248.

exhibits a general principle, while the special circumstances in which such a principle is exhibited furnish the occasion for a further change that exemplifies another.

There are comes where the element of time is one of the most important of the facts. Many effects depend upon the juxtaposition of objects in space, and their juxtaposition depends on time-conditions. The fortune of a campaign may be decided by the rapidity of a march, bringing troops upon the field at a critical moment; the troops may fight upon the same principles and with the same degrees of courage all through, but the result is determined by their being there at the time. The working of a machine would be thrown out by anything that delayed or hastened the movement of a part with which other moving parts had to connect; and the same is of course true as regards the articulated movements of an animal. The disintegration of mountains is largely produced by frost succeeding rain: if rain only succeeded frost, it would not take place in the same way. Professor Marshall has called attention, in his Principles of Economics, to the great importance of the element of time in the working of economic laws.1

There are however also many results that are to be accounted for through the concurrent operation of several principles; or rather -for principles cannot in strictness be said themselves to operatethrough the concurrent operation of several causes, each according to its own principle. The path of a projectile at any moment is determined by its own motion, the pull of the earth, and the resistance of the atmosphere. It is true that at every moment these forces are producing a new direction and velocity in the projectile, which forms the basis for an immediate further change : and that it is by following the continuous series of these successive changes that its path is ascertained—a task which the notation of the calculus alone renders possible. The consideration of any term in the series of changes as the resultant of simultaneously operating causes is however different from the consideration of the succession of one resultant change upon another in the series. And the explanation of many problems lies in showing the concurrent operation of different causes, each acting continuously according to its own law; as opposed to the case just considered, where one 1 e.g. Bk. III. c. iv. § 5, 4th ed. p. 184.

cause may produce an effect that, by virtue of the conditions with which its production coincides, then produces a fresh effect in accordance with a different law. The column of mercury in the becometer is maintained according to laws that ere all continuously exemplified and not first one and then enother of them the atmosphere is always exerting pressure, and in the mercury the pressure is always constited in virtue of its nature as a fluid. Economists are familiar with 'Greekam's Law'that had money drives out good i e that if in any country the circulating medium is not of uniform quality the best is always exported and the worst left behind. By heat is meant that whose intrinsic value hears the highest proportion to its nominal value; a sovereign which contains the proper weight of fine gold being better than one containing less. and so forth. The explanation of the Law is simple. Government. can make the bad money legal tender for the payment of debts at home; it cannot compel the foreigner to receive it. For discharging debts abroad the better money is therefore more valuable, for discharging debts at home it is no more valuable than the worse: it is therefore more profitable to export the good. and keep the bad money for home purposes; and the desire of wealth being one of the strongest and most uniform motives in mankind, what is most profitable is naturally done. Nothing turns here upon the resolution of a sequence into stages exhibiting different laws: the derivative law is shown to follow from more general laws, under the special assemblage of circumstances described in saving that the circulating medium in a country is not of uniform quality; but these general laws are exhibited simultaneously and not successively. That the power of any government extends to its own subjects only, and that men desire wealth. are principles more general than Gresham's Law; and both apply to money, which is at once, as legal tender, a matter to which the power of government applies, and, as medium of exchange, the equivalent of wealth.

No logical importance attaches to the distinction between explanations that derive a complex law from simpler laws exemplified together, and those that derive it from simpler laws exemplified successively. Many explanations involve both features. But there is a difference of more importance between either of these, and that form of explanation which consists in showing that laws, hitherto

recorded as distinct, are really one and the same. Newton showed that the familiar fact that heavy bodies fall to the earth, and the equally familiar fact that the planets are retained in their orbits. were really instances of the same principle the coneral Law of Attraction Something of the same sort is done when Romanes brings Natural Selection, and Sexual Selection, and Physiological Selection and Geographical Isolation under the general conception of forms of Isolation preventing free intercrossing among all the members of a species. In cases like these the derivative law is not deduced from seneral more general laws exemplified together or successively in complex circumstances of a particular kind hat a single more general law is shown to be exemplified in a diversity of circumstances which have hitherto concealed its identity. This operation is sometimes called subsumption, as bringing several conceptions under one, in the character of instances or of subjects of which it can be predicated in common. Yet even here it is plain that the operation, of tracing the distinctive peculiarities of the laws explained or subsumed to the special character of the circumstances in which the same more general principle is exhibited, is of the same kind as occurs in all other forms of explanation : only the further synthesis of the consequences of several laws is lacking.

Explanation, as was said at the beginning of the chapter, is eductive—doductive, that is, in respect of the reasoning involved in it. Yet it has a close relation with the work of Induction, and the consideration of this will form the subject of the remainder of the chapter.

Explanation starts, as we have seen, from principles already known, or taken as known; and it shows that the matter to be explained follows as consequence from these. But it is clear that the reasoning which deduces their consequence from them is unaffected by the nature of our grounds for taking them as true. If they were nothing more than hypotheses, we might still argue from them to their consequence as if they were indubitably certain. Just as we may syllogize in the same way from true premisees and from false, so it is in any other kind of reasoning. Moreover, it was pointed out that many at least of the most general and fundamental of our scientific principles are accepted only

¹ Danein and after Danein, vol. iii. c. i.

because they explain the facts of our experience better than any we can conceive in their stead; they are therefore, or were at whe to coated, hypotheses, used in explanation of facts, and proved by their relative success in explaining them. We do not see why they are true, but only why we must believe them to be true. They are established inductively, by the facts which they explain, and the failure of any rival hypothesis; the facts are explained from

It follows that all the deductive reasoning that enters into an explanation enters into the inductive proof of an hypothesis which is shown to explain, and to be the only one that will explain; the facts. And many explanations are put forward, which do not appeal only to principles arrangly known, but have it as their avowed object to prove one or more of the principles which they employ. Explanation then figures as an instrument of induction; and J. S. Mill spoke accordingly of a 'Deductive Method of Induction', and rightly stributed great scientific importance to the process which he called by that name

No better indance of this operation can be given than the familiar instance of the Newtonian theory of gravitation. Sir Issac Newton showed that the movements of the heavens could be explained from two principles or laws—the First Law of Motion, and the Law of Universal Gravitation. The former is, that every body preserves its state of rest or uniform rectilinear motion until it is interfered with by some other body; according to the latter, every particle of matter attracts every other particle with a force that varies directly as the mass and inversely as the square of the distance. The former had already been established by Gailleo, and Newton took it for granted; but the latter he proved for the first time by his use of it in explanation.

The theory which bears the name of Ptolemy, though much older than he, represented the sun, moon, and stars as moving round the earth; and originally it was supposed that they moved in circles with the earth as centre. While the laws of motion were still

¹ I add these words, because it is important to realize that an hypothesis is not really proved by merely explaining the facts. But many hypotheses are provisionally accepted, which are not proved, on the ground facts at the importance of the provision of

undiscovered, no difficulty was found in their circular motion : indeed Aristotle supposed it to be naturally incident to the substance of which the heavenly bodies were composed, that their motion should be circular. for the circle is the perfect figure : movement in a girole is therefore perfect motion; perfect motion belongs naturally to a perfect hody, and the substance of which the heavens are composed—the quista essentia distinct from the four primary substances, earth, air, fire, and water, that are found composing this globe-is perfect.1 The only difficulty arose when it was found that the orbits of the heavenly bodies other than the fixed stars were not perfectly circular; and that was met by the hypothesis of epicycles referred to in an earlier chapter.2 The substitution of the Copernican for the Ptolemaic hypothesis, though involving a reconstruction of the geometric plan of the heavens. did not necessarily involve any new dynamics: Kepler's discovery that the planetary orbits were elliptical was however a severe blow to the traditional theory of epicycles, which had already by that time become highly complicated, in order to make it square with the observed facts. But when the first law of motion had been grasped, it was evident that a planet, if left to itself, would not continue moving in a circle, and returning on its own track, as Aristotle had thought to be natural to it, and as with more or less approximation it actually does; but would continue moving for ever forward with uniform velocity in a straight line. Circular motion, however uniform, was now seen to involve an uniform change of direction for which a dynamical reason was required. And as the planets were constantly changing direction towards the sun, a force exerted from or in the direction of the sun seemed necessary.

Now the greatness of Newton's achievement did not lie in the conception that the orbital motion of the planets was the resultant of two forces, the 'impressed force' (as it is called) which, left to itself, would carry them forward with constant velocity in a straight

According to Aristotle, every lody left to itself had a natural motion, dependent on in own nature: that of the heaves was round a centre, that of early was the centre of the global and so for his view jof the physical university of t

line and a 'centripetal force' which, left to itself, would carry them to the sun. The resolution of curvilinear into rectilinear motions had been accomplished before him, and the hypothesis of an attractive force had already been haverded. It had even heen engreeted that such a force might vary inversely as the somers of the distance: for the area over which it might be conceived as spreading in any plane taken through the centre of the sun varies directly as the square of the distance, and its intensity might be supposed to decrease as the area increased. Neither was it Newton who secertained the facts about the movements of the planets-no small or easy contribution to the solution of the problem. But he did two things. He conceived that the force which deflected the planets into their orbits was the same as that which made bodies fall to the earth; or, to put it differently, he identified celestial attraction with terrestrial gravity, and conceived the earth as continually falling out of a straight nath towards the sun, and the moon towards the earth; and he invented a mathematical calculus by which he could work out what were the theoretical consequences of the principles which he assumed.

Both these steps were of the highest importance. The first provided data to calculate from; the second made the calculation possible. The amount of sceeleration produced per second in near bodies falling to the earth was already known; from that it could be estimated what it ought to be for a body so many times remoter as the moon, or what acceleration a body so many times more massive than the earth as the sun is ought to produce, if once a method of performing the calculation could be devised.

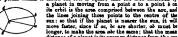
With this method Logic is not concerned. Processes of reasoning are too numerous for Logic to enumerate them all, and those of mathematics are for the mathematician to appraise; it is enough

I Strictly speaking, that acceleration should not be the same at 1,000 feet from the earth and at 100 feet; and in vitros of atmospheric resistance a cricket-ball should not fall as far in a given time as a cannon-ball; but the theoretical differences would be so small as to ecaspe observation, and second for all bodies in the neighbourhood of the earth creates no difficulty. On the other hand, in the occludations of a pendulum, which way in the plains and in the neighbourhood of mountains, we do find orderes agreement to be theory of the same hind as those minute differences would afford the same if it is remembered that a theory, though not proved by its conformity with fact, is disproved by any clearly established unconformity.

if the logician can satisfy himself in general regarding the grounds of mathematical certainty. But assuming the task of deducing from his principles their theoretical consequences to have been performed, we may look at the logical character of the reasoning in which Newton made use of that deduction.

The principal astronomical facts to be accounted for concerned the movements of the earth and other planets round the sun, and the movements of the moon round the earth.1 The former body of facts had been already generalized by Kenler, in his three laws. (i) that the planets move in ellipses round the sun, with the sun in one of the foci: (ii) that they describe equal areas in equal times: (iii) that the cubes of their mean distances vary as the sources of their periodic times. There was also a large body of recorded observations upon the movements and perturbations of the moon: and when Newton first worked out his theory, he found it led him to different results than those actually recorded. He therefore laid it saide; and it was only after several years, when fresh and corrected observations upon the moon's motion were published, that he returned to it. He then found the theoretical results agree with the observed facts; but to show this was not sufficient. He demonstrated further that from any other hypothesis as to rate of variation in the attractive force results followed with which the observed facts conflicted and thus showed not only that his theory might he true but that if the planetary motions were to be accounted for by help of a theory of

Perhaps it should be explained that as a circle is a curre, every point on which is equiditant from a point within it called the centre, so as clipse is a curre, the sum of the distances of every point on which from we points within it called the feet is equal; that the area described by a planet in moving from a point a to a point b on its orbit in the area, and its orbit in the area, sand



during its revolution, and its periodic time the period of the revolution, and its periodic time the period of the revolution, and its periodic time the period of the revolution, as that if the cubes of the mean distance way as the squares of the periodic time the its follows that a planet whose mean distance from the unit in two that of the earth would have a "year" or period or revolution, whose quare was to the earth would have a "year" or period or revolution, whose quare was the its period of revolution would a "y a "the earth a various of one—i.e. that its next of a revolution would a "y a "the earth a various of one—i.e. that

Where the planets are mentioned they may be taken to include the moon, unless the context expressly forbids.
Perhaps it should be explained that as a circle is a curve, every point

attraction at all, the law of that attraction must be as he formulated it 1

The further confirmations which Newton's Law of Universal Gravitation has received from its success in accounting for other physical phenomena, need not detain us: we have to look to the steps involved in its establishment, and they can be sufficiently seen in what has been detailed already. First, there was the idea that the movements of the planets were to be accounted for by reference to two forces acting on them-the impressed force, and the force of attraction . this was not due to Newton Next, it was necessary to determine or conjecture the way in which these two forces severally operated; so far as the impressed force went, that had also been in part already done, and it was expressed in the first law of motion; the actual velocity of each planet was ascertained by calculation from astronomical observations, and the velocity due to the impressed force taken alone was determined by reference to the actual velocity and the velocity acquired by gravitation. But the velocity acquired by gravitation, or through the influence of the attractive force, had to be conjectured; and though the law of its variation had been suggested before, unless the amount of its effect between some given masses at some given distance were known the law of its variation left the matter quite indeterminate. The identification of the attractive force with terrestrial gravity thus completed the necessary data; and principles and facts were now before Newton, sufficient, if a method of calculation were devised, to enable him to determine what should be the consequences of his hypothesis. The next step was the process of calculation. But he had to show, not barely what the consequences of his hypothesis would be, but that they would be the same as the observed facts; and moreover, that his was the only hypothesis 1, whose consequences would be the same as the observed facts.2 The comparison therefore of the facts with the theoretical results of his and of any other hypothesis was the step that succeeded the calculation; and having found that they agreed with his, and with no other, he reasoned thus-Assuming

i. a. if it was to embody a simple ratio: cf. pp. 485-436, 470, supra.

It was possible to show that no other rate of attraction would give results conformable to the facts, because the problem was a mathematical one; and in mathematics it is easier than elsewhere to prove not only that if a is true, by it true, but also the converse.

that the continual defiction of the planets from a rectilinear pash is due to an attractive form, their actual motions, if my statement of the law of attraction is true, would be thus and thus; if it is false, they would be otherwise: but they are thus and thus, and therefore my statement is true.

Now of the stens in this whole logical process, some are not processes of reasoning at all the supported reference of the resultant motions to those two forces the supposted identification of one of the forces with terrestrial gravity, and the comparison of the theoretical results with the observed facts. Resecuing may have been employed in establishing the first law of motion: but that resenting lies ontride the present armeal to it. The reasoning involved in determining the theoretical results of the action of the forces segumed is deductive. But the final argument, in which the agreement of the facts with the results of this hypothesis and of no other is shown to require the acceptance of this hypothesis. is inductive. Had the Law of Gravitation been already proved. we might have said that Newton was merely explaining certain empirical generalizations about the movements of the planets : had it been already proved the disagreement of its consequences with the earlier records of the perturbations of the moon would have led him not to lav saide the theory, but to doubt the observations. or to seeme (as Adams and Leverrier afterwards did for the nerturbations of Uranus) the existence of some other body whose attraction might account for the discrepancy; but insemuch as it was only now proved by its exclusive success in explaining the facts, he was arouing inductively to the proof of it.

If we look for a moment at the simpler inductive arguments which establish the sause of a phenomenon by appeal to 'grounds of elimination', we shall find in them too something of this double character, at once inductive and deductive. The facts appealed to as showing that is it he cause of s are themselves accounted for by that hypothesis. If, for example, facts do not allow us to doubt that makarial ferer is conveyed by the bits of the Anopheles meaquito, then too the power of the Anopheles meaquito to convey malarish ferer accounts for its appearing in persons bitten by that insect. It is impossible but that, if certain facts are the ratio cognoceratio of a causal principle, that principle should be the ratio cognoceration of the facts. But in these simple arguments there is nothing correspond-

ing to the deductive reasoning which works out the joint consequence, in particular circumstances, of the action of two or more causes, from a knowledge (or conjecture) of the effect which each of these causes would produce singly. It is on account of this operation that J. S. Mil gave to reasoning of this kind, even when its primary object was the inductive establishment of a general writing the transport for defencing method of induction.

Such resenting can only be need where the joint effect of several causes is calculable from the laws of their separate effects. Where the joint or complex effect seems totally dissimilar to what any of the senarate effects would be it cannot be calculated from them in anticipation and we rely entirely on the industive method of elimination in order to show that such complex effect is to be attributed to the action of one particular conjunction of causes rather than another, without being able to show a priori that it is the effect they would produce. But into the investigation of any complex effect of the other kind, in which the action of the several causes can be traced as combining to produce it, some measure of this deductive reasoning will always enter. Most obviously is this the case in regard to those complex effects which exemplify what has been called a Aomogeneous intermixture Lie, where the complex phenomenon is quantitative, and there are many factors determining its quantity, some by way of increase and some of decrease. The simpler inductive methods are there quite inadequate : for there need be no two instances of the phenomenon in which its quantity is the same, nor, if there were, need the combination of factors be the same; neither can we infer from the non-occurrence of the phenomenon, or its presence only in an imperceptible degree. where the supposed cause is present, that what we had been inclined

^{1.3.} Mill gave the name of 'homogeneous intermitture of effects' to those cases where the joint effect of several causes acting together is the sum (or difference) of their separate effects, and differs in quantity only and not in quality from the effects which the same cause would produce singly; this happean, e.g., in the mechanical composition of forces—for which reason he spots also of Composition of Causes in such as case. Where the joint effect differs in quality from the separate effects (and so cannot be acknowledge of them he couldn't between the cannot be acknowledge of them he couldn't between the case of the composition. He forms a knowledge of them he couldn't between the case of the compound (unlike its weight) are not homogeneous with those of its constituents, and not dedictible from them; though he equite overlooked the fact that elements were not the 'cause' of a compound in his uses! sense of that term. Cf. Loyir, Ill. vi.

to secribe it to does not produce it: since that cause might be present, but counteracted by another of contrary effect. Even the rule that cause and effect must vary concomitantly and the rule that no such portion of the effect must be attributed to one among the factors making up the cause of the whole, as is already accounted for hy other factors, are not sufficient to ensure success in such enquiries. It is necessary to be able to measure more or less precisely the complex effect, and to know with corresponding precision the amount of effect that the several supposed causes would not duce alone in order to prove that any particular one among them cannot be dispensed with, or rejected from being a part cause. And into this proof a deductive calculation will obviously enter In the fiscal controversy, for example, initiated in Great Britain in 1903 it was alleged that the excess in the value of our imports over that of our exports was due to the crippling of our production by free-trade : but this could only be proved by showing that the difference of value between exports and imports was unaccounted for unless we were living on our capital; and that could not be shown unless the excess in value of imports were ascertained, which was attributable to other causes known to assist in producing their total excess-value—such as the fact that the valuation of our imports was swellen by the inclusion of the cost of carriage to our ports (while our exports, being valued before transport, did not receive this addition): and by the value of the goods that paid for the service which the country performs as ocean-carrier, although nothing appears in the total for exports on that head; and by the value of the goods that represent payment for the use of British capital invested abroad, or pensions charged on the Government of India. The difficulty of determining the amount by which these causes should make our imports exceed our exports in value rendered it exceedingly hard to prove, at least on this line of argument, that we could not be paying out of the year's production for all that we imported in the year.

To sum up—Explanation considered in itself is deductive: it consists in showing that particular known facts, or laws, or general causal connexions, follow from principles already established, in the circumstances of the case; it establishes therefore nothing new, except as it makes understand the reason for that which whe hitherto only known as a fact. But explanation also enters into

induction, so far as the principles, from which the facts, or laws, or general causal connexions, are shown to follow, were not previously cetablished, but are only now confirmed in showing that the actual facts, laws, or causal connexions would follow from them and not from any alternative principles. In such induction there are four main steps distinguishable: (i) conceiving the several agents, or causes, at work; (ii) determining or conjecturing how or according to what law each of them severally would act; (iii) reasoning from these premises to the result which they should produce in common, as well as to the result which they should produce on the common, as well as to the result which would follow on any rival hypothesis as to the agents at work, and the several laws of their operation; (iv) showing by comparison that the facts agree with the results deduced from these, and not with the results deduced from any rival premises.

Many observations might still be made upon this type of aroument-one of the commonest and most important in the sciences. It might be shown how it may be directed to establish either that a particular agent produces a certain kind of effect at all, or how much of that effect, according to its own variations, it produces : or that an agent known to produce an effect of a certain kind is one of the causes contributing to produce that effect on a given occasion. The question may be, what causes can produce such an effect. or which of the causes that can produce it are contributing to produce it now? We may wish to establish a general principle, or only some special fact as to the circumstances that are modifying the results of that principle in the case before us. It is possible too that the laws of the action of the several agents may some of them have been previously ascertained and established, while others are only conjecturally formulated; or, if the question be as to the agents contributing to the result in a particular case or class of cases, the laws of the several actions of them all may have been established previously. But without dwelling on these points, we may conclude the chapter with four considerations.

First, the inductive arguments of science display in every different degree that combination with deductive reasoning which has been now analysed. Thus, though we may represent in symbols the induction whose logical form is a mere disjunctive argument, and contrast it with this into which the deduction of a complax result from several premises so prominently enters, yet in actual practice the contrast is not so sharp; in few inductive investigations is the reasoning merely disjunctive; but the amount of deductive reasoning that has to be performed before one is in a position to apply a disjunction, and to say that this hypothesis is true because the rest can be proved false, varies very greatly in different investications.

Secondly, to show that the facts agree with the consequences of our hypothesis is not to prove it true. To show that is often called registration; and to mistake verification for proof is to commit the fallacy of the consequent 1, the fallacy of thinking that, because if the hypothesis were true, certain facts would follow. therefore, since those facts are found, the hypothesis is true. It is the same mistake as that of incomplete elimination, in the establishment of a simple causal relation : the same as results from overlooking what was called the Plurality of Causes. A theory whose consequences conflict with the facts cannot be true: but so long as there may be more theories than one giving the same consequences, the agreement of the facts with one of them furnishes no ground for choosing between it and the others. Nevertheless in practice we often have to be content with verification; or to take our inability to find any other equally satisfactory theory as equivalent to there being none other. In such matters we must consider what is called the weight of the evidence for a theory that is not riporously proved. But no one has shown how weight of evidence can be mechanically estimated: the wisest men, and hest acquainted with the matter in hand, are oftenest right.

Thirdly, there is no logical difference between the ressoning contained in explanation, and the inductive reasoning that involves replanation, except in one point: that the latter infers the truth of some premise assumed in the explanation from its success in explaining the actual facts and the impossibility of explaining them without assuming it. Where this impossibility is not shown, and we content correleves with verification—that is, with showing that the facts consist with the assumption—there the logical difference is still slighter; it amounts to this, that in explanation the premises are taken as previously known, and in the other case something in

¹ Cf. p. 555, infra.

the premises is taken as not known previously to its use in the explanation.

Fourthly, we may answer here the second of the two questions raised at the end of o. xvii. Demonstration is explanation from principles that are self-evident, or necessarily true. If it be said that in that case very little of what we believe is demonstrated, we must admit it. We can demonstrate little outside mathematics. But we have an ideal of demonstration, and it seems to be that; and it is not necessarily eviloristic, as Aristotle thought it to be.³

³ J. S. Mill, to whose work the above chapter is not a little indebted (*Lopic, III. x-nill), falls to mark sufficiently the difference between showing that the facts agree with a theory, and showing that the theory is true. And the does not bring out clearly enough the relation between what is calls the Deductive Method of Induction (c. ni) and what he calls differ, for how closely they agree, though he gives the same investigation (the Newtonian theory of gravitation) as an example of both of them (ri. 2, iii. 1). Moreover, in readying into three steps the "Deductive Method of the contraction of the contrac

the Explanation of Laws of Nature (c. xiii. He mether notices how they differ, nor how closely they agree, though be gives the man invasigation (the Newtonian theory of gravitation) as an example of both of them (r. i. xiii. 1). However, in renoving into these steps has Detectives Method of a general principle in the steps of the control of the cont

CHAPTER XXIV

OF INDUCTION BY SIMPLE ENUMERATION AND THE ARGUMENT FROM ANALOGY

Tuppe are many reconnings which do not prove their conclusion. It is not merely that we have to use premises of doubtful certainty. for this though it destroys the strictly demonstrative character of our knowledge does not invalidate the reasoning so long as the conclusions are what suset be drawn, if the premises are true. We often draw, and act mon conclusions shout which we cannot say even this much, that they must be true if the premises are. And in so doing, we often find ourselves right: nor, if we refused to do it, could the affairs of life he carried on. Descartes when he set himself to examine all which he had hitherto believed, and to doubt everything which could be doubted determined with himself that he would not let this demand for demonstration in things of the intellect prevent his following the most probable opinion in practical matters.1 But it is not only in practice that we have to hazard an assent to conclusions which our premisees do not strictly justify. Many branches of science would not progress at all, unless we did the same there. In the first place, by committing ourselves to a conclusion, and working upon the assumption that it is true, we may be led to results that will help either to confirm or to overthrow it: whereas if we had merely withheld our assent from any conclusion, because the evidence was inconclusive, we might have remained indefinitely long possessed only of that inconclusive evidence. 'Truth,' said Bacon, 'is more readily elicited from error than from confusion's: and perhaps we might add, than from indecision. Only we must in such cases let our assent be provisional. and hold our opinion not as demonstrated, but as in default of a better. The advice of the politician that a man should make war with another as with one to whom he may be reconciled, and peace

Nov. Org. II. 20.

¹ Discours de la Méthode, Troisième Partie.

as with one with whom he may become at variance, may without spenicion of cynicism be adapted to the assent or dissent with which we receive conclusions that are based on insufficient evidence. But secondly the eciences differ years much in the amount of evidence which they can hope to obtain for their conclusions. A fairly rigorous science may be content to use provisionally principles which are known to be insufficiently proved (and that means really. not proved at all); but some sciences hardly ever obtain rigorous proof of their positions as for example Anthropology and yet much at any rate of their teaching is generally accepted as authoritative. Aristotle said that it was the business of education to teach a man to demand rigorous proof of anything according to the nature of the subject; for it is as foolish to ask demonstration of the orator, as to accept plausibilities from the mathematician 1: and he would have allowed that for this purpose education must include both a training in 'Analytics' and an acquaintance with the different kinds of subject-matter to which one's attitude should he different. It is often said that a man whose studies are too exclusively mathematical is at sea when he comes to deal with matters that do not admit of demonstration : and that contrariwise. if he is trained only in sciences where rigorous proof is impossible. he becomes incompetent to see what is required in matters of a stricter sort.

There are no logical criteria by which to judge the value of such reasonings, unless what is called the Theory of Probability may claim to be such a criterion. But the Theory of Probability is primarily a branch of mathematics; many of the assumptions which underlie its applications are open to suspicion on logical grounds; and its use is at any rate confined to subjects that admit of quantitative treatment. The object of the present chapter however is to considerable arised by two kinds of argument, which while being of this inconclusive character are very common, and have attracted considerable attention from logical writers accordingly.

Induction by Simple Enumeration consists in arguing that what is true of several instances of a kind is true universally

¹ Ελλ. Νέο. α. i. 1094° 23 πεταιδευμένου γάρ δοτω δελ τοσούτον τεαριβέε δευξητέν καθ ξεαστον γένος, όψ δοτω ή τοῦ πράγματος φύσις ἐπιδέχεται παραπλήσιων γάρ φωίνεται μαθηματικού το πιδανολογούντος ἀποδέχεσθαι καὶ ρητορικόν ἀποδείξεις

of that kind. Simple enumeration means more enumeration: and such an argument differs from scientific induction in the absence of any attempt to show that the conclusion drawn is the only conclusion which the facts in the memisses allow while it differs from induction by complete enumeration in that the conclusion is general and refers to more than the instances in the premises. It should however be noted here, that induction by complete enumeration, if the conclusion be understood as a genuinely universal indepenent. and not as an enumerative judgement about all of a limited number of things has the character of induction by simple enumeration. The name of empirical generalization is also given to such arguments by simple enumeration

Bacon's strictures upon this form of reasoning have been already referred to 1 Record it as a form of proof and they are not undeserved. Yet it is still in frequent use, in default of anything better. It has been inferred that all specific characters in plants and animals are useful, or adaptive, because so many have been found to be so. So many 'good meries' have become 'bad species' (i.e. species incanable of any strict delimitation) in the light of an increased knowledge of intermediate forms, that it has been inferred that all species. if we knew their whole history, would do so.2 The familiar generalization that we are all mortal, though not based solely on enumeration, draws some of its force thence. Most men's views of Germans, or Frenchmen, or foreigners generally, rest upon their observation of a few individuals. The 'four peneral rules of geography', that all rivers are in Thessaly, all mountains in Thrace. all cities in Asia Minor, and all islands in the Aegreean Sea, are a caricature of this procedure drawn from the experience of the schoolboy beginning Greek History. The history of the theory of prime numbers furnishes one or two good examples. More than one formula has been found always to give prime numbers up to high values, and was assumed to do so universally: s2+s+41 worked for every value of a till 40: 25"+1 worked for long, but it broke down ultimately.8 It is needless to multiply illustrations.

What is the assumption which underlies arguments of this kind? It is the old assumption that there are universal connexions in

¹ Nos. Org. I. 105. Cf. supra, pp. 852, 864. ² Romanes, Darwin and after Darwin, ii. 282. ³ v. Jevons, Elementary Lessons, pp. 221-222.

*XIV] SIMPLE ENUMERATION AND ANALOGY 491 mature, and the conjunction of attributes which our instances represent to taken as evidence of a connection. The arcuments are weak, because the evidence for the connexion is insufficient. If a Acd instances of the class a present the property a it does not follow that wis connected with those features on account of which they are classed together as a. Yet a large number of instances framishes some presumption. For some reason must exist why all these instances exhibit the same property. If it is not in virtue of their common character at it must be in virtue of some other common feature. When the variety of circumstances is great, under which the instances are found, and the differences many which they present along with their identity as a it is harder to find any other common features than what are included in classing them as z. Therefore our confidence in the generalization increases, although it may still be misplaced. All men are mortal : for if men need not die except through the accident of circumstances that are not involved in being man, is it not strange that no man has avoided

falling in with these circumstances? There is force in the question. The number and variety of our observations on the point are such. that almost everything can be eliminated; almost everything that has befallen a man, except what is involved in being man, has also not befallen other men : who therefore ought not to have died, if it were because of it that men die. Something involved in being man must therefore surely be the cause of dving.

Induction by Simple Enumeration rests then on an implied elimination : but the elimination is half-unconscious, and mostly incomplete; and therefore the conclusion is of very problematic value. But where it is felt that the instances do serve to eliminate a great deal, it is felt that the openings for error are correspondingly reduced in number, and the conclusion is received with greater confidence. General considerations of this kind, however, will not stand against definite opposing facts; therefore such an empirical generalization is at once overthrown by a contradictory instance.1 Neither will they overbear more special considerations drawn from acquaintance with the subject-matter to which the induction belongs. Pigmentation is known to be a highly variable property in many species; therefore the overwhelming range of instances to show that all crows are black was felt to be insufficient to give

¹ Instantia, Ingrane, meant originally a contradictory instance.

the conclusion any high degree of value. Again, a difficulty in conceiving how two properties could be causally connected will incline us to attach less weight to the fact of their conjunction. And contravirsies where the connexion to which the conjunction noints is one which seems conformable with other parts of our knowledge, we are much more ready to generalize from the conjunction. Many general statements are made about the correlation of attributes in plants and animals, which rest on simple enumeration: but the theory of descent suggests an explanation of the constancy of such a conjunction for what was correlated in a common ancestor might well be correlated universally in the descendents. We are therefore readier to suppose that attributes found several times accompanying one another in a species (such as deafness with white fur and blue even in tom-cats, or black colour with immunity to the evil effects of esting the paint-root in nice 1) are correlated universally, even though we can see no direct connexion between them than we should be if no way of explaining the constancy of the conjunction presented itself to us.

The argument from Analogy (at least in the usual sense of the term) is of the same inconclusive character as Induction by Simple Enumeration; and like it, rests on the general belief in universal connexions, and takes a conjunction of attributes as evidence of their connexion.

Analogy meant originally identity of relation. Four terms, when the first stands to the second as the third stands to fourth, were said to be analogous. If the relation is really the same in either case, then what follows from the relation in one case follows from it in the other; provided that it really follows from the relation and from nothing else. Where the terms are quantities, or are considered purely on their quantitative side, and the relations between them are also quantitative, there the ressoning is of course mathematical in character: analogy in mathematics being more commonly called proportion. And such reasoning is necessary, like any other mathematical reasoning. If in respect of weight a: 0: c: d, and if a weighs twice as much as d, then c must weigh twice as much as d, then c must weigh twice as much as d. So soon however as we connect with the relation c: d, on the ground of its identity with the relation a: b, as

¹ s. Darwin, Origin of Species, c. i, 6th ed. p. 9.

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our reasoning ceases to be demonstrative. Suppose that the distance by rail from London to Bristol bears the same relation to the distance from London to Plymouth as the distance from London to Darlington bears to the distance from London to Aberdeen: and that it costs half as much again to send a ton of timber from London to Plymouth as to Bristol; we cannot infer that the rate from London to Aberdeen will be half as much again as it is to Darlington; for the rate need not depend entirely on the relative distance, which all that is alleged to be the same in the two cases.

There are many relations however which are not relations of countity and hold between terms on other grounds. Here too

four terms may stand in an analogy : and what follows from the relation of the first to the second may be inferred to follow from the relation of the third to the fourth. It might be said that the relation of his patients to a doctor is the same as that of his customers to a tradesman, and that therefore as a customer is at liberty to deal at once with rival tradesmen, so a man may nut himself at once in the hands of several doctors. And if the relations were the same, the aroument would be valid, and indeed in principle syllogistic; for the common relation would be a middle term connecting a certain attribute with a man's position towards his doctor. 'Those who employ the services of others for pay are at liberty to employ as many in one service as they pay for ': such might be the general principle elicited from our practice in shopping, and pronosed for application to our practice in the care of our health. The case of patient and doctor is 'subsumed' under the principle supposed to be exhibited in the case of customer and tradesman. Even however if it were not possible to disentangle a general principle, and reason syllogistically from it, we might use the analogy: thinking that there was an identity of relations, and that what is involved in the relation in the one case must be involved in it in the other Unfortunately however the identity of the relations may be doubted. Relations are not independent of their terms. Quantitative

relations are no doubt independent of everything except the quantitative aspect of their terms, and are on that account numally stated as between quantities in the abstract. But with other relations it may be very difficult to abstract, from the concrete nature of the terms between which they hold, the precise features which involve the relation. Hence we may say that two relations are similar, and yet doubt whether they are similar in the way that would justify the inference. They may be partially the same, but the difference may just invalidate the consequence; and reasoning by analogy cannot then possess the character of necessity.

David Hume held that virtue and vice are not attributes of any act or agent, but only feelings which an act may arouse in a spectator: so that if nobody approved or disapproved my actions. they could not be called either virtuous or vicious. And one of the aronments by which he endeavoured to sustain this opinion was as follows. A parricide, he said, is in the same relation to his father as is to the parent tree a young oak, which, springing from an acorn dropped by the parent, grows up and overturns it : we may search as we like, but we shall find no vice in this event : therefore there can be none in the other, where the relations involved are just the same : so that it is not until we look beyond the event to the feelings with which other persons regard it, that we can find the ground for calling it vicions. 1 Doubtless there is an analogy here : but the relations are not altogether the same: for the relation of a parent to a child is spiritual as well as physical, and in the parricide there is an attitude of the will and the affections which cannot be secribed to the oak.

Many arguments from Analogy, in the sense of this loose identify of relations, have become famous; and they are a favourite portion of the orator's resources. How often have not the duties of a colony to the mother-country been deduced from those which a child owes to a parent; the very name of mother-country embodies the analogy. Yet it is by no means easy to find the terms which stand in the same relation. The soil of Britain did not bear the soil of Australia; and the present population of Australia are not the descendants of the present population of Britain, but of their ancestors. To whom then does the Commonwealth over this filial regard, and why? Doubtless the sentiment has value, and therefore some justification; but this argument from analogy will not quite give account of it. Alexis de Tocqueville again said of colonies, that they were like fruit which drops off from the tree when it is ripe.

¹ Cf. infra, pp. 547-549.

^{*} Treatise of Human Nature: Of Morals, Part I. § 1, Green and Grose's ed. vol. ii. p. 248.

Here is enother enclose and two of the terms are the same as in the last. The relation of a colony to the mother-country succreate different comparisons to different minds, and very different consequences which cannot all of them follow from it. We may take another instance, where the relations are really closer, and the argument therefore of more value. To grant that Natural Selection way be able to do all that is claimed for it, and yet object to it on the ground that the facts which are accounted for by it may equally seell be secribed to intelligent design, is, it has been proved as if a man were to admit that the Newtonian theory of the solar system works, and yet were to continue to suppose with Kepler that each planet is enided on its way by a presiding angel: if the latter therefore be irrational, so must the former be 1. Or consider the following passage : - It has been objected to hedonistic svstems that pleasure is a mere abstraction, that no one could experience pleasure as such, but only this or that species of pleasure, and that therefore pleasure is an impossible criterion ' [i. e. it is impossible to judge what is good by the amount of pleasure which it affords). 'It is true that we experience only particular pleasurable states which are partially beterogeneous with one another. But this is no reason why we should be unable to classify them by the amount of a particular abstract element which is in all of them. No ship contains abstract wealth as a cargo. Some have tea, some have butter, some have machinery. But we are quite justified in arranging those ships, should we find it convenient, in an order determined by the extent to which their concrete cargoes possess the abstract attribute of being exchangeable for a number of sovereigns.' The force of this argument will depend on whether the particular concrete pleasurable states do stand to the abstract element of pleasure in the same relation as the concrete cargoes of ships stand to the abstract element of wealth. Doubtless the relatious are partly the same, for each abstract element is an attribute of its concrete subjects. But these are measurable in terms of their attribute, by the fact of being exchangeable for a definite number of sovereigns; and the question is whether there is anvthing that renders the others similarly measurable in terms of

¹ Romanes, Darwin and after Darwin, i. 279.

^{*} M Taggart, Studies in Hegelian Cosmology, § 119.

pleasure. On the value of this argument doctors will probably disagree: and this again shows how arguments from analogy are inconclusive.

There is however another sense in which the terms analogy and

aroument from analogy are used. The analogy may be any resemblance between two things and not merely a resemblance of the relations in which they respectively stand to two other things : and the aroument from analogy an aroument from some degree of resemblance to a further resemblance not an argument from the consequences of a relation in one case to its consequences in another. Expressed symbolically the argument hitherto was of the following type . a is related to b as c is to d: from the relation of a to b such and such a consequence follows, therefore it follows also from the relation of c to d. The present argument will run thus: a resembles \$\delta\$ in certain respects \$\alpha\$: \$\alpha\$ exhibits the character \$\alpha\$, therefore b will exhibit the character walso. Aroument of this type is exceedingly common.1 'Just as the flint and hone weapons of rude races resemble each other much more than they resemble the metal weapons and the artillery of advanced peoples, so,' says Mr. Andrew Lang, 'the mental products, the fairy tales, and myths of rude races have everywhere a strong family resemblance.' 1 It is inferred here that mental products, which resemble certain material products in being the work of rude races will resemble them in the further point of exhibiting the strong family likeness that is known to characterize the latter. Or take this instance from Sir Henry Maine. He is discussing the various devices by which in different systems of law the lack of a son to perform for a man the funeral rites can be supplied. We are familiar with adoption. adoption in England does not carry the legal consequences of legitimate sonship. The Hindu codes recognize adoption and various expedients besides; and the son so obtained has the full status of a real son, can perform satisfactorily the important ceremonies of the funeral rites, and succeed to property as the real son would succeed. One of their expedients is known as the Nivoga. a custom of which the Levirate marriage of the Jews is a particular case. The widow, or even the wife, of a childless man might bear

It was called by Aristotle sapáðesyna: cf. Anal. Pri. β. Exiv, Ehst. a. ii.
 15° 25-36, and p. 501, infra.
 Custom and Math. p. 125, ed. 1901 ('The Silver Library').

We may now compare this with the former type of argument from analogy; and afterwards consider their logical value, and their relation to induction by simple enumeration.

Since analogy properly involves four terms, the latter and looser but commoner sense of the appression argument from analogy seems at first sight difficult to account for. Why should a resemblance which is not a resemblance of relations be called an analogy at all? Perhaps the answer is that where the relation is no longer a quantitative one, it is apt to be regarded as a property of the subject that stands in the relation. The quantitative relation of one thing to another does not affect the intrinsic character of the thing; but other relations do. We should not regard it as constituting a resemblance between a child and a young elephant that one weighed

half a hundredweight, and the other half a ton : but that they both had mothers (though that is also a resemblance of relations) would seem to constitute a resemblance. Such a relation rests on and involves important characters in the thing related of a less purely relational character than quantitative predicates are And in this way the term analogy may well have come to be extended to recemblances generally, even where the resemblance is not a resemblance of relations 1

Even in the stricter sense then the argument from analogy does not commonly mean the mathematical argument from an identity of ratio: the relations are only similar, and must be conceived to involve intrinsic attributes of the things related. In considering the value of the argument therefore we may for the future ignore the distinction pointed out between the two types of inference to which the name is given, and may take the second (to which the first tends to approximate) as fundamental. The argument from analogy is an argument from a certain degree of accertained resemblance between one thing and another (or others) to a further resemblance: because a and b are s, and a is v. . . b is v. What is the logical value of this argument?

It is plainly not proof. As Lotze has pointed out at there is no proof by analogy. Many conclusions drawn in this way are afterwards verified; many are found to be false. Arguments from analogy can often be found pointing to opposite conclusions.

1 I give in a note another possible explanation of the change that has I give in a note another possible explanation of the change that has taken place in the logical use of the term analogy, but one that seems to me less likely than the foregoing. The 'rule of three is in a seems an argument from analogy. Starting with the conception of an analogy, in the strict sense, it supplies from three given terms the fourth term which will complete sems, it supplies from thirse given terms the fourth term which will complied the analogy. It is therefore an argument from the general conception or form of analogy to the actual analogy (or complete terms of the analogy, the property x, and e achibits the bedset the property x, therefore by all also exhibit the property x, and e achibits the bedset the property x, therefore by all also exhibit the property x, and e achibits the confidence of x in a to the presence of x in a to the interpreted thus, it bears less resemblance to the earlier usage than unon

the interpretation in the text.

Metaphysical criticism could easily raise difficulties against the view that relations as such are extrinsic and attributes intrinsic to their subject. But we are concerned here rather with a common way of regarding the matter than with its ultimate tensbility; and I think we do commonly so regard it.

The Parmenides of Plato a dialogue of his later period, diamener various difficulties with regard to the relation between the universal and the particular, which many scholars consider to be criticisms upon his own 'doctrine of ideas' as presented in his earlier writings. One of these is identical with an objection afterwards frequently urged by Aristotle against the Platonic doctrine as he understood it.1 It has been suggested that the dialogue incorporates criticisms which Aristotle had originated as a young man of about 17, when a pupil in the Academy. Are the points Plato's own, or are they borrowed from his pupil? On the one hand it may be said that when he wrote the Parmenides Plato was too old to revise his system. as this interpretation of the dialogue conceives that he was doing : on the other, that at 17 Aristotle was too young to develop criticisms so original and profound.

But Kant's chief works, embodying the system which has made him famous, were written after he was 50; and Berkeley at the age of 20 was entering in his Commonplace-book important and original criticisms of Locke.2 One analogy supports the attribution to Plato, the other that to Aristotle.

If it is not proof, has argument from analogy any value? Can we give any rules by which to judge its value in a given case? Here we must remember that the argument rests altogether on a belief that the conjunction we observe discovers to us a connexion; the presence of both s and s in the subject s points to such a connexion between them as will justify our inferring from s to v in the subject b. If we definitely thought that a and a were irrelevant to one another. it would be foolish to expect b to exhibit one because it exhibited the other. But though the argument thus presumes a connexion between a and s, it makes no pretence of showing that s depends on a rather than on some other property s in s, not shared with a by A. There is no elimination. If however there were any implicit, though not formal, elimination : or again, if there were anything known to us which seemed to support the hypothesis of a connexion between a and y: we should attach more weight to the aroument. Hence if the ascertained resemblance between a and b

¹ It is true that the argument is already found in shorter form in the tenth book of the Republic; Rep. x. 597 C, Parm. 132 D-133 A.
² Cf. D. G. Ritchie, Flate, pp. 108, 120. I have not reproduced the exact use which he makes of the analogies.

is very great, we may think the argument from analogy stronger. For there must be something in a to second for the presence of 4: and if a is not connected with a we must look for that something in the remaining nature of a but the more we include in a (the ascertained resemblance), the less there is that falls outside it, and the fewer therefore the alternatives open to us to account for the presence of win a. Still it must be admitted that so long as we rely merely on this sort of consideration, it remains to the end as possible as not that w is unconnected with w and therefore that s will not be found in a. Of much more weight is the consideration. that the connexion between a and a implied in the argument is one for which our previous knowledge prepares us. The fact that the angle of reflection is equal to the angle of incidence might well be supposed due (as indeed it is) to the propagation of sound in waves: and if so, we should expect the same fact in the case of light to be produced by the same cause.

It will be seen that the considerations which must influence us is determining what weight we are to attach to an argument from analogy are the same as those by which we must estimate the value of an induction by simple enumeration. Both point to a general principle, which if it were true would account for the facts from which we infer it; neither proves its truth; and to try to prove it must be our next business. Mill rightly save that however strong an analogy may be, any competent enquirer will consider it 'as a mere guide-post, pointing out the direction in which more rigorous investigations should be prosecuted. And the same might be said of an empirical generalization. The next sentences from the same passage of Mill's Logic may well be quoted: 'It is in this last respect that considerations of analogy have the highest scientific value. The cases in which analogical evidence affords in itself any very high degree of probability are, as we have observed, only those in which the resemblance is very close and extensive; but there is no analogy, however faint, which may not be of the utmost value in suggesting experiments or observations that may lead to more positive conclusions.' 1

How then does argument from analogy differ from induction by simple enumeration? In the latter, because a number of instances of a class x exhibit the attribute y, we infer that all x are y;

¹ III. xx. 8 med.

in the former, because two particulars a and b agree in certain respects z. we infer that w. which is exhibited by a. will be exhibited by b also. In the latter from the limited extension of an attribute over a clear we infer to its extension over the whole class : in the former, from a partial agreement between two individuals in intension we infer to a further agreement in intension. But the one peece gradually into the other. for the former may be called the application to a particular case of a general principle inferred in the letter from a larger number of instances than in the former. This is very plain in an illustration which Aristotle gives of the 'Example' (his name for the argument from analogy). A man might have inferred that Dionysius of Syracuse designed to make himself tyrant, when he saked the people for a bodyouard: for Pisistratus at Athens asked for a bodyouard, and made himself tyrant when he got it : and likewise Theagenes at Megara. Both these fall under the same general principle, that a man who aims at a tyranny sake for a bodyguard. One of the instances of argument from analogy given above concerned the volatilization of gold: and it might perfectly well be said that it would be contrary to all analogy for gold to be incapable of a gaseous form. But we might equally well say that our experience of other elements warranted the empirical generalization that they could all be volatilized, and therefore gold must be capable of it. This affinity between the two processes of inference is however often concealed by the fact that the points of resemblance in two (or more) subjects.

out the fact of its being an element, as justifying the expectation that it can be volatilized. In the case of Dionysius, his asking for a bodyouard is the circumstance that classes him with Pisistratus and Theapenes, and excites our fear that he aims at a tyranny. But a weatherwise man might be unable to describe what it is in the appearance of the sky that makes him fear a great storm, though 1 Rhet a. ii. 1857b 25-86. To make the inference to Dionysius necessary (it is of course Dionysius I who is meant), the principle would have to be, that a man who sake for a bodygrand sine at a tyranny; and that is really what the supplicious citizen of Byracuse would have had in his mind.

which form the basis of an inference to a further resemblance, have not given rise to any special denomination; there is no general name by which the subjects can be called on the strength of the resemblance, and the resemblance may even be one that we recognize but cannot precisely describe. In the case of gold, we might pick he can say that it was on just such a night as this that some other storm broke out. The general proposition (the induction as some would call it), which mediates his inference from that past occasion to the present, cannot be formulated; and so he may appear to work without it, and the affinity between such a process and induction by simple enumeration may be unobserved. Yet it exists, and, as has been said, the one process passes imperceptibly into the other, as the number of instances increases from which the conclusion is inferred; though where we cannot formulate a general principle, we should certainly speak of the argument rather as one from analogy.

It is of some importance to realize that a general principle is always involved in such an aroument, because it has been contended that all inference goes really from particulars to particulars. There may be psychological processes in which a man's mind passes direct from a to b, and he predicates of the latter what he was predicating of the former, without grounding it on anything recognized to belong to them in common: just as a man who resees a letter-box in the wall may look round at it to see the time. Psychologists explain such actions as due to the 'Association of Ideas". But this has nothing logical about it, and is not inference. Any one must admit when questioned, that unless he supposed & to share with a the conditions on which the presence of a depends he could not rationally infer it in a because he found it in a: and a process which cannot rationally be performed can hardly be called a process of reasoning. But that supposition is the supposition of a general connexion; and therefore inference from particular to particular works through an implicit universal principle.

¹ Mill, Logic, II. iii. 8, and supra, c. xiv, pp. 278-287: cf. also Bradley's criticism, Logic, Bk. II. Pt. ii. a. ii.

CHAPTER XXV

OF MATHEMATICAL PRASONING

MATHEMATICS is frequently and rightly called a deductive science, and for this reason to be fundamentally inductive. There are also certain particular processes of reasoning in mathematics to which the name inductive is more particularly recommendations.

One of these is just induction by complete enumeration, which does occur sometimes in mathematics. A proposition may be proved independently of a right-angled, an obtuse-angled, and an acuteangled triangle, and therefore enunciated of the triangle universally: or of the hyperbola, the parabola, and the ellipse, and therefore enunciated of all conic sections. The formula for the expansion of a hinomial series is proved separately to hold good when the exponent is a positive integer, pegative, and fractional; and only therefore asserted to hold good universally. The peculiar nature of our subject-matter in mathematics enables us to see in each case that no other alternatives are possible within the genus than those which we have considered and therefore we can be sure that our induction is 'perfect'. The nature of our subject-matter further assures us, that it can be by no accident that every species of the genus exhibits the same property; and therefore our conclusion is a comminely universal indomment about the comme and not a mere enumerative indomment about its species. We are sure that a general ground exists, although we have not found the proof by it. This kind of mathematical induction needs no further consideration.

The case is different where some proposition is inferred to hold good universally because it is proved to hold good in one or two instances. This sort of inference occurs in geometry, when we prove something about a particular square, or circle, or triangle, and conclude that it is true of the square, the circle, or the triangle; and again in algebra, when a formula for the

summation or expansion of a series, and such-like, being shown to hold good for certain values of s, is inferred to hold good for any value. The former kind of procedure is too familiar to need illustration; of the latter, the simplest illustration is the proof the formula for the sum of the first a odd numbers—i.e. of the odd numbers, beginning with 1, and taken continuously up to any term that may be chosen. The sum is always s^* ; and this is shown as follows. It is found by addition that the sum of the first three, four, or five odd numbers is 3^* , 4^* , or 5^* ; and then proved that i^* the sum of the first s - 1 odd numbers $s - 1^*$. Like the sum of the first s odd numbers must $s - 1^*$. For the $s - 1^*$ odd numbers $s - 1^*$.

$$1+3+5+7+...+2s-3=s-1^2=s^2-2s+1$$

Add to each side
$$2n-1$$
 (which is the next or n^{th} odd number)

$$1+3+5+7+ + \frac{1}{2n-3}+\frac{1}{2n-1} = n^2-2n+1+2n-1 = n^2$$

If the formula holds for a - 1 places therefore, it holds for a places:
that is, it may always be interred to hold for one place more than
it has been already shown to hold for. But it was found by
addition to hold (say) for 5 places; therefore it holds for 6;
therefore scan for 7, and so on ad infinitions: and therefore

universally.

It is instructive to compare this reasoning with the induction of the inductive sciences. In one respect it presents the same problem, viz. What is our warrant for generalization? Yet it cannot be said that the reasoning is of the same kind.

We saw that in the inductive sciences all generalization rested on the existence of universal connexions—whether we express that as the Law of Canastion, or the Uniformity of Nature, or in some other manner. But the particular problem of any inductive enquiry was to determine what were the conditions with which a determinate phenomenon a was connected universally; and that was only to be done by an exhaustive process of showing with what, upon the evidence of the facts, it was not connected universally, until there was only one alternative left unrejected, which we were therefore bound to accept. Now it is by no such process of elimination as this, that we demonstrate the properties of a figure, or the sum, for any number of terms, of a series. We do not conclude that the angles of a triangle are equal to two right angles,

because we have tried and found that there is nothing else to which they can be equal; but we see, by means of drawing a line through the spex parallel to the base?, that the nature of space necessarily involves that equality. The geometrician sometimes appeals to the conclusion of a previous demonstration, without realizing to himself the reasons for the necessity of that conclusion; thus, for example, in proving that the angle in a semicircle is a right angle be appeals to the fact that the

three angles of the triangle in which it is contained are equal to two right angles, and to the fact that the angles at the base of an isosceles triangle are equal to one another, and shows now only that the angle in the



semicircle must therefore necessarily be could to the other two angles in the triangle in which it is contained. So far as he thus appeals to the conclusion of a previous demonstration, and applies it to the figure before him, he syllogizes; but when he realizes the necessity of that conclusion, he does not syllogize, but sees immediately that it is involved in the truth of other space-relations: and this he finds out by help of drawing the figure. It is felt that a reductio ad absurdum is a defective proof in geometry just because we should be able to show that such and such a proposition is true by direct reference to the conditions which necessitate it, and not indirectly by the refutation of the contradictory. Thus the reasoning proceeds directly from conditions to their consequences?, not as in induction from facts to the only principles with which they cannot be shown to be incompatible. And it proceeds by means of our insight (when we experiment in drawing lines) into the necessary implication of one fact with another in the system of space-relations. For the first reason it is deductive: for the second, its premisses are proper premisees. Dues doyal-geometrical truths which explain other geometrical truths. It is the same with any process of calculation

¹ Or, from the intersection of one side with the base, a line parallel to the other side.
² It is true that in mathematics different truths about the system of spatial or quantitative relations metually condition one another; and therefore the order of demonstration is often indifferent, and condition and consequence may change places. Still the reasoning is deductive, since our premines display to us the rational necessity of the conclusion, and do not leave it resting on a more necessity of inference: of, 401, n. 1, sepro.

in arithmetic or algebra. There too we argue deductively; and there too our premises are proper premises, truths about relations of quantity which render necessary other relations of quantity. Nor is there any special difficulty about the 'mathematical induction' employed in proving the formula for the summation or expansion of a series, &c. When we prove that a formula which holds for s -1 terms holds for a terms, represents any number in just the same way as the circle on a blackboard represents any circle. Geometrical proofs rest on the intuition of quantitative relations, and algebraic on the intuition of quantitative relations, and so far the two sciences differ. But that is not more surprising than the fact that moral philosophy, in which our proofs rest on insight into relations neither of quantity nor space, differs both from scorners and from algebra.

Yet we may return to the question, What warrant have we for generalizing? We must grant that the reasoning by which I prove that the angle in this semicircle ABC is a right angle, or that a formula which holds for the sum of the first sold numbers, is different from that by which I prove connexions of cause and effect in the inductive sciences. Yet why do I conclude that the angle in asy semicircle is a right angle, or that the formula for the sum of the odd numbers, which holds up to the term next to the s -1*, holds up to asy next term, when I have only proved it about this semi-circle, and the series up to the next to the s-1* odd number?

Probably most people's natural impulse would be rather to express surprise at the question than any sense of difficulty in the matter. What difference can it make, they would sak, what direle is taken? What difference can it make that in proving that what holds for so many places of odd numbers holds for one place more, the place you take is represented by s-1? Such counter-questions would be a very proper rejoinder. But it may be useful to see what principles they rest on, firmly grasped but perhaps not consciously formulated.

These principles are, the uniform construction of space, and the uniform construction of the numerical series. It is because space relations are unaffected by locality that what I have seen to be a property of this circle must be a property of any circle; because the difference between one odd number and the next is the same

at every point of the numerical series, that an inference seen to hold from the s-1* to the s* place holds for any value of s. If it were otherwise, I should have to try spaces as I sample cheeses, with no more reason to believe that a property which I had demonstrated of the circle on my blackboard would characterize a circle on the page of this book, than there is to believe that a flavour found in a cheese bought at Bridgwater will characterize a cheese bought at Waterford. So also I should have to try different recions of the numerical series.

But sampling is not altogether an appropriate metaphor; for when I sample a cheese, I generalize about the whole cheese from the piece which I taste; but here I should be unable to perform any generalization. I should examine a circle, or the odd numbers up to 157, to know whether that circle has a right angle subtended at its circumference by the diameter, or whether the sum of that series of numbers was 157. I should not however be able to take that circle as typical of other circles, nor that series of numbers as typical of other circles, nor that series of numbers as typical of other series. For I could have no more reason to transfer my demonstration to a second circle, or a series one place further, than to all circles, and testies up to every place.

In fact our belief in the uniformity of space, and in the uniform formation of the numerical series, stands to mathematical reasoning as our belief in the uniformity of nature stands to inductive. Deny them, and in either case no general proposition remains possible any longer. Nay more: no demonstration remains possible even about a particular case. As we could not even prove that the death of Cleopatra was caused by the poison of an asp, without assuming that it depended on a cause with which such a kind of death is connected universally, but could only say that she died after an asp had bitten her; so we could not prove that the angle in any given semicircle was a right angle, but only say that this semicircle contained a square-looking angle. We rely throughout on universal connexions between qualitatively identical elements. An asp, if it is of the same nature, and bites with the same vehemence a person of the same constitution, must always produce in him the same effect. And a circle, if it is the same figure, must have always the same property; else we cannot even in a single case assign a definite result to a definite cause, or a definite property to a definite subject.

If there is any difficulty in seeing the parallelism, it arises from the fact that a nimle seems obviously the same figure always. Circles differ in size and curvature; and triangles have more differences than circles. But we can easily consider the form of a circle, in abstraction from its size; or the bare triangularity of a triangle, in abstraction from the proportions of its sides or its angles. And when we have in our demonstration proved that some property follows upon the mere form of a circle, and the mere three-sided rectilinearity of a triangle, without taking anything else about either figure into account, we then know that it must be true of all circles, or all triangles. In the inductive sciences our difficulty lies in determining on what conditions. amidst the complexity of the concrete case before us, a particular result depends, and what precisely the result is. It is a difficulty very largely of analysis. No one who had proved that & depended precisely on s in the case before him would heritate to generalize any more than does a geometrician. Indeed he would feel that he was working with general terms all the time, and proving an universal connexion rather than a particular one. But so long as his g and g are not clear-cut and stripped of all irrelevant matter, he cannot trust a generalization. In mathematics our terms are defined and precise from the outset1: our proof shows exactly on what conditions a consequence depends; and we can recognize those conditions elsewhere wherever they occur.

We may sum up this part of our discussion as follows. Mathematical reasoning postulates in space and in number a system exhibiting throughout fixed universal principles, as inductive reasoning postulates it in the course of nature. On that rests the generality of any conclusion in either case. But the nature of the reasoning by which mathematics connects spatial or quantitative conditions with their consequences is quite different from that by which the physical sciences, so far as they are inductive, connect physical condition and consequence. The former works by direct insight into the special nature of its doubtless highly abstract

Speaking generally: but of course we may sensitime fail at first to discover the truly commensaries subject of a prodicate, as if one were to prove that the external angles of a sense were sequal to four right angles, when it is true for any recillimer figure. Here the number of cides, and the magnitude of the internal angles, would be falsely included among the conditions on which the preparty depends.

subject-matter; the latter has no such insight, but looks for terms that, in face of the facts, will alone satisfy the general conditions of a causal connexion. In the former, generalization is unnoticed because it is all-pervading; for the relevant conditions are distinguished from the first. In the latter, generalization comes at the end, and structs attention as the result of a long effort; for all our task is to distinguished he pelevant from the irrelevant conditions.

There remains one question which was referred to at the outset of the chanter. The principles of mathematics have been alleged to be generalizations from experience, and the science on that account at bottom inductive. It is indeed difficult to see why the same should not as well be said of the inferences in mathematics. Their demonstrative force arises from the fact that the nature of space or quantity allows us to see immediately the consequences involved in certain conditions. But any one who requires repeated experience to convince him of the truth of a geometrical principle (such as that two straight lines cannot enclose a space) may just as well require repeated experience to convince him of the truth of a geometrical deduction: we have to do with the mutual implication of spatial conditions in both cases. And so it is also in the science of pure quantity. The multiplication table up to 12 x 12 might be said to contain principles, and the multiplication of 266 x 566 to apply them: but whatever reason there is to doubt that $6 \times 6 = 36$, there will be the same reason to doubt whether it follows that 60 v 60 -3600. However, it will be sufficient if we confine ourselves to the consideration of the alleged inductive character of the process by which we ascertain mathematical principles, without attempting to determine how much would have to be regarded as principles, and how much as valid consequence.

What is really meant by the allegation is, that whereas every mathematical principle, such as the axiom of parallels, or 2 + 2 = 4, is universal, our reason for accepting it as universally true lies in the fact that we have always found it to hold good in experience. Two apples and two apples make four apple; it is the same with cows or sovereigns, window-panes or waterpots. And whenever we have seen a straight line failing on two other straight lines and making the alternate opposite angles measurably equal, we have found—if

Mill, Logic, II. v-vii. Cf. Autobiography, p. 226.
 Or for that matter, of any form of inference.

[·] Or for that matter, or any form of interestor

we have tried—that however far we produced the two other straight lines, so long as they continued apparently straight, they remained at the same measurable distance from one another. All experience confirms these principles, and none is contrary to them; so we accept them as empirical generalizations, possessing, on account of the extent and variety of the circumstances under which they have been found to hold good, the same degree of certainty as if they had been proved by a rigorous elimination of all other hypotheses.

It is really sufficient answer to this view, to recur to what was said man a similar attempt to treat the Law of Canastion as empirically established. If the Law of Causation is true, the facts of our experience help us to determine what are the particular causal connexions in nature : if we start by doubting it, the facts will never bring us any nearer the proof of it. Similarly if we start by doubting whether enatial or numerical relations are constant, the facts will never begin to prove it. Grant that the sum of 2+2 is always the same, and it is worth while to see what it is: and whatever countable things we take to reckon with will make no difference. But question whether it is always the same, and proof that it is so becomes impossible. For you have no ground for supposing that if 2 + 2 could sometimes make 5, cases of its occurrence would have occurred in your experience. Everything becomes problematical: the frequency of any particular sum of 2+2 is quite indeterminate, if the sum is indeterminate; and your experience may assure you that you have never found them making anything else than 4, but cannot assure you that you are never likely to do so. And so it is with geometrical principles also. If geometrical relations are not necessary and universal, we have nothing but a conjunction of facts empirically ascertained. In each place and time the conjunction may be different: there is no reason to suppose that what occurs here and now conveys any instruction about the occurrences at other times and places. If each place and time is loose and independent, the next may always contradict even the uniform results of previous experience.

Other lines of refutation are also possible. It might be pointed out that in point of fact we do not look for confirmation of our principles to repeated experience; but we interpret experience in the light of our principles. Two drops of quicksliver; + two drops of quicksliver; but we insist that

the four drops are there, in a new figure. The angles between the end-lines and the side-lines of a tennia-court may seem each to a right angle, and the sides to be drawn straight; but if we find that one end-line is shorter than the other, we say that we know that the angles cannot be true. It may be said that by this time our principles are well established, and facts in apparent conflict with them are therefore reinterpreted so as to be consistent with them. But facts in apparent conflict must have been frequent from the beginning. Again, it is hard to see what meaning can really be attached to the statement that 2+2 might conceivably make 5, or that lines making equal angles with a third straight line might conceivably remain straight and yet converge; for such a thine cannot be represented to thought as possible.

It is of course true that in the application of mathematical reasoning to what is concrete, our conclusions will only be true if our premises were so. If a wheel which I assume to be circular is not circular, conclusions based on the assumption will prove false. If I am wrong in my linear measurement of a floor, I shall be wrong as to the number of square feet of floor-cloth required to cover it. But that does not shake the certainty and universality of mathematics; indeed nothing else would consist therewith.

It is also true that without experience of counting numerable objects, and of constructing figures in space, I should be unable to apprehend or understand the truth of mathematical principles. But this does not make their truth empirical, or my mode of ascertaining it inductive. For those principles are seen to be intrinsically necessary as soon as they are understood; whereas inductive, conclusions are never seen to be intrinsically necessary, but only to be unavoidable. Nor does further experience add anything to our assurance, when we have once made the construction or the calculation in which their truth becomes manifest to us; whereas further experience of the same conjunction amidst variation of circumstance is precisely what does add to our assurance of the truth of an empirical generalization ¹.

We must conclude that in mathematics there is (or at least should be ') no generalization from experience. To suppose mathematical principles to be such generalizations is like supposing the Law of Canastion to be so. Their universality is the counterpart to the reign

¹ Cf. p. 491, supra.

⁸ Cf. p. 490, more.

of law in physical nature. But the deductive character of mathematical science is due to the nature of the subject-matter, and our peculiar insight into the rational connexion of its parts. What is implied in our possession of this insight is a metaphysical question beyond our nurriew.

The nature of mathematical certainty is a question of farreaching metaphysical importance; and J. S. Mill. in his Autobiography (loc. cit.), frankly acknowledges that the chief strength of the opposition to the truth of the Empirical Philosophy had always seemed to lie here. It was on this account that he sought to show that mathematical principles in their turn were generalizations from experience. He held the same with regard to logical principles. It is logically important to see that there can be no knowledge unless there are truths not empirical-i.e. not open questions, for a decision on which we must go to the tribunal of sense-perception or events. And no one will understand the structure of knowledge, who does not see that mathematical principles are truths of this kind. But it may be asked what their relation is to logical principles. There are some who have represented logic as at bottom a branch of mathematics; and others seem inclined to suppose that mathematics can be reduced to formal logic. A non-mathematician is not well fitted to discuss these matters in print; and the discussion belongs in any case to a more advanced stage of logical science than this book pretends to attain. But I ought perhaps to say that I do not understand how either theory can be true.

CHAPTER XXVI

OF THE METHODOLOGY OF THE SCIENCES

WE have seen that inferences cannot all he reduced to a small number of fixed types. They are not all syllogistic, not even all that are deductive. Their form is not altogether independent of their matter. All inference, according to Mr. F. H. Bradley, is a construction and an intuition.1 The putting together of the premisses is the construction, but it is the terms which determine how it can be effected. The perception of something new to us in the whole which we have constructed is the intuition : and if we do not see its necessity, there is no help for us. But within the unity of this definition, we may examine any particular type of inference which. for its frequency or importance, seems to demand our special atten-Syllogism is one of these types: the disjunctive argument as applied to establish causal connexion is another. The relation of subject and predicate is one of the commonest which our thought uses, and therefore inferences based on it are common. The cancel relation is not less important, and the type of inference used in its establishment equally deserved our study.

We found that this type of inference rested on the conception or definition of cause. We considered very generally what that conception involved, and how we could satisf ourselves that we were right in bringing any particular facts under the conception. We noticed some of the difficulties which the complexity of nature places in our way; and some of the cautions which we must constantly bear in mind in interpreting facts in accordance with the conception. We found that general truths present themselves to the mind at first in the form of conjecture or by notbests; and that

Principles of Logic, p. 235. 'The process is a construction and the result an intuition, while the union of both is logical demonstration.'
Not that all disjunctive argument involves that conception; but only disjunctive argument applied to the discovery of causea.

often there is no means of testing such hypothesis except by first deducing—it may be by very elaborate reasonings—the consequences that should follow in specified circumstances if it were true and if it were not. But all these matters were discussed and illustrated in a very centeral way.

Now different enquiries have their own peculiar difficulties, arising out of the nature of their subject-matter, and of the problem which they set. And any rules for dealing with these peculiar difficulties will constitute rules of method, instructing us how set about the task of singling out the laws or causal connexions from amidet the particular tangle in which the facts are presented in such science. The consideration of such rules, as distinct from the use of them, is Methodology; and so far as herein we consider how certain general logical requirements are to be satisfied in a particular case, it is sometimes called Appicia Logica!

To this subject belongs Mill's discussion of the proper method of studying the moral or social sciences 2. He points out how methods of enquiry appropriate to certain chemical investigations (to which he therefore gives the name of the Chemical Method) are inapplicable in dealing with the sciences of human nature. The chemist, unable in a great degree to predict from his knowledge of the properties of elements the properties which will belong to their compounds, has to proceed by experiment conducted with every precaution to secure a precise knowledge of the conditions: and thus discovers the effect of a new condition or ingredient upon a whole of a certain kind. But we cannot experiment with society out of a merely speculative curiosity; the practical interests involved are too great; and were that not so, the thing is impossible. Our material is not under control; it would be most instructive to prevent the use of alcohol in England for a generation and watch the difference in the amount of pauperism and crime; but there is no means of performing the experiment, for to pass a law is not to enforce it. Nor can we ever know precisely into what conditions we introduce the factor whose effects we wish to study; nor can we maintain those conditions unchanged in all but what is due to the influence of that factor during the course of

¹ Cf. Kant, Introduction to Logic, ii. 4(T. K. Abbott's tr., p. 8), who gives a different sense to the term, but notices this use of it.

Logic, VI. vii-x.

our experiment. For these and other reasons it is honeless to expect much light to be thrown upon the laws of social phenomena. merely by watching what follows in different cases upon the adoption of the same policy, or by comparing the results of different policies. There are so many factors which modify one another: each effect depends on so many conditions, and each condition by its presence or absence makes a difference to so many effects by us regarded as distinct, that it is useless to suppose the effect of any particular social experiment will stand out sharp and recognizable amidst its surroundings, or that we could say-Here is something which could not have occurred but for the measure

We must have recourse then to deduction. From what we know of the laws of human nature, we must attempt to determine the effect which a measure must produce, or the conditions out of which a given state of society must have arisen. But again the great complexity of the subject imposes certain restrictions upon us. We must not expect to be able to trace any pervading feature of society to a single motive as political obedience to fear, or good government to a system by which the ruler's private interest is encaged in governing well. And Mill lave stress on one feature in particular of the method by which the course of human history is to be explained. Instead of working out first the theoretical consequences of certain general principles, and then checking ourselves by comparing our result with the facts, he holds that we should endeavour first to ascertain empirically the subordinate principles that manifest themselves in history, and check our formulation of them by considering whether they are consistent with the more ultimate laws of human nature and conduct from which in the last resort they must be derivable. For the facts of every period are so diverse and manifold, that the former procedure would probably be a waste of time. We may know the laws of human nature, but until we know the circumstances of a given state of society, we cannot tell what result these laws will produce. We never know them sufficiently for it to be worth our while to attempt to develop human history a priori, as the astronomer might attempt to develop a priori the course of a comet or of the tides. We must be content to confirm such generalizations as we can frame a posteriori by showing that they present nothing surprising Ll2

when they have happened, although we might have been unable to predict them.

In the chapter on Non-reciprocating Cansal Relations, questions of methodology were really to some extent discussed. For we were engaged in considering the difference between the evidence required to establish a pure causal relation, where nothing irrelevant enters into the statement either of the canse or of the effect, and a non-reciprocating relation such as is implied when we speak of a Plurality of Canses. Now some sciences find it much harder than others to eliminate the irrelevant; and to them it is specially important to remember the sort of tests by which the non-reciprocating character of a relation may be detected.

In that chapter, two of the 'Rules by which to judge of Causes and Effects' which had been previously enunciated were reconsidered at some length, and it was shown that, although nothing which failed to satisfy their conditions could be in the strict sense the cause of any phenomenon, yet if cause were understood in a looser sense, as non-reciprocating, it was not safe to make the same assertion. But of the precautions to be attended to in the application of the other two Rules little was mid.

These rules were, that nothing which varies when a phenomenon is constant, or is constant when it varies, or varied independently of it, is its cause; and that nothing is so whose effect has already been taken account of in other phenomena. Both these rules are especially useful where we are dealing with mecsurable effects, the total amount of which is dependent on a large number of conditions; and the investigations which employ them have been called 'Methods of Quantitative Induction's' It may be worth while to consider some of the difficulties which beset the use of them; and that will furnish an example of a methodological problem; for a science which deals with measurable phenomena, in spite of the great advantage which their measurability brings, generally meets also with some special difficulties, which it needs particular precautionary measures to surmount.

What is measurable must so far be homogeneous. Sometimes

Mill gives to this order of procedure the name of the 'Inverse Deductive, or Historical Method': by which he means the method appropriate to the study of history. The Historical Method now however commonly means interpreting present facts in the light of their past history.

1 Jerons, Elementary Learns in Logic, XXIX.

Now contributions may be made from many sources to any homegeneous quantity, but when you are merely told what the quantity is, there is nothing to show of how many parcels, so to say, it is made up. The total quantity is a sort of unity. Had one parcel fluctuate in amount, the total fluctuates; but there is nothing to show which parcel is fluctuating and which is constant, and the variation seems to belong to the whole.

It follows that where an effect is quantitative, and there are a number of contributory factors which, one way or the other, influence its amount, fluctuations in these do not necessarily stand out in the result. There is no doubt that overcrowding affects the death-rate; by the death-rate in a town may rise while overcrowding has diminished, if other causes operate to increase it faster than the improvement in housing constate to diminish it.

Hence a hasty application of the rule that nothing is the cause of a varying phenomenon which does not vary proportionately with tim ay lead us into grave mistakes. We might suppose, for instance, in the last example, that overcrowding had no influence on the death-rate, because the death-rate seemed to rise and fall independently. Doubtless it is only seeming; and if the other contributory factors could be kept constant, we should find the rise and fall proportionate. But we cannot keep them constant.

And even if we could we should be exposed to other ermrs of interpretation. The death-rate many as are the causes which contribute to it is yet measured as a whole, and treated as one phenomenon. If all the causes which contribute to it were constant except one, and that one fluctuated, the whole result might be attributed to the one circumstance which exhibited proportional fluctuations with it. In this particular matter, indeed, we know too much to fall into such an error: we know that overcrowding is not the only cause of death. But where our previous knowledge is less it is very easy to attribute the whole of a varying effect to the factor which varies in proportion, instead of only attributing in to the increase or decrease beyond a fixed amount. The influence of education upon character is great; and that is shown by the effects of giving and withholding it. But we cannot thence infer that it is all-nowerful or that the whole difference between the criminal and the good citizen and father is due to comparative defects in the criminal's upbringing.1

It is clear, then, in the case of a fluctuating effect which is the complex result of several causes, that though there must no doub be a proportionate Suctuation (or constancy) in the cause, yet it is unasfe to reject from being a cause either a factor which fluctuates when the effect is constant, or one which is constant when the effect fluctuates. For we see the effect as a whole; and the whole need exhibit no fluctuations proportionate to those of any one part. The rule of elimination is not false; and if the separate effects of each factor were not tost and undistinguished in the total, we should observe the facts conforming to it. But this not being so, the rule is neaff.

The best remedy lies in determining the precise amount of effect which each factor can produce; and as each factor may perhaps be liable to fluctuation, what we need is a principle or law connecting each degree of its activity with a corresponding quantity of the effect. This is done, for example, in the Law of Gravitation. And could we thus calculate the amount of effect which the other causes at work, at the strength at which they were severally present, we capable of producing, we might then safely attribute any difference

¹ The 'Perfectibilitariane', like Godwin, at the beginning of the last century, held very nearly this.

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beyond this to some circumstance that fluctuated proportionately with it.

But in such a procedure we should no longer be appealing merely to the principle that the cause of a varying phenomenon must be something that varies in proportion. We should be invoking also the fourth of our grounds of elimination, that it can be nothing whose effect is already accounted for. Only because we have determined the amount of effect which the other factors can produce are we entitled to say that the residue is in no part due to them. And unless we know with fair accuracy what amount of effect may be justly sastigned to other factors present, we cannot upon the strength of this principle attribute any part to some particular further factor a. The application of this rule therefore is involved in the same difficulties as that of the former, through the fact that the effects of many different causes are compounded and lost in one total aromat.

Moreover, so long as all these causes are freely varying, and masking their separate effects in one total, the determination of the law of any single cause, much as it would help us to discover the others, is the very thing that is so difficult. Hence the necessity of experimenting with each suspected cause singly. It may be impossible to exclude the influence of any others : we must endeavour to keep it constant; or we may employ what is called a controlling experiment at the same time. We may see what happens both when a certain factor is introduced, and when it is not, under circumstances which, though we cannot keep them constant, we have good reason to believe to be the same in either case. A farmer, for example, wishes to know whether some new dressing is of any use to his grass. He cannot remove the other causes which promote or hinder the growth of grass, and see how large a crop of hay this dressing could produce alone : for alone it would produce none at all. Neither can he control those other causes, so as upon the same field to use it one year and not the next, and maintain all other factors the same. But he can select two plots, or series of plots, on which he has reason to believe that the other causes all operate equally. and use the dressing on one and not on the other. But even so, we have not got a great way towards determining

But even so, we have not got a great way towards determining the less of a cause. To show through all that masks it that some part of an effect is due to a particular cause is not the same as showing how much is due to it: still less as finding a mathematical expression that connects definite fluctuations in the one with definite fluctuations in the other. There are many cases where this last achievement is impossible even though the phenomena we study he quantitative and to some degree measurable: indeed it is impossible except in dealing with the physical properties of hodies Eleawhere we must be content with a vacue much and little. In time of war the risk of canture at sea is a great deterrent to neutral commerce - but we cannot may precisely how great. The history of times of places shows that increased uncertainty of life relaxes the hands of costom and morality; but it would be impossible to give any measure of the connexion between the two facts, though the measurability of the facts in the sense that as the death-rate rises the frequency of criminal or reckless acts increases, enables us to establish the connexion. The one fact may be, in mathematical rarlance, a function of the other: but it is not a function of the other alone: and we cannot so disentangle the many causes and their complex result as to give precision to the degree in which one affects the other. Moreover, where the phenomena are more purely quantitative, the law of variation that connects them is by no means easy to establish . for a formula which holds good over a considerable rance of variation may break down beyond those limits. The coefficient of expansion of a metal, which indicates the rate at which its bulk increases with successive increments of heat, no longer applies when the metal vaporizes. There are what have been called critical points, at which the change in an effect no longer observes the same proportion as hitherto to the change in the cause. Great caution must therefore be observed in formulating any law upon the evidence of concomitant variation between two phenomena. even where we are satisfied that we have excluded any variation due to other causes, and can give a precise measure of the phenomena in question.

The causes whose effects are merged in a total may not only vary independently of one another; some may be intermittent in their operation. And whether they are continuous or intermittent, they may be periodic; and one may have a longer period than another. There may again be causes which are both intermittent and irregular in their action, recurring at no definite and periodic intervals. Yet it is possible to cope with many of the difficulties which these

facts present by taking averages. No one would expect the rainfall of one year to agree closely with that of another in the same locality: the circumstances affecting it are too numerous and inconstant. But we have no research to expect that the everage annual rainfall over a considerable period of years should not agree closely for different periods; for though in one year there may be more circumstances that are favourable to rain than in another. in the next it may be the other way. If then the average rainfall for one considerable period of years were greater than for another we should look for some definite reason for the difference : which we might find perhaps in a difference in the amount of forest standing in the district at the different dates: for the intermittent and irregular causes of whose operation we are aware would have roughly balanced in the two periods, though not perhaps in any two single years. Another method is to plot curves. A base line for example is taken, and perpendiculars drawn to it at equal intervals for the successive years. On each of these a point is taken whose height above the base is greater or less in proportion to the number of inches of rainfall in that year; and a line is drawn through those points. The line will rise and fall irregularly; but it is possible that in spite of these intermediate fluctuations there may be long-period fluctuations which stand clearly out: what may be called the create and troughs of the curve may be at fairly equal intervals, though its course is not uniform from trough to crest. This would indicate the action of some cause having a similar period : and if we discovered any factor with a corresponding period of fluctuation, there would be a strong presumption that it was the 001100

The profitable use of statistics depends vary largely on methods like these; but the devices for bringing out their teaching are often much more elaborate than has been indicated. They belong, however, to the detail of particular sciences rather than to the general principles of logical method. Enough perhaps has been said to indicate the misinterpretations of causal relation to which we might be led, in the case of quantitative phenomena that vary in their amount, by too hastily applying rules true in themselves to any unanalysed total effect: as well as the difficulties that beset us in disentangling the component parts and fluctuations.

A few further and miscellaneous examples of the way in which

precepts for the better prosecution of a particular science may be drawn from general logical principles will serve to conclude this chapter. It must not be supposed that the subject is at all adequately treated here; it is only illustrated.

What is called the Aistorical or compensative method has in the last few generations revolutionized many branches of enquiry. It is but an application of the general principle of varying the circumstances in order the better to discover the cause of a phenomenon. But of old, enquirers into matters of historic growth, such as language, or myth, or religion, or legal ideas, were content to attempt an explanation of the facts of some particular age or country by observations carried on within that age or country alone, or if beyond it, only in adjacent ages or countries of the same type. The historic method looks farther afield. It compares the institutions of widely different ages, or of peoples who though contemporaneous stand at widely different levels of civilization and of thought. In the light of such a comparison, facts may take on quite a new appearance. Legal or other quetoms for which a later age had found a reason in some supposed meaning or utility which they now possessed are seen to have had a very different origin, in conditions no longer existing, and ideas no longer entertained. Folk-lore is full of such surprises. The custom of throwing rice after a married couple as they drive away is cometimes explained by saving that rice is a symbol of fertility : Dr. Fraser. comparing a number of other facts, thinks that the rice was originally intended to lure back the spirit of the bride or bridegroom to its body: it was supposed that at critical times-and everything connected with marriage was critical—the spirit left the body. in the form of a bird; the rice would attract it, and if it hovered about the body it would be more likely to re-enter. Whether this be the true explanation of the custom or not, only the comparative method could have suggested it. It is the same with myth: the account of the origin of Greek and Roman mythology popularized by Max Müller represented it as, in the language of Dr. Andrew Lang, a disease of language, the pearl in the oyster.1 Names originally designating the attributes of earth or sun or moon were confused with words of similar sound but different meaning, and out of these other meanings myths arose. Apollo 1 Custom and Myth, p. 1.

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Lykics had no connexion with the wolf - he was only the Shining one: but when that was forcetten, some wolf story would be invented to account for the name. Such theories are however discredited when it is found that a myth occurs in forms substantially alike

. . . among widely different peoples, whose languages do not admit of supposing it to have originated through confusion of similarly sounding words with different meanings. There is no new principle in the use of such an argument against the 'Sun-myth' theory of mythology: we simply say that the theory fails, because

. -_ the phenomena it is intended to account for occur where it cannot - 1 be applied. But Arvan mythology is a large subject by itself; an enquirer might naturally think that it could be explained without - 1. going to the mythology of African or American savages; it has

been found that this is not the case; the long descent of man

connects his present with a past very dissimilar, and connects thereby with one another contemporary forms of civilization wide apart. Therefore it is important to insist upon studying the pre-

sent in the light of history and comparing as extensive a range of

We hear sometimes of 'methodological assumptions'. By the term is meant assumptions made for the sake of cetting forward with the scientific treatment of a subject, but not conceived as neces-

sarily true. For example, there is obviously some connexion

between states of mind and states of hody. The psychologist. seeing quite clearly that to suppose the former to be produced by the latter soon lands him in the most honeless contradiction, and ignorant as to the true way of stating the relation between them.

may think the hypothesis of interaction the most convenient assumption to make, with a view of increasing and systematizing his knowledge of the laws which determine the development of the

individual mind: or instead of the hypothesis of interaction (which

conceives mind and body as producing changes in one another) he may prefer the hypothesis of parallelism, according to which every mental change has a corresponding bodily change, and vice versa, but the two series proceed each uninfluenced by the events of the other. Either hypothesis, if not regarded as true, but only as facilitating enquiry, would be a methodological assumption. Similarly, if he believes in the freedom of the will, the psychologist may still, as a methodological assumption, accept the doctrine of

facts as can be eathered together.

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determinism; because so far as actions have not any cause sufficiently accounting for them in the pre-existing state of the agent, but spring from the activity of a will acting according to no fixed laws, it is hopeless to try to explain their occurrence. In his attempts to do this therefore he will assume what is necessary to the possibility of doing it, even though he may believe that it cannot be allowed her done.

Leatly general logical considerations may indicate the weak places in a particular science at a given time, and thus show what line of enquiry is logically of most importance to the science in question. The theory of Natural Selection assumed the existence of variations, that is divergences from the parent type in offenring : and it assumed these variations to be accidental and non-adaptive. It concentrated itself at first on the task of showing how great a degree of adaptation between an organism and its environment could be brought about through the operation of the struggle for existence among individuals varying slightly from type in all directions: and how by the accumulation of such small variations as happened to be favourable in each generation a profound modification of specific type might ultimately be produced. It was quite worth while to work this out even upon a besis of assumption as to certain of the facts. But the pressure of criticism has directed attention to the question whether variations are all of them non-adaptive; and one of the logical requisites of the theory of Natural Selection is a suitable collection of facts throwing light upon this point. The facts are not very easy to obtain or estimate : but biologists are working at this problem with great assiduity. A study of the contemporary state of biology from a logical point of view would have to consider with some care the kind of facts required on such a point as this, and the sort of instance that would be crucial! i. e. decisive against one or other theory.

¹ From cruz, a sign-post: as directing our choice between two (or more) theories: e. Bacca, Nov. Opr. II. 88. A crucial instance, though it can disprove, can never prove a theory, except upon the assumption that there is the contract of the contract of

CHAPTER YYVII

APPENDIX ON FALLACIES

A PATTACY is an argument which appears to be conclusive when it is not and the chief use of studying fallscies must be that we may learn to avoid them. Regarding Logic as a science, we might therefore justly say that we are not called upon to discuss them. The only way in which their study can beln us to understand how our thought works is by the force of contrast. Show a man an aronment which he recognizes to be unsound, show him where the nnsoundness lies, and he may very likely realize more clearly so far as they can be formally prescribed, what are the conditions of valid reasoning. On this account as we went along we contrasted examples of invalid with examples of valid inference. What more then is wanted? for the case is not as it is, for instance, with psychology, To the psychologist few things are more instructive than the study of marked abnormalities of mental life: just as to the physiologist diseases reveal much which cannot be seen in health. For psychology is an empirical science, so far as it is a science at all: it sime at discovering the principles in accordance with which the various manifestations of consciousness develop in the life of the individual : what these are it is to a large extent unable to anticipate, although the metaphysician may have his views as to the conditions under which alone their action whatever they may be is possible. Now insanity is just as much a fact as any normal mental development; it must equally admit of explanation; and doubtless the same principles, in accordance with which this development proceeds under certain conditions normally and to a same result, are exemplified in the mental disturbances which other conditions evoke. They are exemplified too in a more prominent way : so that such cases furnish what Bacon called a glaring instance 1 to assist us towards their discovery. But it would be absurd to say that the principles of rational thought are

¹ Instantiae Ostensinae, or Elucescentiae. Nov. Org. II. 24.

equally exemplified in fallacy as in sound thinking; and it would he absurd to hope to discover, in the procedure of a fallacious mind. the nature of true thinking. We have said once and again that Logic analyses the operations of thought which the mind has already performed about other matters; but it must not be sunposed that it is on that account, any more than mathematics, an empirical science. The mathematician can only recognize the necessary relations of number or space by the help of some quantities or figures in which he finds them; yet he recognizes their necessity to be absolute and universal, and the fact that his nonmathematical friends make mistakes in their mathematical thinking is not taken by him as evidence that there are really two ways of thinking about the matter; he merely says that on such subjects they cannot really think. So also with Logic. Only in some thought in which they are found can the necessary relations involved in thinking be recognized; but their necessity too is recognized to be absolute, and we say that those who think differently are incarable of thinking about how they think. If any one is inclined to hold otherwise, and to suppose that the laws of our thinking are psychological laws, exemplified no less in fallacy than in its opposite, let him reflect that even in doing so he is bound to assume the contrary. For he who in that mind sets out to ascertain what the principles of thought, as a matter of empirical fact, are, will be unable by rights to know that the thought is valid by which he conducts that investigation. How then could be have any confidence in its results? Yet the fact that he intends to trust them implies that he assumes the principles of thought, in accordance with which he conducts the investigation, to be valid, whatever principles the investigation may report in favour of; and herein he takes for granted that he can recognize immediately what rational thought is, without reference to empirical facts revealed by psychology.

Nevertheless the insertion of a chapter on Fallacies may be defended. It has tradition in its favour; and without it, the nomenclature of fallacies—a nomenclature by no means fallen out of common use—would remain unexplained. There are practical uses it also; and it would be ridiculous to say that because Logic is a science we may not turn the study of it to advantage in practice. Familiarity with some of the commonest types of fallacy is no security that we shall never fall into them ourselves: still less are

we bound to fall into them unless we have acquired that familiarity. But it may help us to avoid them, by helping us more readily to perceive them. The overtones which a man has never noticed till they were pointed out to him he may afterwards detect easily for himself. A flavour in a dish a line in a micture, whose presence had cone unobserved, a man may be unable to ignore, if it has been singled out and presented to him in isolation. So it may be with a fallacy. There are many whose percention of the unsoundness of an argument is not unaffected by their belief in the truth or falsity of its conclusion : they will detect it where they think that what it proves is false : but let it be true-still more, let the supposed truth be precious to them, or familiar-and the same form of argument in its support may pass unchallenged. Yet if we have accustomed ourselves to the look, or type, of the fallacy, we are less likely to be the victims of such an imposition. It is true that, in the words of Archhishon Whately 1 . After all indeed in the prace tical detection of each individual Fallacy, much must depend on natural and acquired acuteness, nor can any rules be given the mere learning of which will enable us to apply them with mechanical certainty and readiness; but still we shall find that to take correct general views of the subject, and to be familiarized with scientific discussions of it, will tend, above all things, to enceuder such a habit of mind, as will best fit us for practice.' And, as Aristotle intimates a man who may be able to detect a fallacy well enough, if you give him time, by the light of nature, may be placed at a practical disadvantage by not being able to do it quickly enough: here the systematic study of fallacies will help him. Nor is it only in arguing with others that he may reap some benefit from the study; it will accrue to him also in the conduct of solitary thinking.8 It was however chiefly with reference to the conduct of debate that Aristotle discussed the subject. It was from this point of view that he observed, that a man might be suspected of incompetence, who only found fault with an opponent's argument, and could not show in what the fault consisted. It may be added. that so far as fallacies are referable to recognized types, it is a great abridgement of criticism to be able to name the types, and refer a particular fallacy to one of them.

Logic, p. 158, 8th ed.
 Ib. 175* 9.

Soph. El. zvi. 175* 23.
Ib. 175* 14.

These are practical considerations, and it would probably be found that importance has been attached to the doctrine of fallacies chiefly by those who have viewed Logic as an instrument for reasoning. But an use may be found in the doctrine, of a more theoretical kind. It is intellectually unsatisfactory to see that an aroument is faulty, and not to see precisely why. We desire for ourselves, no less than we owe to our opponent, an analysis of the error. Otherwise, and if we can only see it, and not see through it. the mind, as Aristotle expresses it, is bound, and unable to proceed. It is probable that some of the fallacies of which he finds the solution in different ambiguities of language did once constitute a more serious entanglement than they do to-day. This is partly because, as others have pointed out, such fallacies generally disappear by translation into a foreign tongue; and peoples more familiar than the Greeks were with a diversity of tonoues have a great advantage in detecting such. It is partly also because an analysis new in his day is common property in ours; and many of its results are so incorporated into the currency of common thought and speech, that a man whose attention is called to them feels as if he was taught only what he already knew.

If however we are satisfied that Logic should treat of fallacies. it is very difficult to be satisfied with any treatment of them. Truth may have its norms, but error is infinite in its aberrations. and they cannot be digested in any classification. The same inconclusive argument may often be referred at will to this or that head of fallacies. 'Since, in any Argument,' says Whately, 'one Premiss is usually suppressed, it frequently happens, in the case of a Fallacy. that the hearers are left to the alternative of supplying either a Premise which is not true, or else, one which does not prove the Conclusion. E.g. if a man expatiates on the distress of the country. and thence argues that the government is tyrannical, we must suppose him to assume citter that "every distressed country is under a tyranny", which is a manifest falsehood, or, merely that "every country under a tyranny is distressed", which, however true, proves nothing the Middle-Term being undistributed.' The assumption

¹ Eth. Nic. n. iii. 1146° 24. ² Cf. de Morgan, Formal Logic, p. 287. 'There is no such thing as a classification of the ways in which men may arrive at an error: it is much to be doubted whether there ever can be.' Logic, p. 159, 8th ed.

of a false premies is not indeed perhaps to be called a fallacy, as we shall see presently: it is at any rate different in its nature from inconclusive argumentation. But the choice may equally well lie between two modes of inconclusive argumentation when we have to alcounty a falleny: a man who attempts to refute by an enumeration of striking instances the proposition that some specific characters in plants and animals are not adaptive might either he charged with illicit process of the minor term, in drawing an universal conclusion where his premises only entitle him to a particular one. or with what is called Invocatio Eleuchi in supposing that a particular affirmative refutes a particular negative. And not only is it impossible to make such a classification of fallacies as will never leave it in doubt to which class a particular example is to be referred : if that were all, it might be said that the types were distinct, and the classification so far a good one, although individuals could not be assigned to their types unambiguously: but it may be doubted as well, if the types of error can be exhaustively detailed, and the classification completed.

The reason for this is twofold. In the first place, there may be arguments so foolish and inconsequent, that they cannot even be said to simulate cogency; these cannot be positively characterized, but must be lumped together by the mere negative mark of inconclusiveness. And secondly, there are many fallacies, the detection of which requires not general logical training, but acquaintance with a particular scientific subject-matter. The latter point is of some importance, as connecting with what has been already said short demonstration.

We have seen that the syllogism cannot sustain the claim once made in its behalf, of being the type of all valid inference; but that there are deductive reasonings—to say nothing of hypothetical and disjunctive argument—whose validity lies in no conformity to a scheme exhibitable in the abstract, or symbolically, but rests for its apprehension upon acquaintance with the nature of the special subject-matter with which they deal. The readiest illustration of this, but by no means the only one, is furnished by geometry. Now what is true of valid is equally true of invalid reasonings. There are many which are not of a sort that can occur in reasoning

¹ Cf. Ar., Soph. El. xxiv. 1795 17 οδδέν δέ απλύει τόν αύτον λόγον πλείους μοχθηρίας δχευέ, and xxxiii. 1825 10.

on every subject-matter, but are bound up with misconceptions of the special subject-matter in which they occur. This too may he readily illustrated from geometry. 'Lewis Carroll' devised a proof that 'a right angle is sometimes equal to an obtuse angle'. The demonstration was in all other respects unimpeachable, but vitiated by one-of course intentional-error in the construction of the figure, in which a line was drawn to one side of a point which must in fact fall on the other. I Just as a knowledge of peometry can alone show where this line must fall, so a knowledge of geometry can alone expose the inconsequence of the false demonstration. And similar inconsequences occur in every particular science, which only an understanding of that science can show to be inconsequences. Thus if it were around that because a and b were halves of the same thing, therefore they were halves of one another, and since a = 4, δ must = 2, it is only a perception of the nature of quantity that reveals (doubtless in this case to the least mathematical of us) the invalidity of the first step in the aronment. It is less obvious that among a people who acknowledge kinship only through the female, a man would inherit not from his father but from his brother or maternal uncle. Yet a little reflection shows this to be the case, and shows therefore the fallacy of

¹ a. the Losic Corroll Printer Rock, edited by S. Dodgwon Collingwood, (London, 1899), pp. 286-287. (OK most really full the right of C.)

164 ACC De a square. Black AS at S, and through S draw EF at the Company of the Company

Since AB, AG are not parallel, EF, HK are not parallel. Therefore they will meet if produced. Produce EF, and let them meet at K. Join KD, KA. KG and KC.

The triangles KAH, KOH are equal, because AH = HG, HK is common, and the angles at H are night. Therefore KA = KG.

The triangles KDF, KCF are equal, because DF = FC, FK is common, and the angles at F are right. Therefore KD = KC, and angle KDC = angle KCD.

Also DA = CB = CG.

AND DA = CP = CV. RCC have all their fide equal. Therefore the angles RDA, RCC have equal. From these equals are the equal angles RDA, RCC are equals. From these equals expected by the equal angles RDC, RCD. Therefore the remainders are equal: i. e. the angle CD = the angle ADC. But GCD is an obtain angle, and ADC is a right angle.

'Therefore an obtuse angle is sometimes - a right angle.

arguing, where female kinship prevails, that because A is in possession of a property, his son will possess it after him. Here the detection of the fallacy rests upon our perception of the system of relationship uniting the members of a society which takes account only of union by descent through the female line.

Aristotle, who noticed that every science afforded its own special opportunities for erroneous inference, gave to those that involved mistakes in geometry the name of werboypdonua, or false construction.1 As an example he gives Hippocrates' method of sonaring the circle by lunules. A lunule is a figure enclosed between area of two circles concave in the same direction. Hippogrates found a rectilinear area equal to a lunule whose upper arc was a semicircle, and its lower arc the fourth part of the circumference of another circle; he then found another rectilinear area equal to the sum of (a) three equal and similar lunules whose outer area were semicircles, and their inner ares the sixth part of the circumference of another circle, and (b) a semicircle of the same diameter as the three lumiles (i.e. of diameter equal to the chord of the arcs enclosing them); and he supposed that by subtracting from this rectilinear area an area equal to the three lunules, he could obtain in the remainder a rectilinear area coust to the semicircle. He overlooked the fact that because you can find a rectilinear area equal to a lumule of the former sort, whose inner are is a quadrant, it does not follow that you can find one equal to a lunule of the latter sort, whose inner arc is a sextant : and in fact a rectilinear area equal to these three lunules cannot be obtained \$

Now it will indeed be seen that, in this or any other case of erroneous reasoning dependent on misconomiving the consequences which follow from given conditions in a special subject-matter, the error can be expressed in a false proportion. It is false that because a rectilinear area can be found equal to one of these lunules, it can be found equal to the other: it is false that things which are halves of the same things are halves of another: it is false that, if we take account only of kinship through the female line, a man will be in the same line of descent with his father. But we cannot see that any of these propositions is false, unless we understand

t, xi. 9 s. Poste's ed. of Soph. El., App. F, pp. 245-247.

something of the respective subject-matter. They are as it were false 'special principles', or Ran Appel. It is not desirable to call every false proposition a fallacy, as e.g. that snakes eat dust, or that South America is an island; nor can we extend the name to every valid argument that use a false premise. If the falsity of the premise can only be ascertained empirically, there is be ascertained by thinking out the consequences of ortain relations, or conceptions, in the circumstances of a given case, then we are guilty of fallacy, or effect of reasoning, in overlooking it; and that is what frequently occurs in the matter of any particular science.

There are indeed general heads under which many such fallacies can be brought. In particular, they very often arise from overlooking some of the special circumstances of the case : from assuming that what is true under certain conditions will still be true when those conditions are in some way modified. Thus, if two things a and b are count to the same thing, they are count to one another: from which we may conclude that if they bear any some quantifative relation to a third thing, they bear that relation to each other: and then it would follow that if they were halves of the same thing they would be halves of one another. But in fact, it is only when their same relation to a third is one of conslity, not merely when their relation to it is the same that they bear to one another the relation horne to it. We shall meet with this type of fallacy by and by under the name of Secundum Quid. That heading embraces a great range of examples. But though we can detect in them a common character, it is only by understanding something of the special matter of the argument, that we can see that the fallacy is being committed in a given case. The type, if one may say so, is fluid; the instances are not so far of one form, that we can separate their common form from the variety of their matter, and exhibit it symbolically: nor, though the type admits of all this diversity, can we subdivide it, and carry our classification down to infimae species. We recognize that its character differs in different cases: but the differences cannot be formulated.

Our task then is one which does not admit of fully estisfactory performance. Still no doubt it can be better and worse done. What classification of fallucies are we to adopt?

The earliest, and for long the accepted, classification is that of Aristotle given in the last book of his Tonics, called the Sondistics Elenchi. It is not free from defects: and others, some of which will be referred to have been propounded. But the subject is emphatically one upon which some consensus is desirable. If it is neeful to have a nomenclature of fallacies it is useful to have a standard nomenclature. And it is remarkable how even in rival classifications, many of the Aristotelian species of fallacy still hold their own Leter writers have given new meanings to the Aristotalian names in certain cases; or have invented names for special forms of some of the Aristotelian fallacies; or have included in their list what are not forms of erroneous argument, but sources of error of a different kind! vet it is surprising how little there is which cannot be brought within Aristotle's list. And if we consider not the enumeration of types of fallacy, but their classification, it will appear. I think that there is no such merit in any alternative scheme as justifies us in sacrificing the advantage of keeping to the standard and traditional scheme of Aristotle.

Aristotle divided fallacies into two main groups-fallacies in

Thus the fallacy of Accident has practically been identified with Secundam Quid by many writers: that of Consequent has, a.g. by the Morgan does not follow from the premisers (de Morgan, Fromel Logic, p. 2051; divers forms of Ignoratic Elected have received special names: Whately have represented by the property of the property o

dictions or wood ray Affer arising through ambiguity of language. and fallacies axtra dictionem, or If wife Affens, which do not have their source in such ambiguity. Although one of his species of fallacies extra dictioner the fallacy of Many Questions might nerhans he referred more naturally to the other ornun, vet the division being dichotomous, is sound. It suffers, however, like all such divisions, from the defect of not positively characterizing one member.1 Later writers, willing to remedy this defect, called the follogies entre dictiones fallacies is es or material fallacies. But this introduces a cross-division. For it cannot be said that fallacies in dictions are independent of the res or matter of the argument. On the contrary, inasmuch as they arise through giving different meanings to the same words either in the two premisses, or in premise and conclusion they disappear if we abstract from the matter of the argument and look only to the form in which it is cast. The proper antithesis to matter is form: a fallacy not in the matter must be in the form . i.e. it must be independent of what the terms are, and must therefore persist, if symbols be substituted for the terms, and whatever term he substituted for the symbols. This cannot be said of the fallacies is dictions.

It is true that Whately gives a somewhat different interpretation to the expression material fallacy. He divides fallacies into logical and material. By the former title he means fallacies where the error lies in the fact that the premisses do not prove the conclusion : by the latter, those in which the premises prove the conclusion, but either the premisses are false, or such at least as we are not entitled to assume, or else the conclusion proved is not that which we profess or are required to establish. He then subdivides logical fallacies into two groups, according as their defect of proof can be seen in the mere form of the argument (e.g., in the case of undistributed middle) or only if we attend to the ambiguity of the terms employed; the former group he calls purely logical, and the latter semi-logical. Though the nomenclature here is unfortunate (for according to his own definition of a logical fallacy, those which lie in ambiguity of language are altogether and not only half logical). vet the division is sound. It includes however arguments which have no fault except that their premisses are false; and it is true that in

¹ Cf. supra, pp. 107-109.

this he follows the words of Aristotle! but in the body of his treatise Aristotle proceeds as if he had not included them. And the practice of Aristotle appears preferable in this respect: for false premises are certainly incapable of any classification, and the consideration of one does not help us to detect another. That if the premises are false, the conclusion is not bound to be true, every one should certainly realize; and it is good advice to a disputant to consider well the truth of the premises he is asked to grant or to a solitary thinker to consider well the truth of what he proposes to assume and build upon. Nevertheless there seems to be a real difference between a plansible but inconclusive accument, which we can see through by clearer and more attentive thinking, and a false proposition (whether or not plausible), which cannot be exploded by any more attentive consideration of itself, though it may by reasonings that are within our power. For this reason the extension of the term fallacy to cover 'any false assumption employed as a premise ' seems undesirable : the only sort of false proposition to which it ought to be applied is false canons of reasoning. If this correction is made. Whately is left with only two kinds of material fallecy (Petitia Principii and Ignoratio Elegali), both of which are in Aristotle's list of fallacies exten dictiones : and there is no particular advantage in that regrouping of the species enumerated in both lists, which the adoption of Whately's principle of division carries with it. Whately certainly enumerates under the head of purcly logical fallacies those breaches of syllogistic rule with which we long ago became familiar by the names of undistributed middle. quaternio terminorum, and illicit process of the major or minor term: and Aristotle makes no mention of these. But that is not because his classification provides no place for them ; they are clearly fallacies extra dictionem. They were omitted because they did not, in

¹ Top. a. i. 1009 28 Japarenke 8 fort: analyzargake 6 is quantative lehkker, and forme bit, and 6 if Felkker 6 havarprive lehkker quantures: CSph. 25. ii. 1859 7 Japarene is likepa of it is via quantum lehkker pi forme bi valorgarman from premises really endocrical (i.e. probable or supported by opinion, and squaments from premises really endocrical (i.e. probable or supported by opinion, and be deliberate. The expression wires used in Sph. 25. i. 1(148 × 25 m při veje a pir viel evalorgarman i To expression uvico used in Sph. 25. i. 1(148 × 25 m při veje a pir viel evalorgarman i vedente premise an circ kapteropri can Eryrar quantum při volkoparman, and ich supporture for mai evalorgarma an Eryrar quantum při volkoparman a Proprag durafusere při volko 30 implit perhaps by liselí be more naturally undentood to refer access in the fallatí of their promises.

Aristotle's view simulate copency: no one who could not detect these anoth to undertake a disputation : and even a sonhist airning only at appearing to confute his adversary and not at truth would hardly done to employ such methods as these. And so it was with the writers who for many centuries reproduced—often with increasing divergence—the Aristotelian doctrine. 'The pure syllogism and its rules were to them as familiar as the alphabet. The idea of an absolute and glaring offence against the structure of the syllogism being supported one moment after it was challenged, would no more engagest itself to a writer on logic than it would now occur to a writer on astronomy that an accidental error (which mis-ht happen to any one) of affixing four ciphers instead of five when multiplying by a hundred thousand would be maintained after exposure 1 A sophism, or sophistical confutation as Aristotle called a fallacy (for he had in mind throughout the conduct of a disputation, and the methods by which one might attempt to confute a thesis maintained by an opponent: though these are of course countly methods of establishing a conclusion that confutes it). must be at least decodureros gullovigude, apparently conclusive: these he wished in his treatise to enable the learner to expose 2: but a plain breach of syllogistic rule had not any appearance of conclusiveness, and enough had already been said in the Prior Analutics to enable any one to expose that.

We may therefore abide by the Aristotelian division into fallscies in dictione and extra dictionem. In each member of the division he enumerates a variety of types. The lists are as follows 3:-

de Morgan, Formal Logic, p. 240.

Oct. Soph. Et l. 1859-28 rbs di spublisher supparifers discarden.

Whately, as was observed above, regroups the fallacies here enumerated to suit his division. It is of course inadmissible to adopt the nomenclature. to suit his division. It is of course inadmissible to adopt the nomencladars of his division, and retain Aristotle's grouping, as is done by Jerons in his Elementary Lessons, XX and XXI. He treats as purely logical fallacies the four breaches of splingstic rule above mentioned; as semi-logical, Aristotle's event fallacies and as fallacies, Aristotle's event fallacies extra six fallacies in dictions; and as material, attracties seven issued and dictionem. He does not therefore understand the distinction between logical and material as Whately does. 'The logical fallacies,' he says, 'are those which according the material's the material as fallacies, on the contrary, arise outside of the mere verbal statement, or as it is said, extra dictioners (p. 170). This is not of course what those words meant. But clearly Jevons means by a logical fallacy one which can be detected in the form without consideration of the matter; it should therefore be capable of illustration in symbols, as his 'purely logical' fallacies are. A moterial fallacy, on the contrary, needs that we should understand

- a. Fallacies in dictione, or mapa the Affir.
 - 1. Equivocation, or παρά την διωρυμίαν.
 - 2. Amphiboly, or wash the dudification.
 - 8. Composition or mad ray girdegue.
 - 4 Division, or good the highester.
 - 5. Accent. or mand rive monomedian
 - 6. Figure of speech, or mand to grang the Affence.
- b. Pallacies extra dictionem, or Ifm rise Affense
 - 1. Accident, or wood 70 anu. 848 proce
 - 2. Secundum Quid, or παρά το άπλως ή πή λέγεσθαι καὶ μή
 - 8. Innoratio Elenchi, or mapa the tou thereou deposar.
 - 4. Petitio Principii, Begging the Question, or παρά τὸ ἐν
 - 5. Non Causa pro Causa, False Cause, or παρά τὸ μὴ alrιον
 - Consequent, or παρά τὸ ἐπόμενον.
 - 7. Many Questions, or παρά τὸ τὰ δύο έρωτήματα ἐν ποιείν.

the term for its stated too. From this point of rise, it is nonesnee to spake of mininger of Mattiers, a fallow rithms on an detected it rymboles or for its interest to the property of the state of th

The fallacies is dictions are so many different forms of error that may arise through the double meanings of language. They differ according to the character of the ambiguity and it may be any of the three terms which is ambiguous! Obviously such arouments are invalid; and if the different meanings were expressed by different terms in each case, we should have a plain oraternio termisorum, which would impose on nobody. As it is, the shifting of the meaning may sometimes pass unobserved : or the identity of the language seem to afford some proof of identity of meaning: and even where it is obvious that we are tricked by the argument. we may wish to be able to show how

1. Equivocation is the simplest form of ambiguity, where a single word is used in divers senses. 'The sick man is well; for men who have recovered are well, and the mok man has recovered '1. here the equivocation is in the minor term, and arises from the fact that the expression 'the sick man' may mean either 'the man who is sick' or 'the man who was sick'. The following is an old example: 'Finis rei est illius perfectio: mors est finis vitae: erro more est perfectio vitae': the equivocation in this case lies in the middle term. Trivial and punning examples of this fallacy, as of all those that depend on ambiguity of language, will occur to any one: but in many cases it is serious and elusive. 'It is the business of the State to enforce all rights : a judicious charity is right : therefore it is the business of the State to enforce a judicious charity.' 'A mistake in point of law,' save Blackstone, 'which every person of discretion not only may, but is bound and presumed to know, is in criminal cases no sort of defence's: the State must perhaps presume a knowledge of the law, and so far we are bound to know it, in the sense of being required under penalty; but a criminal action done in ignorance of the law that a man is levelle bound to know is often considered morally discreditable, as if the knowledge of the law on the matter were a plain moral duty. How far that is so in a particular case may be a very doubtful question: the maxim quoted tends to confuse the moral with the legal obligation. In a long and closely reasoned argument, where important terms have been defined at the outset, it may still be very difficult

Many arguments referable to Aristotle's headsof fallacy are not syllogistic. Ar., Soph. El. iv. 185° 89. Quoted by Austin, Jurisprudence, i. 482.

to hold them throughout to the precise meaning set forth in the definition: and so far as this is not done, the fallacy of Equivocation arises. Locks in his Essay ! defines 'idea' as 'whatsoever the mind nameives in itself or in the immediate chiest of nemention. thought, or understanding': but in the course of it he is at times a victim to the ordinary associations of the word in English which contracts 'my ideas' with the 'realities'

2 Amphibaly 2 is ambiguity in a phrase, in which the words are used univocally throughout, but the meaning of the phrase as a whole changes through change of the construction in which the words are taken. A traditional example in Latin is 'Quod tancitur a Socrate illud sentit : lanis tangitur a Socrate : eron lanis sentit ' : in the major premise, illed is the object of scalit; the conclusion is drawn as if it had been the subject. So we might say in English : 'Polyphemus what he best loves doth devour : the ram that leads the flock he loves the best : therefore the ram devours him . Lawvers are well aware of the importance of avoiding ambiguity in the construction of a legal document (though under that head they would include the ambiguities which Aristotle assigned to Division and Composition, as well as Amphiboly and Equivocation too). Whately cites a good example from the rubric at the beginning of the Form of Service formerly ordered for use on Jan. 80, the anniversary of the execution of King Charles I: 'If this day shall happen to be Sunday, this Form of Prayer shall be used and the Fast kept the next Day following ': is the form of prayer to be used on Sunday and the Fast kept on Monday, or are both to be deferred? Another famous and deliberate example is in the oracle which Ennius said was delivered by Apollo to Pyrrhus-' Aio te, Acacida, Romanos vincere posse.' 8 Ambiguous words and constructions are still not unfrequently used to deceive by those

That palter with us in a double sense : That keep the word of promise to our ear. And break it to our hone.'

¹ Br. II., c. viii. § 8.
² Br. Greek word in specification which is said to be an invitor work the before.
³ The Greek word in specification when the sunbiguity is in an Cospa (Sept. M. vii. 1989 22). Hence store the composal specification, which became recurrent into Amphibology, as sideal-law-prise became correpted into Idolatry. There seems to be no reason for not exprise Amphibology in English! Amphibolia is frequent in Latin (e.g. Cruckenthorpe, Addrich).
³ Ch. Cit. & Diministronie, it Se. Ciccer reasonably observes that Apollo

3 and 4. Composition and Division are the converse one of the other. They consist in taking together in the conclusion (or one premise) either words, or objects of thought, which in the premise (or the other premise) were not taken together, or vice versa. Plato in the Republic 1 aroues, from the fact that a man can refuse the thing that he desires, that there must be a principle of reason as well as of appetite in the soul. For, he says, it is impossible to be contrarily affected at the same moment towards the same object in the same part of oneself (one cannot for example at once loathe and long for the same object); yet a man who is thirsty and refuses to drink is contrarily affected at the same moment towards the same object. he does not therefore refuse drink on account of the character of his annetites, but because of his reason: he reckons that to include his appetite would interfere with the pursuit of some other end which he prefers. Now a sonhist might attack this conclusion as follows: 'Are you now drinking? No. Can you now drink? Yes. Therefore when you are not doing a thing, you still can do it? Yes. But if you can do a thing when you are not doing it, you can desire a thing when not desiring it? Yes. And so you can be contrarily affected in the same part of vourself (your appetitive nature) towards the same object at the same time.' The fallacy is one of composition. The admission is that a man can when not desiring a thing desire it, i.e. that when not desiring it, he is capable of doing so : this is used as if it meant that he can desire when not desiring it, i. e. that he is capable of at once desiring and not desiring it: the words 'when not desiring it' are taken, or compounded, in one case with 'can' and in the other with 'desire'. If a man were to argue that three and two are five, and three and two are odd and even, therefore five is odd and even, and the same number may thus be both, he would be committing the same fallacy; when

did not speak in Latin. Cf. Augustina, ds Civ. Ds_i iii, 17 °Cai mae de rerum fattor sentat consulent situs urbane Apollo sie ambigumo oraculom edidit, at, e duobas quicquid accidiatet, ipse divinus haberetter: ait enim, libro te Fyrphs vincers poses Romania et e Romania in Fyris vincers poses Romania in the Romania in Fyris vincers process and the situation of the situati

^{*} Hep. 1v. 430 a. eq.

3 Tō δύσταθει μὰ γράφοντα γράφειν is an example of fallacy παρὰ τὰν σύσθειν in Soph. Εl. iv. 186* 24. I do not know if the principle involved was ever brought agrainst Plato's argument.

it is said that three and two are odd and even, it is true only if o'dd and even' are not taken together, and predicated thus of three and two, but if 'odd' is separately referred to three, and 'even' to two; but the conclusion is drawn as if they were taken together. On the other hand, the same argument furnishes an example of the counter fallacy of taking separately in one premise words which were taken together in the other; for three and two together are five, but it is separately that they are odd and even, and separately that in the conclusion each of them is declared to be both. And the reader will doubtless have observed that the previous example illustrates no less the division from one another in the conclusion of words that were combined in the premiss than the combination in the conclusion of words that in the premiss were divisited.

It was said above that in these fallacies either words or objects of thought are taken in one place in the argument together and in another separately. Of course the combination or separation of certain words carries with it that we think differently in either case of the things signified. But sometimes the illicit combination or division made in thought is not reflected by taking words together or apart. If any one were, upon the strength of the text in Gen. i. 27-'So God created man in his own image, in the image of God created he him male and female created he them '-to aroue that man was originally created bisexual 1, and that the present division into male and female was the result of the Fall and were to base on that a condemnation of marriage, he would be guilty of the fallacy of Composition; and quite as foolish arguments have been drawn from the words of Scripture upon such subjects. Now here the fallacy lies in referring the words 'male' and 'female' together to each person signified by 'them', instead of referring 'male' to one and 'female' to another. But the point is the same in the story of the showman who announced that children of both sexes were admitted free, and then charged admission to boys and girls alike on the plea that neither of them were children of both sexes. Yet in the latter case there are no words that are wrongly taken together; it is the sexes thought of, to which the showman pleaded that he had only promised to give free admission when

¹ Cf. the fancy in Plato's Symposium, 189 D E.

combined. Words like bots and all, which may indicate equally a distributive and a collective reference to the things signified by the substantive to which they belong, are specially adapted to facilitate this fallacy.\(^1\) Another and a double example of the fallacy of Coposition, in a business transaction, is afforded by the talle of a railway enterprise in one of the British Islands. A company is said to have been formed to build a railway, and to have announced in its prospectus that a guarantee of 8\(^1\), on the share capital had been given by the Government, and a guarantee of 2\(^1\), by the local authority; and later in the same document to have stated that a guarantee of 5\(^1\), had been given by the Government and by the local authority.

5. The fallacy of A accent meant to Aristotle one arising through the ambiguity of a word that has different meanings when differently accented. It was perhaps distinguished from Equivocation, because words differently accented are not strictly the same word. The Latin writers illustrate it in words which have different meanings when their quantity is different; a.g. 'omne malum est fugiendum. Domain est malum est fugiendum, pomum est malum: ergo fugiendum. The ambiguity is course one which is more likely to occur in what is written than in what is spoken. In English, which does not distinguish words by tonic accent, the name is generally given to arguments that turn on a wrong emphasis of some particular word in a sentence; in which if the emphasis were placed differently, the meaning might be very different. The words of the Catechism in the 'Duty towards thy

¹ It illustrates how much skin the different fallacies in dictions are, and how the same example may from different points of view be regarded as falling under different heads, that any non-wio likes can call the showman's trick, or others where words like off and how figure similarly, fallacies of active of the same of the control of the control

Neighbour '—' to hurt no body by word nor deed '—have by laying stress on body been wrested to include the injunction to be kind to animals.

6. The fellow of Blomps of Speech arises through the embiguous forms of some werbal inflation, which is wrongly alleged to imply in one case what it really implies in others. If a man were to argue from the use of such an expression as 'I am resolved what to do', that, because the passive signifies not action but being acted on as in (I am heaten' (I am praised therefore a man's resolution is not his own free act, but the result of something done to him, he would be guilty of this fallacy. Arguments from linguistic usage of that sort are by no means uncommon or necessarily unsound : as that the object of sight is not a visual sensation, because you say that you feel a sensation, but no one would say that he felt a colour. In this case there is no ambiguous inflexion, which is what was held to constitute the differentia of the fallacy now under consideration. But let a man may that important is a negative notion, because imperturbable or impendent is, and we have a case in point.3 J. S. Mill in his Utilitarianism affords an excellent example of a man misled by this fallacy in a critical point of his argument. He is trying to prove that the chief good, or one thing desirable, is pleasure. 'The only proof,' he says, 'capable of being given that an object is visible, is that people actually see it. The only proof that a sound is audible, is that people hear it : and so of the other sources of our experience. In like manner, I apprehend, the sole evidence it is possible to produce that anything is desirable, is that

This example was given me from personal recollection. Not unlike this fallow, underdood as consisting in basing on a wrong emphasis a conclusion not intended by the speaker or writer, is the error of inferring from the stress which a man laye on one element of a truth that he necessarily overlooks another. It might be said to be Hegel's conception of the progress of population to propose that its farmer by that the emphasis on so the strength of the propose of the truth of the contribution of the propose of the truth of the contribution of the propose of the truth of the contribution of the propose of the truth of the contribution of the propose of the contribution of the contribution of the propose of

A lady once observed: 'The question is, is he a postor or an mpostor?'

n. 52 (Routledge's ed., 'New Universal Library,' n. 66).

people do actually desire it. But visible, audible mean what one he seen or heard; whereas Mill is trying to prove that happiness anought to be desired, or is the thing world desiring. Yet the termination-able or-ible must be taken to have the same force in the word desirable as in audible or visible, if the argument is to have any force at all; and the only thing shown is really that men case desire hanniness: which was never in question.

To distinguish the different sources of the ambiguity in the different fallacies annumented above is not a matter of first-rate importance. but to be alive to the errors into which ambiguities of language may lead us is so. 'Verba plane vim faciunt intellectui, et omnia turbant.' wrote Bacon.1 Perhaps the disturbance which they caused was in some respects more serious of old than now. We do not suffer less from the subtle and unconscious shifting of the meaning of important terms in a sustained argument; but some of the more trivial and (as we should say) obvious ambiguities may have been a more real puzzle in olden days. 'The genius of uncultivated nations,' says de Moroun s cleade them to place undue force in the verbal meaning of engagements and admissions, independently of the understanding with which they are made. Jacob kept the blessing which he obtained by a trick, though it was intended for Essa; Lycurgus seems to have fairly bound the Spartans to follow his laws till be returned, though he only intimated a short absence, and made it eternal; and the Hindoo and who begoed for three sters of land in the shape of a dwarf, and took earth, sea and sky in that

No. Org. I. 43. The false ideas above nature generated through language Bacon called tides froit. These false ideas or dole were classified by his according as they had their sources in universal properties of human nature in ideograces see of the individual, in language, or in false theories of science and philosophy. The division was not logically perfect, and the commentation in each group is doubles not complete. This illustrates in classification of fallacies impracticable. Bacon himself calls attention to he sparalled that exists between his undertaking and a classification of fallacies: Decrema estim didolis similities whether of interpretationes matterns are decrined as applicated denotes of the control of th

of a giant, seems to have been held as claiming no more than was granted. The great stress laid by Aristotle on so many forms of verbal deception may have arisen from a remaining tendency among disputants to be very serious about what we should now call play upon words. Yust as many people tend to think that in conduct the claims of verseity are satisfied or broken, according as the facts can or cannot, by some verbal quibble, be brought within the four corners of what they said or promised, so with argument men may think that there is something in it, though the conclusion turns upon an ambiguity of language. Not but what men are often also too ready to assume that a controversy is merely verbal

In the enumeration of the fallacies which he recognizes. Aristotle obviously had before him the practices of disputants in his own day.1 One man, the 'respondent', undertook to defend a thesis: the other, the 'questioner' attempted to extract admissions from the respondent which involved the contradiction of his thesis. But we find that a man might endeavour to discredit his opponent by confuting him on a side issue : and that it was a recognized device to get him to admit something easier to attack than his original thesis: though when Aristotle wrote, men had learned to reply to the entrapping question by asking what it had to do with the original thesia. Similarly we are told that answers in the form of a plain ves or no were less insisted on when he wrote than formerly: whereby a bountiful source of unfair confutations was cut off.3 The questioner is advised also not only to endeavour to involve the respondent in a contradiction of his own thesis, but to bring out its inconsistency with what is held by those whose authority he or others may respect, or by mankind at large, or by the majority of mankind, or by his own school.4 Nowadays formal disputation has gone out of fashion. Men still harangue; and we understand by a debate a series of set speeches, in which a pronosal is attacked and defended. Many of the devices which can be

Minto, in the first chapter of his Logic, Inductive and Deductive, speaks as if Aristotle worked out his system of logic as a whole chiefly with the conduct of disputation in view. He seems to me to have very much overstated his case; but so far as the treatise on Sophistical Confutations is concerned, it is true.

Soph. E7. zii. 172b 16-24.

¹ lb. 1750 8-10. Cf. on the fallacy of Many Questions, p. 556, infra.

employed to produce the appearance of confuting an adversary are common to rhetoric and dialectic-to the harangue and to the interchange of question and answer. But if we were more familiar with the letter mode of trying an impa we should perhaps understand better the seams that exists for some of the conhistical confutations that Aristotle mentions. Such disoutation is seen chiefly to day in courts of law, when counsel cross-examines a witness; and an unacrupulous counsel can still confuse a timid witness and discredit him before the jury, by involving him in contradictions more annarent than real. And there have been times when matters. which to-day are submitted to the indosement of the public by means of speeches to and fro, reported in the newspapers, were around by chosen discutants according to fixed rules of debate before an audience whose verdict, as to which side got the best of the discussion, was of high practical importance. Not a few controversies of that sort were aroued during the Reformation, at Leinsic or at Marburg or at Zurich or elsewhere.

The fallacies is distinue have to some extent become of less importance through the decay of the habit of disputation. The same cannot be said of those extra dictiones.\(^1\) These are not united by any common character, as the others were by springing from anticutiv in language.

1. The first in the list is the fallacy of Acottant. The following are some of the cramples referred by Aristotle to this head:—'This dog is your: this dog is a father: therefore he is your father.' 1De you know the man approaching you with his face muffled? No. But he is Corriecus, and you said you knew him.' 'Six is few: and thirty-six is six times six: therefore thirty-six is few.' His solution of the error involved seems to be thin. A thing has divere sociedues, ic a taributes which are not commensurate with it nor essential to it; what is predicable of the thing may or may not be predicable of its accidents, and vice versa.' Thus the dog is a father, and is yours; but it does not follow that the father is yours—that he is yours as a father, as he is yours as a dog. Coriscus is approaching with his face muffled; to be a man approaching with his face muffled; to be a man approaching with his face muffled; to

Except perhaps 'Many Questions'; but cf. infra, p. 557.
 Soph. El. v. 166 80-32, xxiv. 179 27-31.

an accident of Coriscus: and it does not follow that, because Coriscus is known a man approaching with his face muffled is known to you. It is an accidental way of regarding thirty-six things that they are giv groups of giv things; and though the groups are few, the thirty-six are not therefore few. The defect of the solution offered is that it does not enable us to distinguish between those cases in which what is predicated of a thing's acridents may be predicated of the thing itself, or vice versa, and those in which it may not. 'This door is yours and this door is property (or a spaniel) therefore he is your property (or wone spaniel) '. why is this aronment valid and the former one not? If you say that the former is invalid because it constant subject and accident ! when they are incommensurate, why do you allow the latter, which does so just as much? A term and its definition may be equated: they are commensurate, and wherever one occurs in a indoment you may substitute the other without detriment to its truth. But you cannot extend that rule to terms that have any less close relation: in other cases, you may be led into error by such substitution or you may not: the rule would not be infallible

We learn from Aristotle himself that other solutions than what he formulated were offered for some of the fallacies referred by him to the head of Accident's, and as Poste says', the fallacy per socidens has been generally misunderstood.' It has been every commonly expounded in a way that does not really distinguish it from the fallacy next to be considered, Secundum Quid. Indeed what has happened is that the notion of the former has been dropped, being somewhat ill defixed, and the name of the latter, being somewhat clums; so that what to-day is commonly called Accident is what the Aristotelian tradition called Secundum Quid. But because the tradition recognized them as two, a distinction between the direct and the conserve form of the latter fallacy was drawn, which is really quite unsubstantial.

 The fallacy of Secundum Quid, or—to give the formula in full—A dicto simpliciter ad dictum secundum quid, from which the argument a dicto secundum quid ad dictum simpliciter is sometimes

¹ The phrase is from Poste's ed. of Soph. El. (e. p. 78): cf. esp. his remarks on p. 158, from which the above interpretation and criticism are borrowed. Soph. El. xxiv.

distinguished as its converse is one of the subtlest and commonest sources of error. It consists in using a principle or proposition without regard to the circumstances which modify its applicability in the case or kind of case before us. Water boils at a terroperature of 212° Fahrenheit: therefore boiling water will be hot enough to cook an ego hard in five minutes : but if we aroue thus at an altitude of 5,000 feet, we shall be disappointed : for the height, through the difference in the pressure of the air qualifies the truth of our general principle. A proposition may be intended simpliciter or without analification . or it may be intended subject to analifications and reservations. In the latter alternative, we may proceed to apply it where the circumstances implied in our qualifications are not present; in the former, where there are circumstances present which onalify its applicability. In saving that a proposition may he intended simpliciter, it was not meant that it is intended as alsolutely universal: for the application of a principle true absolutely universally cannot of itself lead to error, and a respondent brought to admit a case inconsistent with a principle put forward thus absolutely would be convicted of having put forward more than be could sustain. It was meant that it is conceived to hold true normally, or in any circumstances that the speaker contemplates: the fallacy where there is an unfair confutation lies in extending it beyond those circumstances. But it is not only in disputation that the fallacy occurs. We are all of us at times guilty of it: we argue from principles that hold good normally, without even settling what conditions constitute the normal, or satisfying ourselves that they are present in the case about which we are arguing. Freedom is good, and therefore it is supposed that every community should have free institutions, though perhaps there are some races only fit for a very moderate degree of 'freedom'. A man should be allowed to do what he will with his own; and that is often urged as a conclusive argument against any interference either with his disposition of his property, or his education of his children. Paris did nothing wrong in carrying off Helen, for her father left her free to choose her husband : but the freedom allowed her extended only to her first choice, like the authority of her father. ² Cf. Dicey. Law and Opinion in England, p. 487, on the extension of

² Cf. Dicey, Law and Opinion in England, p. 487, on the extension of principles to fresh cases in 'judge-made law'. Cf. also Ar., Eth. Nic. c. z. 4, 11379 14-19.

Ar., Rhet. β. xxiv. 1401" 84, quoted by Poste, p. 117.

There are trivial examples of this as of any other fallacy, as that if it he maintained that an Ethiopian is black it is contradictory to say he has white teeth 1: 'Few men die over eighty: I am over eighty . therefore I shall probably not die 's Rut there is no fallacy more insidious than that of treating's statement which for many proposes is true as if it were true always and without qualification.

8. Ignoratio Elenchi means proving another conclusion than what is wanted. The name does not literally mean that, but 'ignorance of confutation' But the business of any one undertaking to confute a statement is to prove the contradictory; and if I prove anything else I show that I do not know what confutation requires. Of course every fallacious confutation shows that I am ignorant of. or ignore, what is required. But other fallacies have other defects: in this, the argumentation may be perfectly sound, and the sole defect lie in the fact that the conclusion proved does not confute the there maintained Or-since it makes no difference whether we record a man as undertaking to confute one thesis or to sustain another contradictory to it—we may say that the fallacy lies in proving what is not the precise conclusion which we are called upon to prove. Against a minister who proposes to put a small duty on corn to-day it is no sufficient answer to prove that the people are much more presperous under free trade than in the days when corn stood at 60 or 80 shillings a quarter; against a free-trader it is no sufficient answer to prove that foreign nations injure us by their tariffs. Subterfuces of that kind are however so frequent a resource of the orator, that it is hardly necessary to illustrate them. Every reader of Plato's Apology will remember how Socrates refused to appeal to his judges with tears and entreaties, or to bring his wife and children into court to excite their commiseration ; for his part

¹ Sonh. FZ. v. 167a 11.

The fallop here lies in referring to men over eighty a proposition which is only true of man simpliciter, via. that few of them die over eighty. Solutions however are possible, which would bring the argument under other bead.

The qualification may consist either in the presence of conditions not

In quantozion may consist either in the presence of conditions not contemplated in making the statement, or in the absence of some that were contemplated in making the statement, or in the absence of some that were the statement of the statemen verse fallacy. But it is clear that there is no difference in principle between

^{*} Cf. Soph. Et. vi. 168* 17 sq.

was to persuade them, if he could do it, of his innocence and not of his sufferings 1

Such appeals as Socrates declined to make are sometimes called the accumentum ad miscricordiam, arouments addressed to show that a man is unfortunate and deserves pity, when it ought to be shown that he is innecent or her the law on his side. Other favourite forms of irrelevant conclusion have also received special names. The best known is the accumentum ad tominem in which being called upon to confute an allegation. I prove something instead about the nerson who maintains it. The politician who attacks an opponent's mesenres by showing that they are inconsistent with his former oninions commits this fallacy: it is the same if I condemn Home Rule for Ireland on the ground that Parnell was an adulterer. But the accumentum ad komisem need not be altogether irrelevant. A barrister who meets the testimony of a hostile witness by proving that the witness is a notorious thief, though he does less well than if he could disprove his evidence directly, may reasonably be considered to have shaken it : for a man's character bears on his credihility. And sometimes we may be content to prove against those who attack us, not that our conduct is right, but that it accords with the principles which they profess or act upon. Christ replied to these who censured him for healing on the Sabbath, by asking which of them, if his ox or his ass had fallen into a ditch, would not pull it out on the Sabhath day. Their practice was sufficient to justify him to them, whatever were the true theory of our duties on the Sabbath. And Aristotle answers the Platonists, who held all vice to be involuntary, by showing that they could not discriminate in that respect between vice and virtue; there was no more reason for calling one involuntary than the other; virtue, however, they called voluntary; and whatever be the true state of the case. their position at least was not sustainable.3

4. The nature of Petitic Principii is better expressed in the English name, Begging the Question.4 It consists in assuming

what is to be proved, in order to prove it. To do this within the compass of a single syllogism-assuming in the premises the very thing to be proved and not merely some thing which depends on that for its proof-is only possible by the use of synonyma. If I aroue that C is A because R is A and C is R and if the middle term R is identical either with the major or the minor then I use the proposition to prove itself: for let B be the same as A: then. by substituting A for B in the minor premiss. I get 'C is A' as a premiss : or let B be the same as C: then by substituting C for B in the major premiss. I again get 'C is A' as a premiss: and in either case therefore the conclusion is among the premisses. Thus let the syllogism be that to give to beggars is right, because charity is a virtue : so far as charity is taken to include giving to beggars. we have no business to assume that it is a virtue: for the question whether it is a virtue and the question whether it is right are the same question: to call it a virtue is to call it right. Here the major premise, that virtue is right, is a tautology, and the minor contains the netitio. On the other hand, if I defend legacy duties hy saving that property passing by will queht to be taxed. I her the question in the major: for a legacy duty is a tax on property passing by will, and to say that such property should be taxed is only to assert in other words the justice of a legacy duty.1

But the fallacy is generally committed less abruptly. The premiss

his thesis; let the thesis, for instance, be that the Pope cannot remit the temporal punishment of sin in Purgatory; the opponent many not ask the respondent to admit that he can. If Purgatory the opponent many not ask the respondent to admit it, it is only a sophistical confustation; the respondent did not see what he was granking, and would have refused to great it if he respondent to affect by the owing that he cannot reasonably deapy something which does that: but because it sees the contradictory of it. It is quite fair to try to get a man to admit a general principle, and then to show that his thesis is inconsistent with it, provided that the general principle does not earlier reasonably deapy in the contradictory of the singular principle does not be applied to the determination of the matter, but of the very matter, in guestion. As occurring in a book or speech, where a man puts forward his own premises, and has not to get them by the admission of a repondent, it consists in assessing among the premises attlest the conclusion lated thin the book in the conclusion lated thin the book in Cf. Manuel's Adfr.eb.
App. E.

App. E.

'It is also possible to beg the question when the conclusion is negative, but then only in the major premiss; and to beg it in other figures than the first (for details see Posts, Soph. El., App. A). Cf. also sayres, p. 588, n. l.

unduly assumed is generally not the conclusion itself differently expressed, but something which can only be proved by means of the conclusion and aroning thus is often called aroning in a circle. If I around that early Tentonic societies were originally held together by kinship, because all societies were so held together originally 1 I might be accused of arguing in a circle: for the major premiss, it might be said, is only arrived at by enumeration: early Tentonic societies have to be examined in order to show that it is true. Of course to show that the generalization was not enumerative would be to rebut the accusation . but as we saw in discussing the view that all syllogism is netition principii every syllogism whose major premiss is an enumerative judgement is so.1 The circle is fairly manifest in such cases; but in others it may often escape the notice of its author. 'There are certain people,' says Dr. McTaggart , 'who look on all nunishment as essentially degrading. They do not, in their saner moods, denv that there may be cases in which it is necessary. But they think, if any one requires punishment, he proves himself to be uninfluenced by moral motives, and only to be governed by fear. . . . They look on all nunishment as implying deep degradation in some one .- if it is justified, the offender must be little better than a brute: if it is not justified, the brutality is in the person who inflicts it. This reasoning appears to travel in a circle. Punishment, they say, is degrading, therefore it can work no moral improvement. But this been the question. For if punishment could work a moral improvement, it would not degrade but elevate. The humanitarian argument alternately proves that punishment can only intimidate because it is brutalizing, and that it is brutalizing because it can only intimidate.' Romanes finds an example of petitio in an argument of Huxley's, adduced to show that all specific characters are adaptive.4 'Every variety which is selected into a species is favoured and preserved in consequence of being, in some one or more respects, better adapted to its surroundings than its rivals. In other words, every species which exists, exists in

Darsein and after Darsein, ii. 807.

¹ For the general statement see Sir Henry Maine, Early Institutions. p. 64.

p. 282, supra.

Studies in Hapsican Cosmology, § 142. By punishment here is meant the indiction of pain on a person because he has done wrong (§ 187). And it is of corporal punishment that we most often hear this view expressed.

virtue of adaptation, and whatever accounts for that adaptation accounts for the existence of the energies.' Here the fallacy lies in substituting, for 'every variety which is selected', 'every species which exists', the statement in the first clause is true for every variety which is selected, since selection means the survival of those best adapted to the conditions of life. But the question is whether every species which exists has originated by 'selection'. One more instance may be cited, from a work on the squaring of the circle called The Net to Crack by James Smith 1 Smith held the ratio of circumference to diameter to be 81, and proved it thus: 'I think you will not dare to dispute my right to this hypothesis. when I can prove by means of it that every other value of # will lead to the grossest absurdities; unless indeed you are prepared to dispute the right of Euclid to adopt a false line hypothetically, for the purpose of a reductio ad absurdum demonstration, in pure geometry.' That is, he argued first that if 81 be the right ratio, all other ratios are wrong; and then, that because all other ratios are wrong. St is the right ratio. And he conceived that he had established his conclusion by a reductio ad absordum-by showing that the denial of his thesis led to absurdity. But the absurdity, in such an argument, quest to be ascertained independently, whereas here it rests upon the assumption of the truth of what it is used to prove.

5. The fallacy of False Canse is incident to the reductio ad absurdum. That argument disproves a thesis by showing that the assumption of its truth leads to absurd or impossible consequences. or proves one by showing the same for the assumption of its falsity." In False Cause, the thesis alleged to be discredited is not really responsible for the absurd or impossible consequences, which would follow equally from the other premises, whether that were affirmed or denied. 'It is ridiculous to suppose that the world can be flat : for a flat world would be infinite, and an infinite world could not be circumnavigated, as this has been.' Here the supposition inconsistent with the fact of the circumnavigation of the world is not that the world is flat, but that it is infinite; it might

¹ Cf. de Morgan, Budget of Paradoxes, p. 827.
² James Smith argued, not that 'if A is false, B will be true: but B is las. . A is true'; but if A is true, B will be false—(as to which nothing) was known) - . . A is true .

be flat and still circumnavigable, if it were finite; the thesis of its flatness is therefore unfairly discredited.

From a passage in the Prior Analytics it would seem that Aristotle normaled this fullecy as of frequent compressed. But the fact that later writers have largely given a different meaning to the name snocests that it is not really a prominent type. It is often identified with the fallacy Post koc. ergo propter koc: i.e., supposing that one event is due to another merely because it occurred after it . as the countryman is said to have declared that the building of Tenterden Steenle was the cause of Goodwin Sands because the sands only appeared after the steenle was built. Such as Bacon truly gave, is the origin of almost every superstition—of men's astrological fancies, and their fancies about omens or dreams. The story which he quotes may well be repeated in his own words. 'Itaque recte respondit ille, qui, cum suspensa tabula in templo ei monetraretur corum qui vota solverant, quod naufractii periculo clapsi sint. atque interrogando premeretur, anne tum quidem deorum numen agrosceret, quaesivit denno. At ubi sunt illi devicti qui post vota nuncupata perierint?"

Inferences of this kind are undoubtedly both frequent and fallacies in the same sort of way as those enumerated by Aristotle. That is, it is a general or dislectical principle—a principle applicable in diverse sciences, and not exclusively appropriate in any: and it is a false principle, the application of which is as likely to lead to error as torth. Nor is it peculiar to this fallacy, that it can be expressed as a false principle. Equivocation proceeds on the false principle that a word is always used with the same meaning: decided, on the principle that whatever is predicated of a thing may be predicated of its attribute, and vice versa: Scensdaw Quid, on the principle that whate is true with certain qualifications is also true without them. And the fact that these different types of fallacious inference severally depend on a false, or mislanding, principle is

¹ Anal. Pri. β. xvii. 65° 88 rò δὶ μὴ παρὰ τοῦτο συμβαίστε τὸ ψεῦδος, ἐ παλλάκε τὸ τοῦς λόγοις εἰάθαμες λέγεις, ε.τ.λ. Cf. Posto's Soph. E7., App. B, on this passage.

on thu passage.

Nos. Ory, I. 46. Bacon cites the story in illustration of one of the 'Idola Tribus', the tandency to overlook or despise facts which do not agree with an opinion which we have once adopted. J. S. Mill would call this the fallacy of Non-observation (System of Lopic, V. iv).

what was meant by calling them loci of fallacy ! But the locus Post hor proper hor is not quite the same as that of Non cause pro cause : in other words, the type is a little different. In Fales Cause we are dealing with the logical sequence of premises and conclusion . the fallacy lies in connecting the conclusion with a particular premies which might, so far as getting the conclusion is concerned. have been equally well included or omitted; and because the conclusion is false, we erroneously infer this premiss to be false also. In Post hoe, ergo propter hoe we are dealing with the temporal relation of cause and effect: the fallacy lies in connecting the effect with a particular event which might equally well have happened or not happened, so far as the effect in question is concerned; and we erroneously suppose that the effect, which did occur, occurred because of that event. But if any one likes to use the name False Cause as equivalent to Post hoc, propter hoc, there is not much harm done : for the fallacy which Aristotle meant is not one that we have much occasion to speak of.

6. It is otherwise with the fallacy of the Consequent, which some modern writers have also misunderstood. For this is one of the very commonest, and we have already had occasion to notice it in discussing inductive reasoning. It consists in supposing that a condition and its consequent are convertible; that you may argue from the consequent to the condition, no less than vice versa. If a religion can elevate the soul, it can survive persecution; hence it is aroued that because it has survived persecution, such and such a religion must elevate the soul; or perhaps (for we may follow Aristotle 4 in including under the name both the forms of fallacy

- 1 The Sophistics Elenchi is the concluding book of Aristotle's Topics.
- e.g. de Morgan, Formal Logic, p. 267; Jevons, Elementary Lessons, p. 181. p. 486, supra.

p. 486, supra.

Cf. Soph. Bl. xxviii 181° 27 map 8 sal 6 rol Mellorov lóyor el yèp rè proofs \$200 dopin, to driver dies up \$2000, for al driver of observe, and devices. It is not form defeater papel dechotopes ("with this accords the argument of Melismes; for he thinks that if what is generated has beginning, argument or mensus; for se that that it was a generated as a beginning, what is ungenerated has not; so that if the heaven is ungenerated, it is also infinite. But this is not so; for the sequence is the other way'); i.e. from 'A is B' you cannot infer 'not A is not B', but only contrariwise, 'not B is not A'. It appears by the same chapter that Aristotle would bring the not.d. : t appear by the same canper tast Arastotic would oring the illicit, via, simple, conversion of an universal silicit, and implement under properties of the same silicit, and the same silicit, and some silicit properties of the same silicit properties and talkers in hypothetical, and Bordors and Camestre in sylicities possess and talkers in hypothetical, and Bordors and Camestre in sylicities might parhaps be inferred from the fact that he does not include Undistributed Middle and Illicit Process of the Major in his list of ophistical confrontations, to which hypothetical reasoning is liable) that because it is incapable of elevating the soul, it will succumb to persection. Sucfilacies are committed whenever a theory is assumed to be true for no better reason than that the facts exist, which should result if it were true—i.e. whenever verification is mistaken for proof 1; and whenever the redutation of an argument advanced in support of a theory is supposed by itself to be fatal to the theory. If it can be shown that no other theory accounts for the facts, or that no other argument can be advanced in support of the theory, then the matter is different; but without some reason to believe this, such inferences are worth nothing. Nevertheless, they are inferences which we are all very act to make.

7. There remains lastly the fallacy of Many Questions. This consists in putting questions in such a form that any single answer involves more than one admission. If one admission he true and another false and the respondent is pressed for a single answer. he is exposed to the risk of confutation, whatever answer he makes. 'The execution of Mary Queen of Scots was brutal and sacrilegious-was it, or was it not?' If it was brutal but not sacrilezious, what is a man to answer? He will be accused by saving no of denving the brutality, by saving yes of affirming the sacrilege. Sometimes, instead of submitting two problems for decision together, the question appears to submit only one; but that is one which would not arise except on the assumption of a certain answer to another; and so the respondent again cannot answer it without committing himself to more than he intended, or on a matter which has not been definitely submitted to him. Of this sort is the famous enquiry, 'Have you left off beating your

while he does include, under the name of the fallery of the Consequent, the corresponding though not identical errors which may be committed in hypothetical reasoning. It may be noted that such inferences would only not be fallacious where condition and consequent reciprocated—a relation which corresponds to that of commensuate terms in an universal affirmative judgment. Hence Aristotic surys that the fallery of the Consequent is brough! Fast fac, proper loc. If Goodern Sands were enamed by building Tenstands Research, they would have appeared, as at hy did, so soon as the steeple was built; but they might equally have done so, if the building of the steeple had nothing to do with thair appearance.

the Recyce and Magnetian of Cr. p. 486, septra.

This fallacy is 'logical', or formal; it can be expressed in symbols. So can argument in a circle sometimes be; e.g. if it is of the form 'A is B, B is C : A is C: and B is C because A is C and B is A'.

mother?' as well as any question that sake for the reason of what has not been admitted to be true. It is often recounted how Charles II saked the members of the Royal Society why a live fish placed in a howl already full of water did not cause it to overflow whereas a dead fish did so; and how they gave various ingenious reasons for a difference which did not exist. If one were to enquire why a protective system encourages the industry of the country which adopts it, the fallacy would be the same : there would perhaps he some diamete as to whether it is fallacious to ask how downers are made aware by their feelings of the presence of subterranean waters. It may be said that a respondent is always able to give an answer which will save him from any misconstruction : to the question ' Have you left off beating your mother?' the answer 'no' might seem to be an admission of the practice; but why should not a man reply 'I never becan it '? To this it may be rejoined, first, that in the old disputations, and in some situations, such as the witness-box, to-day, a man might be more or less precluded from 'explaining himself', and required to give a 'plain answer' to a question which does not admit of it. With the use of the fallacy under this sort of duress may be compared the custom of 'tacking' in the American legislature. The President of the United States can veto bills, and does veto them freely; but he can only veto a bill as a whole. It is therefore not uncommon for the legislature to tack on to a bill which the President feels bound to let pass a clause containing a measure to which it is known that he objects: so that if he assents, he allows what he disapproves of, and if he dissents, he disallows what he approves.1 But secondly, even where no unfair duress is employed, the practice of presupposing a certain answer to one question in the form of putting another throws the respondent off his quard, and makes him ant to admit without considering it what, if it had been explicitly submitted to his consideration, he might have doubted or denied.

The fallacy therefore is not a trivial one; such questions are a real source of error, when we put them to ourselves: of unfair confutation, when we put them to others. But it is doubtful whether it is a fallacy extra dictionem. For the ambiguity or unavoidable falsehood which must in some cases attach to the answer is a consequence of the way in which the question is

1 Bryce's American Commonwealth,

worded; and the same may be said of the acquiescence in false assumptions, into which in other cases we are entrapped.

The foregoing remarks have been directed to explain what are the types of fallacy which have been traditionally distinguished and are still many of them very commonly referred to by name The types are not all consily distinct frequent or important . but the original meaning of each name has been given as far as nossible, because nothing but misunderstanding can result when different writers employ such terminology each in his own meaning, and there did not for the most part seem sufficient reason to prefer any later interpretation for a standard. In a few cases later interpretations which have much to be said for them have been given as well. No doubt Fallacy is a subject on which successive generations to some extent need a new treatise; not because the principles change, but because the fields change in which they are most prolific. Many engogestive illustrations of the dominion which fallery holds in important subjects of contemporary thought may be found in the pages of Whately, Mill, or de Morgan. to which reference has already several times been made.

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